Review and Application of Model and Spectral Analysis Based Fault Detection and Isolation Scheme in Actuators and Sensors


1College of Engineering, Biju Patnaik University of Technology, Bhubaneswar, Odisha, India
2Department of Industrial Technology, Jordan College of Agricultural Sciences and Technology, California State University, Fresno, California, USA
3National Institute of Technology, Rourkela, India

Email address: skmohanty03@yahoo.com (S. K. Mohanty), nmahalik@gmail.com (N. P. Mahalik), bibhuti.biswal@gmail.com (B. B. Biswal)

Abstract: For condition monitoring of machineries and systems conventional method such as hardware or sensor based error checking scheme were in use. As the automated systems are becoming complex, recently most of the condition-monitoring schemes have been applying sophisticated analytical tools and methods to achieve improved performance. The objective of this paper is to demonstrate model based Fault Detection and Isolation (FDI) schemes for mechatronic systems and devices. First we have reviewed FDI approaches and implementation schemes. Then, we have developed two frameworks: model and spectral signature based for the implementation of FDI schemes. The model based feature estimation and spectral analysis based multiresolution methods are implemented in exemplar devices such as actuators and sensors used in mechatronic systems. Based on the frameworks, the diagnostics and isolation algorithms were developed using MATLAB code. The algorithms are capable of detecting and isolating faults within the systems. The study is comprehensive and the implementation scenarios can be extendible to many types of systems and devices used in the mechatronic domain.

Keywords: FDI, Model-Based, Spectral Analysis, Multiresolution, ANN, FL

1. Introduction

For condition monitoring of machineries and systems conventional method such as hardware based error checking [1, 15] has been very popular since long. As the automated systems are becoming complex, recently most of the condition-monitoring schemes have been applying sophisticated analytical tools and methods to achieve improved performance [2]. Review on various condition monitoring and FDI approaches can be found from [3]. In this paper we have presented sophisticated analytical methods and approaches in order to develop FDI algorithms which can be applied to a range of systems and devices. A brief review on model-based FDI technique for actuating systems is presented below. Primarily, the model-based approach prepares a model that facilitates generating residuals which are measured and tested statistically in order to compare with the logical normal patterns for decision making of fault symptoms as illustrated in the Fig. 1 [16-17].

Mechatronic systems are composed of actuators and sensors. We have applied model-based technique to actuators and multi-resolution spectral analysis methods to sensors. The objective is to detect faults in the motor during its operation. First, we reviewed a framework to define appropriate model equations in order to accommodate features capable of finding faults. Fig. 2 shows the schematic of model based FDI scenario. For detail derivation, refer [2-5]. Here, A(s) and B(s) are system matrix, u and y are
inputs and outputs respectively. The feature estimation process is based on a task that determines the dependencies between different measurable signals - expressed by mathematical models. Based on measured input/output signals the detection methods generate residuals and then estimate the feature for comparison with the normal features. The changes of features are detected and faults are isolated.

![Figure 2. Feature estimation method with minimum errors (a) Equation error; (b) Output error [3, 15, 17].](image)

### 2. Feature Estimation Based FDI for Actuation Valve Driven by Motor

In this experimental study, we developed a prototype to replicate the motor-actuation based valve control system as shown in Fig. 3. The main valve has two openings: left side opening and right side opening. There are two motors. Each motor drives its corresponding auxiliary valve which is interfaced with the main valve to either open the left side or right side based on the control need. This each motor drives the outflow valve either in positive or negative direction depending upon the amount of opening and closing need. The entire control strategy was implemented based on Distributed Control Scheme (DCS). Under this scenario

\[ \omega_r (t) = RI (t) ; R \] is the resistance of the coil and \( \psi_e \) flux linkage. Thus, flux is derived to be one of the auxiliary measurands featuring faults because the generated rotor torque is proportional to the effective magnetic flux linkage. Note that \( \psi_r < \psi_e \) and is given by \( \mathcal{S} (t) = \psi_t I (t) \). Similarly, the dynamic equation of the motor can be written as \( J \dot{\omega}_g (t) = \psi_r I (t) - \mathcal{S} (t) - \mathcal{L} (t) \), where \( J \) is called the moment of inertia. The friction torque becomes \( \mathcal{S} (t) = c_r \text{sign} (\theta_g) \) and load torque is \( \mathcal{L} (t) \). The expression \( \theta_g = \theta / v \) is the relationship between the gear ratio \( v \) and shaft position (\( \theta_g \)) and flap position (\( \theta_g \)). The value of \( v \) from the data sheet is 1294. Now the torque of the flap becomes \( \mathcal{L} (t) = c_r f (\theta_g) \). Let us formulate a model equation that can reflect the feature estimation scheme. A suggested formulation can be \( y(t) = \Delta (I) \theta \). The following expressions are written to describe the residuals; each is coupled from at least one measurands [3]. Respective residuals are considered as the image of the respective faults [5]. Several residuals can be combined to represent some form of composite faults. The important variables that are considered for measurement are voltage \( V \); current \( I \); friction \( c_r \), resistance \( R \), and position \( \theta = \phi \) [2-5].

