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Mathematical and Kinetic Modelling for Convective Hot Air Drying of Sweet Potatoes (*Ipomoea batatas L*)

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Abstract: The kinetic modelling of thin layer drying is performed with various agricultural products such as seeds, grains, fruits and some plant species with economic importance. Sweet Potato ($Ipomoea\ batatas\ L$) is a widely consumed, and its industrialization is on the increase. The thin layer drying kinetics of sweet potato were experimentally investigated in a convective hot air dryer. Comparison was made between the experimental and model predicted moisture ratio by nonlinear regression analysis. Furthermore, the effect of drying temperature and slice thickness on the selected model constants was evaluated. From the experimental data obtained, it was observed that moisture ratio of the potato sample was directly proportional to the mass of the sample while the time of drying was inversely proportional and these two parameters (mass and time) were used to develop a mathematical model for the thin layer drying of sweet potatoes using a convective hot air dryer. The mathematical model developed was validated. The experimental data fitted the developed mathematical model and gave the Sum of Squares (SSE) value of 0.0001296 and coefficient of determination (R^2) as unity. The parameters obtained from the kinetic modelling of the selected models studied could be used in designing low cost dryers for optimum drying conditions.

Keywords: Sweet Potato, Moisture Ratio, Model Constant, Drying Kinetics, Thin Layer

1. Introduction

Drying operations had been applied for the reduction of moisture content in food materials for the prevention of microbial growth and deterioration, for shelf life elongation, to minimize packaging and improving storage for easy transportation. Although there are many ways in which drying can be achieved, the choice of a method depends on the material and the sanitary measures [1, 2]. Fresh sweet potatoes are highly perishable due to their high moisture content and their availability is seasonal, so in some countries they are processed into various products by drying [3]. Therefore, it is necessary to predict the removal of moisture content of the sample (product) for preservation to avoid deterioration or spoilage [4]. Sweet Potato (Ipomoea batatas L.) is a tuberous crop of great importance in the world economy and feeding. It is widely consumed fresh, and its industrialization is on the rise, especially in the production of starch and chips [5]. Potatoes are also the fourth most

important vegetable crop for human nutrition in the world [6]. Nigeria is among the major producers of potatoes, others are Uganda, China, Indonesia and Viet Nam [3]. Several investigators had proposed numerous mathematical models for the thin layer drying of many agricultural products and porous materials [7]. This process (thin drying method) is advantageous, because a full scale experimentation of different products and configurations of the drying system is time consuming and also costly [7]. Thin-layer equations are often used for a description of the drying kinetics for various types of porous materials. Thin-layer drying models that describe the drying phenomenon of biological materials fall mainly into three categories, namely, theoretical, semitheoretical and empirical. The first category takes into account only the internal resistance to moisture transfer, while the other two consider only the external resistance to moisture transfer between the product and the air [2, 8].

The aim of this study is to develop a mathematical model for predicting the thin layer drying conditions like mass and drying time using the hot air drying method and to fit experimental data to some selected kinetic models for the sweet potato under study.

2. Materials and Methodology

2.1. Preparation of Samples

The White Sweet Potatoes (*Ipomea batatas L.*) (Inyang UUH3729 (Uyo)) of the family of convolvulaceae were obtained from Itam market in Uyo, Akwa Ibom State and were identified in the department of Botany and Ecological Studies' herbarium. They were peeled and cut into a cylindrical shape of 30 mm in diameter using a locally fabricated peeler, after which they were sliced into various thickness of 2mm, 4mm, 6mm and 8mm

2.2. Drying Experiments

Drying operation was carried out with a hot air Oven (model Wiseven 105). The potato slices were placed in a single layer on a wire mesh tray and placed inside the oven at different temperatures of 40°C, 50°C, 60°C, and 70°C. The initial weight of the sample used in the drying process was 200g of the potatoes for the different thickness. The oven was switched on for 30 minutes [9], to simulate and keep the inside at required operating temperature, which gives steady state of operation before placing the samples inside the in oven every 30 minute interval. The wire mesh tray was removed from the oven and weighed using a digital weighing balance (Ohaus), [4, 10, 11]. The drying was continued until a constant weight was achieved under that drying condition. Aghbashlo *et al.* [6], [4, 12] among others asserted that moisture ratio could be determined from Equation (1):

$$MR = \frac{M_t - M_e}{M_o - M_e} = \exp(-kt) \tag{1}$$

where M_t is the moisture content at any time t

 M_o is the initial moisture content of the sample

 M_{e} is the equilibrium moisture content

k is the drying rate coefficient (reciprocal minutes)

t is the time (minutes),

According to Aghbashlo *et al.* [6], the value of M_e depends on the relative humidity and is negligible as the relative humidity is not constant throughout the entire drying process. Consequently, the moisture ratio was calculated according to the ASAE [13] standard as expressed in Equation (2):

$$MR = \frac{M_t}{M_o} \tag{2}$$

In order to determine the model(s) to predict the drying kinetics of sweet potato, the experimental moisture content data was used. The moisture content data for each drying process was estimated as a non-dimensional moisture ratio, due to the assumption of a uniform initial moisture content of all the samples [14, 15]. Furthermore, the best model(s)

describing the thin layer drying characteristic of potato was chosen as the one with the highest R^2 value and the lowest SSE value [16, 17 and 18]. The statistical error used to minimize the difference between the experimental and models predicted data in order to achieve a good fit was the Sum of squares error (SSE). The goodness of fit of the models was established using coefficient of determination (R^2).

