Analysis of Bio-inspired Kinematic Patterns Pectoral Fin with Shape Memory Alloy (SMA)

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Abstract: Pectoral fins have received the attention of many researchers because of their important role in maneuverability underwater in the recent years. This paper presents the study of a novel flexible robotic-fin actuated and the swimming propulsion by Shape Memory Alloy (SMA) inspired by a Koi Carp. In this paper, the morphological and mechanics parameters of a koi Carp pectoral fin from a carp is first studied. The motion of the pectoral fins is analyzed, which are difficult to reproduce by artificial pectoral fins and descending and ascending, the five basic gestures of the robotic fin are well achieved by the coordinating control of the fin base and fin rays, which are relaxation, expansion, bending, cupping and undulation. Secondly, a simplified theoretical model of the SMA fin plate is derived, thermodynamics of the SMA plate and the relationship between curvature and phase transformation are analyzed. Thirdly, Dynamic modeling of a flexible SMA tail, several simulations and model experiments are conducted according to the previous computation and analyses. Consequently, the five basic gestures of the robotic fin such as relaxation; expansion; bending; cupping; undulation, are extracted from the 3D grid graph. The results of kinematic of flexible pectoral fins will provide a basis to flexible pectoral fin and butterfly-inspired underwater.

Keywords: Biomimetic Underwater Robot, Bio-inspired Pectoral Fin, Fin Patterns, Oscillation, Shape Memory Alloy (SMA), SMA-Driven Plate, Maneuverability

1. Introduction

Zoologists, biologists, and engineers have all examined fish and other aquatic creatures with intense interest, including their specific behavior, swimming pattern, high maneuverability, and efficient design [1]–[5]. The thorough researches on fish physiology and morphology have indicated that the notable swimming propulsion efficiency is entirely due to not only orchestrated motion of multiple fins, but also their flexible, diverse and complex three-dimensional movements, the superiority of the flexible fins cannot be matched by any bionic fins [6, 7]. In previous studies, many fish-like underwater robot were developed using various kinds of, such as Shape Memory Alloy (SMA) [8]–[10], Ionic Conducting Polymer Film (ICPF) [11], [12], and Ionic Polymer Metal Composite (IPMC) [13], [14] have been adopted in biomimetic underwater robots. Fascinated by the crucial role of pectoral fins in fish maneuvers, a large number of researches were conducted to study mechanism and characteristic of pectoral fins. Yan investigated morphological parameters, the kinematic pattern of a carp pectoral fin and the mechanical properties fin rays to design a flexible pectoral fin driven by Shape Memory Alloy (SMA) [15]. The case of flexible pectoral fins in robotic fish has been studied by several groups. Lauder and coworkers explored the hydrodynamics associated with pectoral fins Simulated [16], [17] and with Computational Fluid Dynamics (CFD) simulation. Deng et al. [18], [19], modeled a robotic fish with two pectoral fins and a caudal fin and used it to design controllers. However, the flexibility of the pectoral fins in their prototype was not accommodated in their model. With CFD simulation, Shoele et al. [20] numerically
examined the fluid-structure interaction and force generation by pectoral fins of a fish during labriform swimming.

Webb [21] and Blake [22] performed some theoretical modeling of pectoral fins-based swimming of live fish, which provides useful tools for calculating hydrodynamic forces acting on the pectoral fins. There have been a variety of robotic fish reported that involve pectoral fins. Most of these use rigid, oscillating fins [23], [24]. The existing simulation research on the kinematics of pectoral fins mainly concerns the analysis of kinematic parameters in fish steady swimming [25–29]. Whereas pectoral fins play a more important role in fish maneuvers, especially during retreating and hovering [30]. The present work is concerned with the kinematics study on Koi Carp, whose swimming is a typical carangiform, possessing a great maneuverability and a high swimming efficiency.

The paper is structured as follows. Section 2 proposed the mechanical characteristics of a pectoral fin of Koi carp comprehensively. Subsequently, the simulation of SMA driven plate is described and discussed in section 3. The theoretical analysis of the SMA plate, for instance, thermodynamics of SMA plate, relationship between curvature and phase transformation of SMA plates are investigated in section 4. Lastly, the paper ends with the conclusion section.

2. Morphology and Mechanical Characteristics of a Pectoral Fin of Koi Carp

Carp is a kind of typical carangiform fish, which has a highly effective swimming ability with the aid of its pectoral fins. Thus, as it can be seen in Table 1, our concentration is based on taking carp as a sample in order to measure the morphological parameters of the fin.

<table>
<thead>
<tr>
<th>Morphological features</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>The body length of the carp (mm)</td>
<td>200</td>
</tr>
<tr>
<td>The area of the pectoral fin (mm²)</td>
<td>680</td>
</tr>
<tr>
<td>The number of fin rays belongs to the fin</td>
<td>14</td>
</tr>
<tr>
<td>The length of the longest fin ray (mm)</td>
<td>34</td>
</tr>
<tr>
<td>The length of the shortest fin ray (mm)</td>
<td>13</td>
</tr>
</tbody>
</table>

Figure. 1 demonstrates manifestly the marked points of both sides ought to be aligned with the longitudinal axis of the fin ray. As it can be seen from Figure. 1, the pectoral fin of Koi Carp [32] consists 14 fin rays, in which 20 black dots on one side of pectoral fin are marked points. It is worth noting that the fin ray adjacent to dorsal fin below neutral condition is dorsal leading ray while the pectoral fin adjacent to ventral fin underneath neutral condition is the ventral leading ray. Additionally, the outer edge of pectoral fin is the part of pectoral fin away from the fish's body whereas the inner edge of pectoral fin indicates the section of pectoral fin near the fish's body (rigid body).