\[
\begin{align*}
F_{\delta_1}(t) &= V(t) - RI(t) - \psi_e \omega_r (t) \\
F_{\delta_2}(t) &= \psi_r I(t) - J \omega_g (t) - c_r \text{sign} \omega_g (t) - c_r f (\theta_g) \\
F_{\delta_3}(t) &= V(t) - R / \psi_r (J \omega_g (t) + c_r f (\theta_g)) \\
F_{\delta_4}(t) &= \theta_g (t) - \theta_g (t) / v 
\end{align*}
\]

#### 2.1. Results

Previously we had implemented the FDI algorithm in DSP (Digital Signal Processor) platform, a centralized system, and presented the results in [4]. This work is a step forward to earlier work in that the control architecture and strategy have been implemented based on DCS (Distributed Control Systems) scheme rather than centralized. That is the FDI algorithm was embedded within the DCS architecture using fieldbus type technology. Once the model is developed, the feature estimation algorithm is written to identify abnormality in the features or parameters. In order to achieve this, two sub-processes are needed: classification and decision. ANN (Artificial Neural Network) based classification is very popular for nonlinear systems. The decision algorithm was implemented using FL (Fuzzy Logic) methods. Fig. 4 illustrates the FDI processes that include both learning and run-time phase.

![Figure 3. The prototype of motor-actuation based valve control system.](image)
some of the features were observed via estimation using the model equations. Finally, the fault signatures such as residuals were generated to isolate and localize the exact fault. Some of the experimental results are shown in Table 1. We also conducted the success rate of identifying the faults. The success rate in this laboratory based demonstration system was 100%.

Table 1. Feature deviation due to faults.

<table>
<thead>
<tr>
<th>Faults introduced</th>
<th>Estimation of some features</th>
<th>Residuals generated in percentage (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\hat{R}$</td>
<td>$\hat{c}_f$</td>
<td>$\hat{v}$ $\hat{\phi}$ $\hat{I}$ $\hat{F}<em>{r1}$ $\hat{F}</em>{r2}$ $\hat{F}<em>{r3}$ $\hat{F}</em>{r4}$</td>
</tr>
<tr>
<td>$\hat{c}_f$</td>
<td>$\hat{v}$</td>
<td>$\hat{\phi}$ $\hat{I}$ $\hat{F}<em>{r1}$ $\hat{F}</em>{r2}$ $\hat{F}<em>{r3}$ $\hat{F}</em>{r4}$</td>
</tr>
<tr>
<td>$\hat{v}$</td>
<td>$\hat{\phi}$ $\hat{I}$</td>
<td>$\hat{F}<em>{r1}$ $\hat{F}</em>{r2}$ $\hat{F}<em>{r3}$ $\hat{F}</em>{r4}$</td>
</tr>
<tr>
<td>$\hat{\phi}$</td>
<td>$\hat{I}$</td>
<td>$\hat{F}<em>{r1}$ $\hat{F}</em>{r2}$ $\hat{F}<em>{r3}$ $\hat{F}</em>{r4}$</td>
</tr>
<tr>
<td>$\hat{I}$</td>
<td>$\hat{F}<em>{r1}$ $\hat{F}</em>{r2}$ $\hat{F}<em>{r3}$ $\hat{F}</em>{r4}$</td>
<td></td>
</tr>
</tbody>
</table>

Figure 4. Experimental set up and algorithm development phases.

Figure 5. Feature estimation based FDI results (Residuals when the valve leaks): Residuals at 15-50% during normal operation. (a) leakage fault, (d) sensor offset positive, (e) sensor offset negative; (B) Residuals for positive offset on supply air.