The experimental moisture ratio of the potatoes was fitted into thirteen (13) thin layer models widely utilized in describing the drying behaviour of agricultural products [12] as shown in Table 1.

2.3. Moisture Content Determination

The oven dry method described by ASAE [13] was used to determine the average initial moisture content of the samples. The samples were initially weighed using an electronic balance having a sensitivity of 0.001 g and placed in an air oven for 24 hours at 105°C. After 24 hours, the samples were taken out of the oven and weighed to determine the final individual weight. The average values of the initial mass and final mass were used to calculate the moisture content expressed on a wet basis as shown in Equation 3. The process was repeated three times and the average was calculated.

Moisture content
$$(MC) = \frac{W_i - W_f}{W_i} \times 100$$
 (3)

Where W_i is the average initial weight of the sample and W_f , is the average final weight of the sample.

2.4. Model Development

Amer *et al.* [19, 20] applied multiple linear regression analysis to establish mathematical equations for the drying kinetics which relate the drying process with the affecting factors. Literatures had established that the non – linear regression (or equation) technique could be used to develop a model which takes care of many variables [21, 22].

In developing the empirical model for drying of sweet potatoes, the following assumptions were made:

- a. The moisture movement is only diffusion since most agricultural products use diffusion theory and this will be unidirectional.
 - b. The drying process is isothermal.
 - c. Shrinkage is neglected.
 - d. Materials to be dried is spherical but thin in size
- e. Coefficient factor (a_o), is independent of moisture concentration

For the development of the correlation in this study, the Moisture ratio (MR) depends inversely on time (as shown in Equation 4) and directly on mass (as shown in Equation 5). Based on this assertion, the relationships of MR with the drying parameters are presented in Equations (4) and (5):

(a)
$$MR \alpha \frac{1}{t}$$
 (4)

(b)
$$MR \alpha M$$
 (5)

Thus, the proposed correlation considers the proportionality of the MR to the different drying factors (mass and time); as presented in Equations 4 and 5.

In other words, the moisture ratio is expressed as a function of the mentioned parameters in Equation 6:

$$MR = f(t, M)$$
 (6)

Equations 4 and 5 can be expanded in the basic form of nonlinear multivariable algebraic expression as given in Equation 7:

$$MR = \alpha_o \left(M^{\alpha_1} \cdot t^{-\alpha_2} \right) \tag{7}$$

Alternatively, we will have

$$MR = \alpha_o \left[\frac{M^{\alpha_1}}{t^{\alpha_2}} \right] \tag{8}$$

Applying the logarithmic transformation to linearize the Equation 8; we obtain

$$Log(MR) = Log(\alpha_o) + \alpha_1 Log(M) - \alpha_2 Log(t)$$
 (9)

where α_o is a coefficient while α_1 and α_2 are exponential

constants of the drying parameters.

The variables α_o through α_2 could be determined iteratively using multivariable numerical optimization method. To determine these variables, existing literature indicates that, there are several approaches to performing this iterative estimation, namely, Gauss-Newton, the Marquardt-Levenberg, the Nelder-Mead, the steepest descent, General Reduced Gradient (GRG) protocol [23-26].

To estimate the variables in the Equation 8 iteratively, these parameters (mass and time) were obtained experimentally. Then the unknown coefficient (α_0) and the exponential constants α_1 and α_2 were solved iteratively using GRG protocol in the Microsoft Excel SOLVER. To validate the correlation, its prediction was compared with the experimental data and some authors' correlation predictions. Also, the closeness of the correlation's predictions and experimental data were established using coefficient of determination (\mathbb{R}^2).

2.5. Kinetic Models for Thin Layer Drying

Some kinetic models with parameters ranging from one to six were selected for fitting to the experimental data under study (see Table 1). The parameters were determined using the nonlinear regression method.

Table 1. Mathematical models applied to the thin layer drying of various agricultural products.

S/N	MODEL NAME	MODEL EQUATION	REFERENCE
1.	Newton/Lewis	$MR = \exp(-kt)$	[27]
2.	Page	$MR = \exp(-kt^n)$	[28]
3.	Modified Page	$MR = \exp\left[\left(-kt\right)^n\right]$	[29]
4.	Henderson and Pabis	$MR = a \exp(-kt)$	[30]
5.	Logarithmic	$MR = a \exp(-kt) + c$	[31]
6.	Two Term	$MR = a \exp(-k_0 t) + b \exp(-k_1 t)$	[32]
7.	Two Term Exponential	$MR = a \exp(-kt) + (1-a) \exp(kat)$	[29]
8.	Singh et al	$MR = \exp(-kt) - akt$	[33]
9.	Aghabashlo Model	$MR = \exp\left(\frac{k_1 t}{1 + k_0 t}\right)$	[34]
10.	Midilli et al	$MR = a \exp\left(-kt^n\right) + bt$	[35]
11.	Hii et al	$MR = a \exp(-k_1 t^n) + b \exp(-k_2 t^n)$	[36], [43]
12.	Demir et al	$MR = a \exp(-kt)^n + b$	[37]
13.	Modified Midilli	MR = exp(-kt) + bt	[38]

a, b, c, k, k₁, k₂, and n are model constants

2.6. Statistical Analysis

The following statistical measures were used in determining the goodness of fit for the model [2, 12, 39]:

(i) Chi Square
$$(\chi^2) = \sum_{i=1}^n \frac{(MR_{\text{exp}} - MR_{pre})^2}{N - n}$$
 (10)

(ii) Residual Sum of Square (RSS) =
$$\sum_{i=1}^{n} (MR_{exp} - MR_{pre})^{2}$$
 (11)

(iii) Mean Bias Error (MBE) =
$$\frac{1}{N} \sum_{i=1}^{N} \left(MR_{\text{exp}} - MR_{pre} \right)^2$$
 (12)

(iv) Root Mean Square Error
$$(RMSE) = \left[\sum_{i=1}^{n} \frac{1}{N} (MR_{exp} - MR_{pre})^2\right]^{\frac{1}{2}}$$
 (13)

(v) Coefficient of Determination
$$(R^2) = 1 - \left[\frac{(MR_{\text{exp}} - MR_{pre})^2}{(MR_{\text{exp}} - MR_{preAVER})^2} \right]$$
 (14)

(vi) Sum of Square Error(SSE) =
$$\frac{1}{N} \sum_{i=1}^{N} \left(\frac{MR_{\exp} - MR_{pre}}{N} \right)^{2}$$
 (15)

3. Result and Discussion

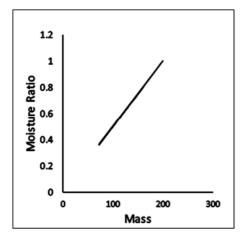


Figure 1. Moisture Ratio Versus Mass.

For the experiment, the experimental moisture content data were used to determine the moisture ratio. Thus, it was observed that Moisture Ratio (MR) depends directly on the mass (as shown in Figure 1) and inversely on time (as shown in Figure 2). In Figure 1, the moisture ratio increases as the

mass increased while Figure 2 shows that the moisture ratio decreases as the time increased. Figure 1: Moisture Ratio Versus Mass Figure 2: Moisture Ratio Versus Time

The experimental data of sweet potato were fitted into thirteen thin layer drying models and these were compared with the developed model using the statistical indicators of R^2 and SSE as listed in Table 2. The best model was the one with the highest R^2 value and the lowest SSE value.

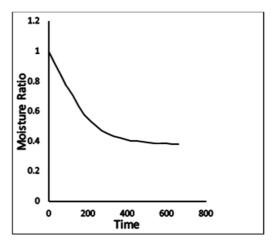


Figure 2. Moisture Ratio Versus Time.

Table 2. Statistical Comparison of selected models for drying of sweet potato.

<u> </u>	Slice thickness (mm)	Drying air temperature								
Model name		40°C		50°C		60°C		70°C		
		\mathbb{R}^2	SSE	\mathbb{R}^2	SSE	\mathbb{R}^2	SSE	R ²	SSE	
Lewis Model	2	0.7685	0.1307	0.1318	0.1752	0.9058	0.2051	-0.4733	0.1572	
	4	0.7452	0.1445	0.4929	0.2408	0.9109	0.2167	0.1295	0.1944	
	6	0.9494	0.0445	0.3027	0.1118	0.7000	0.1299	0.1295	0.1944	
	8	0.9878	0.1752	0.8443	0.1003	0.6800	0.1735	0.5840	0.1108	
Page	2	0.9358	0.0361	0.8782	0.0243	0.8225	0.0293	0.7895	0.0224	
	4	0.9576	0.0239	0.9929	0.0599	0.8701	0.0358	0.8466	0.0342	
	6	0.9972	0.0136	0.9537	0.0312	0.9293	0.0306	0.8466	0.0342	
	8	0.9928	0.0064	0.9808	0.0123	0.9437	0.0305	0.9480	0.0230	
Modified page	2	0.1307	0.1307	0.1318	0.1752	0.2377	0.2051	-0.4733	0.1572	
	4	0.1445	0.1445	0.4929	0.2408	0.7980	0.2167	0.1295	0.1944	
	6	0.0445	0.0445	0.8342	0.1118	0.9035	0.1299	0.1295	0.1944	
	8	0.0119	0.0119	0.8443	0.1003	0.9606	0.1735	0.7493	0.1108	