The estimation in all experiment showed positive (+). Using the normalization method, we have set the threshold value (minimum) of the residual as 75%. The faults were introduced manually. The employed control scheme is closed loop based. Both ANN and FL algorithms were used to classify [6] and isolate [5] the faults, respectively.

2.2. Classification and Decision Using ANN and FL

The FDI phases are described in the Fig. 3. It can be stated that ANN forms the basis of classification, [4] while FL serves as the decision tool. [2]. Both classification and decision together are treated as residual evaluation phases of the FDI [6-7]. Residual evaluation is thus a part of fault isolation [8]. The goal of residual evaluation for FDI is to device whether a fault in a system under consideration has occurred avoiding wrong decision that cause false alarm. In order to reduce the false alarm rate, classification and decision by combination of ANN and FL, respectively are suggested. As a validation of the residual evaluation we conducted several experiments with the above actuator based valve control system. As another example, the Fig.5 shows some other faults corresponding to appropriate residuals. In particular, it is necessary to understand the leakage fault of
the valve when it is completely closed. The figure is self-explanatory and the results presented in Fig.4 and Fig.5 are based on the FDI algorithm represented in Fig.3. The classification and decision aspect of the algorithm is realized using ANN and FL toolset of the MATLAB software [9]. The mapping for a given input to an output using FL can be formulated by using a process called fuzzy inference. Fuzzy inference system is having wide range of applications in the fields such as automatic control, data classification, decision analysis, expert system and computer vision [10]. MATLAB has been designed with three functions namely plotfis, plotmf and gensurf which provides a high level view of the fuzzy inference system. All the fuzzy inference system information is contained in the MATLAB object known as FIS (Fuzzy inference system) structure. This structure is stored inside each GUI tool. This structure is examined by access functions such as getfis and setfis.

3. Second Experiment with Wheelchair

In considering advancements in computing platform and digital technology, this work studies FDI in actuating systems [11]. Actuators are a class of technological systems that always entail greater reliability. This work presents a study on two types of FDI approaches. They are model-based and spectral analysis.

3.1. Model-Based FDI

In the second experiment for the evaluation of the feature estimation based fault detection is a wheelchair shown in the Fig.6. Fig.7. shows schematic of the steering system.

Based on theoretical modeling it is perceived that the characteristic velocity will be the preferred choice as regards to a feature of this system [3-5]. Here the lane-change behavior is reflected through three behaviors such as normal-steering, under-steering and over-steering. The wheelchair has 3 wheels as shown in the Fig.7. By referring [3], the dynamic model equations of this wheelchair were presented in detail in [5] and [4]. The important model equations used in this paper can be written from [3]. Since this is a lane change scenario, the dynamics can be modeled considering lateral movement. The following terms are defined.

- \( a \): position error
- \( b \): lateral position error
- \( c \): vertical position error
- \( \psi \): yaw angle
- \( \Delta \): steering angle
- \( \Delta \alpha \): wheel angle
- \( F \): slip angle
- \( m \): mass
- \( I_1 \): moment of inertia
- \( V \): driving velocity
- \( S_1 \): front wheel stiffens
- \( S_2 \): rear wheel stiffness
- \( L_1 \): front axle length to C.G
- \( L_2 \): rear axle length to C.G
- \( \rho \): radius of rear tire
- \( F_1 \): force acting on rear tire

First, consider the characteristic equation as of a vehicle as follows.

\[
S^2 + C_1S + C_0 = 0
\]

Where,
The characteristic velocity \([3]\) can be written as follows.

\[
V^2(t) = \frac{S_i(t)S_j(t)}{m(S_i(t)L_2 - S_j(t)L_1)}
\]

The above characteristic expression that is used for stability is as follows.

\[
V^2 > \frac{1}{V_{\alpha}}
\]

The input and output model equations \([3]\) are as follows.

\[
\begin{bmatrix}
\dot{b} \\
\dot{\psi}
\end{bmatrix} = \begin{bmatrix}
s_1' - \frac{m v}{s_1 L_1} \\
\frac{s_1 L_1}{L_{1s}}
\end{bmatrix} \Delta s \\
\begin{bmatrix}
\dot{b}(t) \\
\dot{\psi}(t)
\end{bmatrix} = \begin{bmatrix}
1 & 0 \\
0 & 1
\end{bmatrix} \begin{bmatrix}
\dot{b} \\
\dot{\psi}
\end{bmatrix}
\]

The steering wheel angle during natural steering will be

\[
\dot{\psi}(t) = \frac{1}{\Delta a(t)} \left(\frac{v(t)}{i_s L_1} \right)^2
\]