		Drying air temperature								
Model name	Slice thickness (mm)	40°C		50°C		60°C		70°C		
		\mathbb{R}^2	SSE	\mathbb{R}^2	SSE	R ²	SSE	\mathbb{R}^2	SSE	
Two Term	2	0.9981	0.0019	0.9991	0.0002	0.9950	0.0008	0.9998	0.0000	
	4	0.9950	0.0028	0.9961	0.0018	0.9990	0.0005	0.9974	0.0006	
	6	0.9979	0.0007	0.9976	0.0016	0.9347	0.0650	0.9974	0.0006	
	8	0.9885	0.0103	0.9999	0.0000	0.9996	0.0002	0.9988	0.0005	
Two Term Exponential	2	0.0059	0.9896	0.8837	0.0233	0.7876	0.0351	0.7552	0.0261	
	4	0.0088	0.9844	0.9411	0.0280	0.8723	0.0280	0.8681	0.0295	
	6	0.0005	0.9999	0.9949	0.0034	0.9831	0.0073	0.8681	0.0295	
	8	0.0015	0.9983	0.9897	0.0066	0.9731	0.0146	0.9859	0.4663	
Hii et al	2	0.9739	0.0147	0.9999	0.0000	0.9999	0.0000	0.9957	0.0005	
	4	0.9963	0.0021	0.9651	0.0165	1.0000	0.0001	0.9999	0.0000	
	6	0.9947	0.0066	0.9999	0.0001	0.9999	0.0001	0.9434	0.0126	
	8	1.0000	0.0000	0.9999	0.0000	0.9998	0.0001	0.9998	0.0001	
Agbashalo	2	0.9757	0.0136	0.9642	0.0072	0.9377	0.0103	0.9102	0.0096	
Ü	4	0.9871	0.0073	0.9522	0.0227	0.9619	0.0113	0.9449	0.0123	
	6	0.9964	0.0048	0.9834	0.0112	0.9757	0.0105	0.9449	0.0123	
	8	0.9962	0.0034	0.9979	0.0014	0.9867	0.0072	0.9848	0.0067	
Singh	2	0.7685	0.1307	0.1227	0.1757	0.2377	0.2051	0.4733	0.1572	
	4	0.7452	0.1445	0.4929	0.2408	0.4009	0.2167	0.1295	0.1944	
	6	0.9041	0.0445	0.8342	0.1118	0.6975	0.1309	0.1295	0.1944	
	8	0.9868	0.0119	0.8443	0.1003	0.6760	0.1751	0.7493	0.1108	
Demir et al	2	0.9966	0.0019	0.9995	0.0002	0.9997	0.0000	0.9998	0.0000	
	4	0.9952	0.0027	0.9961	0.0018	0.9990	0.0005	0.9974	0.0006	
	6	0.9983	0.0005	0.9976	0.0016	0.9989	0.0011	0.9974	0.0006	
	8	0.9990	0.0009	0.9999	0.0001	0.9999	0.0002	0.9988	0.0005	
Midilli et al	2	0.9976	0.0013	0.9957	0.0009	0.9974	0.0004	0.9944	0.9974	
	4	0.9443	0.0316	0.9941	0.0028	0.9968	0.0020	0.9950	0.9968	
	6	0.9806	0.0401	0.9995	0.0003	0.9948	0.0079	0.9935	0.9948	
	8	0.9994	0.0005	0.9999	0.0001	0.9979	0.0059	0.9846	0.9979	
Modified Midilli	2	0.9968	0.0018	0.9909	0.0018	0.9776	0.0037	0.9687	0.0033	
	4	0.9970	0.0017	0.9883	0.0056	0.9921	0.0031	0.9859	0.0031	
	6	0.9997	0.0002	0.9995	0.0003	0.9994	0.0006	0.9859	0.0031	
	8	0.9996	0.0004	0.9993	0.0005	0.9996	0.0008	0.9859	0.0003	
Henderson and Pabis	2	0.8669	0.0749	0.7357	0.0528	0.6494	0.0578	0.6212	0.0403	
	4	0.8917	0.0611	0.7455	0.1208	0.7217	0.0766	0.8817	0.0683	
	6	0.9665	0.0295	0.9024	0.0658	0.8499	0.0650	0.6940	0.0683	
	8	0.9885	0.0103	0.9362	0.0409	0.8879	0.0765	0.8810	0.0525	
Logarithmic	2	0.9966	0.0019	0.9991	0.0002	0.9997	0.0000	0.9999	0.0001	
	4	0.9952	0.0027	0.9988	0.0018	0.9981	0.0005	0.9999	0.0001	
	6	0.9992	0.0007	0.9976	0.0016	0.9974	0.0011	0.9997	0.0001	
	8	0.9990	0.0009	0.9995	0.0001	1.0000	0.0002	0.9999	0.0005	

From Table 2 it was observed that the statistical measurements of some selected models for drying sweet potatoes gave good fit, but when compared together Hii *et al* model gave higher values of coefficient of determination (R²) of 0.9999 for the various thickness and different drying temperatures studied and was also found to have corresponding low values for sum of squares calculated as they tended towards zero. This observation was found to be in agreement with the findings of other researchers [12]. Singh model was the least among the fitted models.

The model with the highest value for R² was selected to

describe the drying curves, as well as the lowest of values of the Sum of squares error (SSE) gave the best fit.

The quality of the developed model has been evaluated using different statistical criteria. Table 3 shows that the value of R^2 is 0.999963 while other error functions are RMSE 0.001022, MBE -0.10673, SSE -0.000001055 and Chi square (χ^2) 0.000001044475. The values of R^2 and other statistical measures were better compared to the findings of several previous works in fitting the model to the experimental data [4, 9].

Table 3. The statistical values of the developed model for this study.

\mathbb{R}^2	RSS	RMSE	MBE	SSE	\mathbf{x}^2
0.999963	0.000999264	0.001022	-0.10673	1.05519E-06	1.04475E-06

However, two parameters [12, 40] were used to develop a model that relates moisture ratio (MR) to mass (M) and time (t) for drying sweet potato which this research work has been able to establish. These constants (0.005263, 0.991698 and

0.002583) were obtained using solver (after the iteration with the GRG protocol).

The empirical model developed is given as Equation 16:

$$MR = 0.005263 \left[\frac{M^{0.991698}}{t^{0.002583}} \right]$$
 (16)

The individual constants of the selected thirteen models for the drying sweet potato in this study were presented in Table 4. When the rate constant is small, the evaporation rate is so small that the moisture content decreases very slowly [41]. Also, the drying coefficient gives a measure of the time required to dry out the moisture content from the material [42]. From the results determined, the rate constants are very small (less than 1) which means the evaporation rates involved in drying sweet potato were slow apart from Hii *et al* model where K was up to 5 at 70°C for 2mm. Moreover, the other model constants for some thin layer drying kinetic models were small apart from Midilli and Hii *et al* where some constants were above 1.

The application of these are useful engineering tool for the design of equipment and optimization.

Table 4. Selected Models with their Constants at different Temperatures and Thickness.

Model	Temperatu	ire							
name	40°C		50°C			60°C		70°C	2
		Model constant	R ²	Model constant	R ²	Model constant	R ²	Model constant	\mathbb{R}^2
Lewis	2	K=0.002136	0.7680	K=0.004285	0.1310	K=0.005194	0.9050	K=0.007076	-0.4730
	4	K=0.002015	0.7450	K=0.003128	0.4920	K=0.003462	0.9100	K=0.005212	0.1290
	6	K=0.001536	0.9490	K=0.002609	0.3020	K=0.003449	0.6990	K=0.005212	0.1290
	8	K=0.00123	0.9870	K=0.001713	0.8440	K=0.002607	0.6790	K=0.003412	0.5830
Page	2	K=0.018752	0.9350	K=0.077578	0.8780	K=0.1108	0.8220	K=0.138555	0.7890
		n = 0.632172		n = 0.456215		n = 0.411401		n = 0.394533	
	4	K=0.021606	0.9570	K=0.04505	0.9920	K=0.065875	0.8700	K=0.087611	0.8460
	•	n = 0.603662	0.5570	n = 0.531598	0.5520	n = 0.467224	0.0700	n = 0.4611	0.0100
	6	K=0.00562	0.9970	K = 0.017589	0.9530	K=0.03179	0.9290	K=0.087611	0.8460
	· ·	n = 0.790284	0.5570	n = 0.673063	0.7550	n = 0.601256	0.5250	n = 0.4611	0.0100
	8	K=0.002294	0.9920	K = 0.013988	0.9800	K=0.030142	0.9430	K = 0.028473	0.9470
	O	n = 0.90063	0.7720	n = 0.655464	0.7000	n = 0.580559	0.5450	n = 0.619668	0.5470
Modified	2	K=0.032679	0.7680	K=0.031742	0.7450	K=0.048044	-0.2370	K=0.059482	-0.4730
page	2	n = 0.065358	0.7000	n = 0.063485	0.7430	n = 0.108099	-0.2370	n = 0.118964	-0.4/30
	4	K=0.031742	0.7450	K=0.033944	0.9490	K=0.041604	0.7980	K=0.051048	0.1290
	4	n = 0.063485	0.7430	n = 0.045259	0.9490	n = 0.083209	0.7980	n = 0.102097	0.1290
	6	K=0.033944	0.9490	K=0.045284	0.9860	K=0.041525	0.9030	K=0.051048	0.1290
	6	n = 0.045259	0.9490	n = 0.02717	0.9800	n = 0.083049	0.9030	n = 0.102097	0.1290
	0	K=0.045284	0.0060	K=0.031742	0.7450	K=0.036105	0.0600	K=0.041302	0.7400
	8	n = 0.02717	0.9860	n = 0.063485	0.7450	n = 0.072209	0.9600	n = 0.082604	0.7490
		a = 0.70346		a = 0.707484		a = 0.813895		a = 0.92369	
Logarithmic	2	K = 0.00661	0.9960	K = 0.016705	0.9990	K = 0.023185	0.9990	K = 0.032999	0.9990
C		c = 0.366044		c = 0.359283		c = 0.341934		c = 0.332617	
		a = 0.652812		a = 0.795417		a = 0.718074		a = 0.116225	
	4	K = 0.005429	0.9950	K = 0.010947	0.9980	K = 0.013953	0.9980	K = 0.008653	0.9990
		c = 0.34956		c = 0.323369		c = 0.363798		c = 0.308695	
		a = 0.730995		a = 0.760523		a = 0.751903		a = 0.814707	
	6	K = 0.003154	0.9990	K = 0.006265	0.9980	K = 0.009609	0.9970	K = 0.019199	0.9990
		c = 0.299462		c = 0.289745		c = 0.30976		c = 0.311617	
		a = 0.767738		a = 0.631224		a = 0.708956		a = 0.73754	
	8	K = 0.002124	0.9990	K = 0.003879	0.9990	K = 0.00728	0.9990	K = 0.008754	0.9990
		c = 0.261943		c = 0.338606		c = 0.319596		c = 0.301264	
Henderson		a = 0.851751		a = 0.69215		a = 0.63344		a = 0.603394	
and Pabis	2	K = 0.00164	0.8660	K = 0.002304	0.7350	K = 0.002419	0.6490	K = 0.003036	0.6210
unu 1 uo10		a = 0.827938		a = 0.747359		a = 0.708791		a = 0.660201	
	4	K = 0.001479	0.8910	K = 0.002005	0.7450	K = 0.001939	0.7210	K = 0.002738	0.8820
		a = 0.934434		a = 0.855444		a = 0.799534		a = 0.660205	
	6	K = 0.001377	0.9660	K = 0.002082	0.9020	K = 0.002473	0.8490	K = 0.002738	0.6940
		a = 0.980114		a = 0.864499		a = 0.793157		a =0.811336	
	8	K = 0.00114	0.9880	K = 0.001343	0.9360	K = 0.001833	0.8870	K = 0.002507	0.8810
		a = 1.050136		a = 3.098222		a = 4.428267		a = 5.989524	
		K = 0.00528		K = 0.524682		K = 0.729246		K = 0.896964	
Midilli	2	n = 0.951291	0.9980	n = 0.284328	0.9960	n = 0.266459	0.9970	n = 0.266202	0.9940
		b = 0.000473		b = 0.00048		b = 0.00061		b = 0.000878	
		a = 1.797361		a = 1.21959		a = 2.524963		a = 1.727501	
		K = 0.312868		K = 0.02685		K = 0.372856		K = 0.15133	
	4	n = 0.256263	0.9440	n = 0.737562	0.9940	n = 0.320272	0.9970	n = 0.502302	0.9950
		b = 3.96E-05				b = 0.000415		b = 0.000626	
				b = 0.000478					
	6	a = 1.78469	0.0010	a = 1.013301 $V = 0.003046$	0.0000	a = 3.560496 $V = 0.606871$	0.0050	a = 3.690931 $V = 0.571427$	0.0020
	6	K = 0.217979	0.9810	K = 0.003946	0.9990	K = 0.606871	0.9950	K = 0.571427	0.9930
		n = 0.294226		n = 1.014267		n = 0.242032		n = 0.299485	