With the measured steering wheel angle at the input, the velocity and the yaw rate at the output the characteristics velocity can be written as follows.

\[
\begin{bmatrix}
V_{\alpha}^2(t) \\
V(t)
\end{bmatrix} \left[1 - \frac{\Delta a(t)V(t)}{\dot{\psi}(t)i_s L_1}\right] = -V^2(t)
\]

### 3.2. Results

The overall objective of this research was to develop advanced diagnostic and prognostic method by making the systems more predictable and available through developing model-based dynamic health management algorithms. The developed algorithm utilizing model equations to estimate the features \([12]\) (both variables and parameters) by using sensor signals and refining it to a data infrastructure for FDI usage based in DCS implementation strategy. Thus the research not only demonstrates FDI scheme, but its implementation methods using advanced fieldbus type technology systems and architecture (e.g., DCS). The architecture can serve as basis for developing a framework for identifying fault symptoms before it occurs.

The work involves techniques for managing uncertainty and predictive modeling of future behavior. The steering behavior depends on the velocity. We set the nominal velocity as reference. 50% of nominal velocity either side was set as understeering and oversteering. Several sensors were calibrated and compensated beforehand in order to measure the measurands such as angle, acceleration, yaw rate and normal velocity. As mentioned in the equation, the effect of instability scenario was also introduced in the modeling. The wheelchair’s lane change behavior was studied multiple times. Similar to actuation valve, the residuals were generated and estimation was produced. Fig.8 shows the results corresponding to lane change behavior and its predictive model.

Figure 8. Results showing command signal (Joystick, measured signal (Sensor O/P), faulty driving behavior, and predictive driving behavior (non-faulty based on model based FDI).

### 3.3. Spectral Analysis based FDI

The wheelchair has many components responsible for its operation. The bottom part of the Fig. 6 depicts the movement of the joystick and the resulting output. One such essential component is the LVDT sensor which plays significant role in lane change behavior. It is an electromechanical transducer which is coupled to the wheelchair and it converts the joystick movement into the core movement. LVDT is encountered with different kind of fault, out of which the most common are overvoltage faults, core not moving fault and inductance or coil fault. Over- or under-voltage occurs when the applied voltage is in excess that cannot be handled by the primary coil of the LVDT.

Non-movement of core is associated with flux equivalency and corresponding differential voltages at both the coils. In this study, we have modeled the system where all these faults can have one index or signature that what we call inefficiency of the coil. It is assumed that the joystick makes slight deviations of about 8° with respect to the expected line while moving along a straight path. Due to this core movement there is an angle involved which is detected with the help of an angle sensor. The output of an angle sensor is a random signal as shown in Fig.9(a).
Scalogram of the non-faulty random signal we get is shown in Fig.9b.

The fault in the core takes place when the command is given by the joystick but the relative movement of the core stops. In our simulation study the random signal from an angle sensor and the dither signal are superimposed and its WT is computed using the MATLAB. The Fig.9(c) shows the superimposition of the random signal obtained from an angle sensor output and the LVDT fault (core not moving). It is clear from the figure that the WT is able to record the change in the frequency components, as well as their time localization.

4. Conclusions

This paper provides validation of different FDI schemes based on the results obtained through several experimental studies [13]. The studies were carried out for model based feature estimation and spectral analysis based multiresolution signal decomposition methods, respectively. First the feature estimation based FDI for actuating valve driven by two motors was illustrated. In this case the experimental study was carried out for an electrical motor. Several experiments were conducted with actuator based valve control system for the validation of residual evaluation. As a second example, in this paper a rehabilitation wheelchair was considered for feature estimation based fault detection evaluation. The objective was to detect and isolate the faults in steering actuators. The classification and confirmation of the faults are implemented with the help of Artificial Neural Network (ANN) and Fuzzy Logic (FL) [14]. Finally, the validation of multiresolution technique of a sensor was demonstrated. The failure modes were considered. The scalograms of the output signals with the faults signatures were examined and detected.

Acknowledgements

The authors acknowledge Prof. R. Isermann for developing the model based approaches for several dynamical systems. The model-based work is based on much of Prof. R. Isermann’s earlier work.

References


[18] Harbilas Bal and N. P. Mahalik, “Fault detection (FDI) in actuators, 32nd Annual Central California Research Symposium, California State University, April 6, Fresno, California.