Model	Temperatu 40°C	ire	500C			60°C		70°C	
name		Model constant	50°C R ²	Model constant	\mathbb{R}^2	Model constant	\mathbb{R}^2	Model constant	R ²
		b = 2.11E-05		b = 0.0004		b = 0.000149		b = 0.000512	
		a = 1.024667		a = 1.033973		a = 2.288927		a = 3.683419	
	8	K = 0.001628	0.9990	K = 0.006937	0.9990	K = 0.332296	0.9980	K = 0.664916	0.9850
	O	n = 1.007941	0.5550	n = 0.836983	0.7770	n = 0.296599	0.7760	n = 0.222597	0.7650
		b = 0.000182		b = 0.000265		b = 0.000119		b = 7.6E-05	
Modified		K = 0.00294	0.0050	K = 0.016046	0.0010	K = 0.021219	0.0500	K = 0.025195	0.0600
Midilli	2	n = 1.051711	0.9970	n = 0.862239	0.9910	n = 0.844273	0.9780	n = 0.865174	0.9690
		b = 0.000504 K = 0.004948		b = 0.000812 K = 0.006285		b = 0.000887 K = 0.011862		b = 0.001176 K = 0.015528	
	4	n = 0.934499	0.9970	n = 0.98656	0.9880	n = 0.889376	0.9920	n = 0.90192	0.9860
	7	b = 0.000387	0.5570	b = 0.000544	0.7660	b = 0.000695	0.5520	b = 0.000783	0.7000
		K = 0.001748		K = 0.00337		K = 0.005872		K = 0.015528	
	6	n = 1.047153	0.9990	n = 1.041626	0.9990	n = 1.00206	0.9990	n = 0.901919	0.9860
		b = 0.000273		b = 0.000407		b = 0.000569		b = 0.000783	
		K = 0.001044		K = 0.005111		K = 0.006548		K = 0.006388	
	8	n = 1.083479	0.9990	n = 0.885295	0.9990	n = 0.927841	0.9990	n = 0.975357	0.9990
		b = 0.000214		b = 0.000282		b = 0.000416		b = 0.000521	
		a = 0.703462		a = 0.707487		a = 0.813896		a = 0.982221	
Demir et al	2	k = 0.087816	0.9970	k = 0.120899	0.9990	k = 0.162781	0.9990	k = 0.172117	0.9990
Denni et ai	2	n = 0.075271	0.5570	n = 0.13817	0.7770	n = 0.142433	0.5550	n = 0.200803	0.7770
		b = 0.366046		b = 0.359282		b = 0.341934		b = 0.334773	
		a = 0.652814		a = 0.795415		a = 0.718074		a = 0.814706	
	4	k = 0.079586	0.9950	k = 0.090611	0.9960	k = 0.139763	0.9990	k = 0.195952	0.9970
		n = 0.068217		n = 0.12081		n = 0.099831		n = 0.097976	
		b = 0.349562		b = 0.323369		b = 0.363798		b = 0.311617	
		a = 0.737187		a = 0.760524		a = 0.751901		a = 0.814707	
	6	k = 0.180402	0.9980	k = 0.084618	0.9980	k = 0.089486	0.9990	k = 0.107327	0.9970
		n = 0.01804 b = 0.304659		n = 0.074041 $b = 0.289745$		n = 0.107383 b = 0.30976		n = 0.178879 b = 0.311617	
		a = 0.767729		a = 0.651503		a = 0.708958		a = 0.73754	
		k = 0.043108		k = 0.060404		k = 0.708938 k = 0.246302		k = 0.100022	
	8	n = 0.049266	0.9990	n = 0.069033	0.9990	n = 0.029556	0.9990	n =0.087519	0.9990
		b = 0.261953		b = 0.345808		b = 0.319596		b = 0.301264	
		a = 0.703463		a = 0.707484		a = 0.339387		a = 0.982216	
		$K_0 = 0.00661$		$K_0 = 0.016705$		$K_0 = 4.86E-07$		$K_0 = 0.034562$	
Two Term	2	b = 0.366046	0.9980	b =0.359282	0.9960	b = 0.711025	0.9950	b = 0.334773	0.9990
		$K_1 = 0$		$K_1 = 0$		$K_1 = 0.020375$		$K_1 = 0$	
		a = 0.353184		a = 0.795408		a = 0.718074		a = 0.814711	
	4	$K_0 = 7.62E-07$	0.0050	$K_0 = 0.010947$	0.0060	$K_0 = 0.013953$	0.0000	$K_0 = 0.019199$	0.0070
	4	b =0.659939	0.9950	b = 0.323368	0.9960	b = 0.363798	0.9990	b = 0.311617	0.9970
		$K_1 = 0.005598$		$K_1 = 0$		$K_1 = 0$		$K_1 = 0$	
		a = 0.299455		a = 0.289739		a = 0.799531		a = 0.311618	
	6	$K_0 = 0$	0.9980	$K_0 = 0$	0.9980	$K_0 = 0.002473$	0.9350	$K_0 = 0$	0.9970
	O	b = 0.731	0.7700	b = 0.760512	0.7700	b = 0.008	0.7550	b = 0.81471	0.5570
		$K_1 = 0.003154$		$K_1 = 0.006265$		$K_1 = 1.155609$		$K_1 = 0.019199$	
		a = 0.008		a = 0.364922		a = 0.319592		a = 0.737536	
	8	$K_0 = 0.98011$	0.9890	$K_0 = 6.11E-05$	0.9990	$K_0 = 0$	0.9990	$K_0 = 0.008754$	0.9990
		b = 0.001187		b = 0.634302		b = 0.708948		b = 0.301264	
		$K_1 = 0.010553$		$K_1 = 0.004312$		$K_1 = 0.007279$		$K_1 = 0$	
Singh	2	K = 0.002136 a = 0	0.7680	K = 0.004374	0.1227	K = 0.005194 a = 0	-0.2380	K = 0.007076	-0.4730
		a = 0 K = 0.002015		a = 0 $K = 0.003128$		a = 0 $K = 0.003462$		a = 4.83E-07 K = 0.004	
	4	a = 0	0.7450	a = 0	0.4930	a = 0	-0.4010	a = 0.005212	0.1300
		K = 0.001536		K = 0.002609		K = 0.003537		K = 0.005212	
	6	a = 0	0.9040	a = 0	0.8340	a = 0	0.6970	a = 0	0.1300
		K = 0.00123		K = 0.001713		K = 0.002685		K =0.003412	
	8	a = 0	0.9870	a = 0	0.8440	a = 0	0.6760	a = 0	0.7490
	2	$K_1 = 0.004263$	0.0500	$K_1 = 0.012863$	0.0740	$K_1 = 0.017325$	0.0200	$K_1 = 0.023411$	0.0100
Agbashalo	2	$K_2 = 0.002529$	0.9760	$K_2 = 0.009147$	0.9640	$K_2 = 0.012091$	0.9380	$K_2 = 0.015938$	0.9100
	4	$K_1 = 0.004213$	0.0050	$K_1 = 0.007871$	0.0500	$K_1 = 0.010318$	0.0620	$K_1 = 0.014987$	0.0450
	4	$K_2 = 0.002563$	0.9870	$K_2 = 0.004711$	0.9520	$K_2 = 0.007375$	0.9620	$K_2 = 0.009242$	0.9450
	($K_1 = 0.002194$	0.0060	$K_1 = 0.004682$	0.0020	$K_1 = 0.007211$	0.0760	$K_1 = 0.014988$	0.0450
	6	$K_2 = 0.000818$	0.9960	$K_2 = 0.002128$	0.9830	$K_2 = 0.003832$	0.9760	$K_2 = 0.009242$	0.9450
	0	$K_1 = 0.00146$	0.9960	$K_1 = 0.003177$	0.0000	$K_1 = 0.005782$	0.0970	$K_1 = 0.006815$	0.0050
	8	$K_2 = 0.000327$	0.9960	$K_2 = 0.0018$	0.9980	$K_2 = 0.003296$	0.9870	$K_2 = 0.003474$	0.9850

34 11	Temperature											
Model	40°C		50°C			60°C		70°C				
name	Thickness	Model constant	\mathbb{R}^2									
		a = 0.041907		a = 0.733742		a = 0.755104		a = 52.86507				
		$K_1 = 0.257035$		$K_1 = 0.702389$		$K_1 = 0.016358$		$K_1 = 5.094837$				
Hii et al	2	n = 0.410749	0.9740	n = 9.35E-08	0.9990	n = 1.071261	0.9990	n = 0	0.9960			
nii et ai	2	b = 2.343353	0.9740	b = 0.600552	0.9990	b = 0.475716	0.9990	b = 76.38476	0.9900			
		$K_2 = 0.398378$		$K_2 = 0.005764$		$K_2 = 0.323469$		$K_2 = 2.187207$				
		n = 0.241939		n=1.212526		n = 0.001803		n = 0.263271				
		a = 0.745248		a = 70.02726		a = 0.534108		a = 0.631275				
		$K_1 = 0.716233$		$K_1 = 5.928962$		$K_1 = 0.002076$		$K_1 = 0.689391$				
	4	n = 0	0.0060	n = 1.69E-06	0.0650	n = 1.384415	0.0000	n = 0	0.9990			
	4	b = 0.583894	0.9960	b = 70.06436	0.9650	b = 0.692542	0.9990	b = 0.617217				
		$K_2 = 0.00174$		$K_2 = 3.096805$		$K_2 = 0.441938$		$K_2 = 0.002966$				
		n=1.204611		n=0.113728		n = 0.05881		n = 1.378516				
		a = 1.167105	0.9990	a = 0.454973	0.9990	a = 0.623595		a = 0.3	0.9430			
		$K_1 = 0.022845$		$K_1 = 0.386237$		$K_1 = 0.001812$		$K_1 = 4$				
		n = 0.595909		n = 2.14E-09		n = 1.318813	0.0000	n = 0.9				
	6	b = 0.494017		b = 0.65654		b = 0.375357	0.9990	b = 18670387				
		$K_2 = 0.912311$		$K_2 = 0.001315$		$K_2 = 0.119222$		$K_2 = 15.78937$				
		n = 0.608096		n = 1.286032		n = 0.038132		n = 0.02252				
		a = 0.661317		a = 0.341803		a = 0.479353		a = 0.38943				
		$K_1 = 0.000662$		$K_1 = 8.71E-09$		$K_1 = 0.39277$		$K_1 = 0.220181$				
	0	n = 1.213715	0.0000	n = 0.034157	0.0000	n =0	0.0000	n =0	0.0000			
	8	b = 0.332816	0.9990	b = 0.662946	0.9990	b = 0.678277	0.9990	b = 0.656199	0.9990			
		$K_2 = 1.35E-08$		$K_2 = 0.004822$		$K_2 = 0.004991$		$K_2 = 0.003152$				
		n = 0.274594		n = 0.973731		n = 1.069026		n = 1.19391				
Two Term	2	a = 0.961616	0.9900	a = 0.972854	0.8840	a = 0.978959	0.7880	a = 0.980516	0.7550			
Exponential	2	K = 0.003258	0.9900	K = 0.006777	0.8840	K = 0.008076	0.7880	K = 0.010889	0.7550			
	4	a = 0.963668	0.0040	a = 0.978283	0.9410	a = 0.972135	0.9720	a = 0.982418	0.000			
	4	K = 0.00304	0.9840	K = 0.004671	0.9410	K = 0.005516	0.8720	K = 0.007707	0.8680			
	6	a = 0.963138	0.9990	a = 0.975267	0.9950	a = 0.97568	0.9830	a = 0.982418	0.8680			
	U	K = 0.002044	0.7770	K = 0.003612	0.3330	K = 0.004977	0.9630	K = 0.007707	0.0000			
	8	a = 0.965198	0.9980	a = 0.959486	0.9900	a = 0.97414	0.9730	a = 0.975509	0.9860			
	O	K = 0.001494		K = 0.002502	0.3300	K = 0.003807	0.9730	K = 0.004835	0.3000			

The experimental moisture ratio was plotted against the predicted moisture ratio for all the temperatures and thickness studied as represented in Figure 3, this was to validate the developed model with experimental moisture ratio data. The R² was found to be unity which indicated the closeness of the data obtained from the model developed for this study to the experimental moisture ratio data.

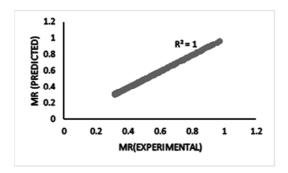


Figure 3. Experimental Moisture Ratio versus Predicted Moisture Ratio.

4. Conclusion

Drying process of sweet potato slices was investigated using a hot air oven dryer. A drying model showing the relationship between moisture ratio, drying time and mass on sweet potato drying process was developed. The statistical measures used for this study indicate that the derived model

was in good agreement with experimental moisture ratio data. The developed model was fitted to experimental data and the coefficient of determination value obtained was 0.9999 and the sum of squares error value was 0.0001296. The developed model was further validated by comparing the predicted moisture ratio against the experimental moisture data. The data points were identified to lie on a straight line, showing the suitability of the model in describing the drying kinetics of sweet potato at a temperature range of 40°C to 70°C and a sample thickness of 2 mm to 8 mm.

Thirteen different kinetic models were compared with the developed model in order to determine the best model for predicting the drying kinetics of sweet potato, the drying rate was experimentally investigated at different temperature and material thickness levels. The experimental data were fitted to the thirteen selected thin layer models and the results obtained showed that the developed model resulted in an excellent fit for all drying temperatures of 40, 50, 60 and 70°C and sample thickness levels of 2, 4, 6 and 8mm. This result clearly shows that the developed model was suitable for predicting the drying of sweet potato. At all drying temperatures tested, the value of R^2 was higher than 0.9999 and the SSE value tended towards zero. Therefore, the developed model can be applied in describing the drying behaviour and predicting the drying kinetics of sweet potato and this developed model could be compared to Hii et al and Logarithmic models which had good R² with least SSE; and can be useful in engineering tool for the application in the design of equipment and optimization.

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