The phase difference of two adjacent sample points in a sinusoidal function is crucial to satisfy the requirement, according to Shannon’s sampling theorem [33] as:

\[ \Delta \varphi \leq \frac{\pi}{2} \]  

(1)

Moreover, the phase difference of two nearby fin rays in a pectoral fin can be written as follows:

\[ \Delta \varphi = \frac{2\pi n_\lambda}{n-1} \]  

(2)

In which \( n \) expresses the number of fin rays and \( n_\lambda \) stands the wave number of undulation motion. By combining Equation (1), (2), the relationship between wave number and the number of fin rays can be expressed by:

\[ n \geq 4n_\lambda + 1 \]  

(3)

Based on the equation (3), as a minimum, 5 markers are essential so as to simulate a thorough cycle of undulation motion. In this work, five markers along the outer edge of fin rays (see Figure. 1 for the numbers of 1, 4, 7, 9, and 12) are opted respectively. Hence, the 3D motion profiles of the pectoral fins can be achieved by using simulation processing.

As is evident, the movements of the pectoral fins are sophisticated which made researchers to reproduce artificial pectoral fins. Luckily, from plentiful images of the pectoral fins, for example, cruising, turning, retreating, ascending, descending, and the five simple gestures of the bio-inspired fin are well achieved in Figure. 2 [31]. Similarly, Lauder’s group [34, 35] perceived some interesting patterns of koi carp swimming.

![Figure 1. Illustration of the marked pectoral fin. Model of the koi Carp pectoral fin.](image)

![Figure 2. Five basic gestures of a robotic pectoral fin and natural. a) Relaxation; b) Expansion; c) bending; d) cupping; e) undulation [31].](image)
Figure 3. Bending stiffness of the respective fin rays. The standard deviations are in the range of (0.002 to 0.031) \times 10^{-4} \text{N.m}^{-2}.

Figure 4. Young’s modulus of the respective fin rays. The standard deviations are in the range of (0.04 to 0.257) GPa. EM=14.8 GPa, EA=39.3 GPa.

Figure 5. Oscillation of the SMA-driven plate.

The mechanical properties of a fin ray are important for developing a robotic fin. In order to obtain the distribution of bending stiffness and Young’s modulus of the pectoral fin ray, regarding the base side to the distal side, five fin rays (Figure 1.) are chosen carefully for conducting the test. The stiffness of one location is calculated for five times with changing force, and the standard deviations are also obtained. The simulation results are shown in Figures 3 and 4.

It can be seen from Figures 3 and 4 that both bending stiffness and Young’s modulus diminish from Fin Ray 1-9. It should be emphasized that Young’s modulus of 30% length location was approximately 1.1 times as that of 50% length location. Both bending stiffness and Young’s modulus of SMA plates are approximate to that of the carp’s fin rays, which are presented in Figures 3 and 4. In these figures, $K_M$ and $E_M$ denote bending stiffness and Young’s modulus of SMA plates in the martensite phase. However, $E_A$ denotes Young’s modulus of SMA plates in austenite phasing. On the other hand, the SMA plates are stiffer when they actuate.

3. Simulation of the SMA-Driven Plate

A flexible plate, embedded with SMA wires and SMA-driven plate, is utilized as the basic unit of the bio-inspired pectoral fin. In order to ensure a relatively large bending angle, the length and the thickness of the SMA-driven plate is set as 50 mm and 1 mm, respectively. The width of the SMA-driven plate should match the stress of the SMA wires, which is related to the diameter of the SMA wires. Considering the assembling of SMA wires on the plate, the width of the SMA-driven plate is set as 20 mm. The diameter of the SMA plates will be determined by simulation. As illustrated in Figure 5, as an SMA wire is heated to $A_s$ by passing a pulse width modulation (PWM) current. It will undergo phase transformation, contract to its original length, and pull the tip of the plate. Therefore, the plate will bend to the side where the SMA wire is heated. Since the base plate is flexible, its elastic modulus is large enough to provide a resilience force back to the middle state. When the SMA wire
cools, the SMA driven plate will return straight. By successively heating SMA wires on both sides of the plate with two PWM currents with phase difference, the SMA plate can bend and oscillate [36]. It is worth mentioning that the motion of the SMA-driven flexible plate is related to the dynamical constitutive equation of SMA, the thermodynamic between SMA wires and their environment, the dynamics related to large deformation flexible beam, two SMA wires, and hydrodynamics. The dynamics of flexible plates embedded with SMA wires are tiresome to model. Hence, the diameter of SMA wires was estimated through static equilibrium, and determine the range of some key parameters by simulation, such as the diameter of SMA wires and the current that passes through the SMA wires.

a) Control of the bending direction of the SMA-plate by heating SMA wires. A, B denote SMA wires on the top and bottom surfaces of the plastic plate, respectively. 0 denotes the oscillation angle of SMA-driven plate, which can be measured by the angle between the horizontal line and the tangent to the tip point of SMA-driven plate.

b) Time sequence of the heating current for SMA wires A and B.

4. Theoretical Analysis of the SMA Plate

4.1. Thermodynamics of SMA Plate

Usually, SMA wires are heated by electric current. However, the SMA plate has a bigger volume, and needs more energy than SMA wires. As a result, it is inappropriate to heat the SMA plate directly with electric current.

Three assumptions are made in the thermodynamic analysis of SMA plate: (4) The PVC tube is thin. It covers the enamel-insulated copper wire and the SMA plate closely and tightly. The tube, copper wire and SMA plate can be considered as an integrated plate. (5) Radiation can be ignored because of little amount of radiation of the tube, copper wire and SMA plate. (6) The connection between the integrated plate and water is presumed as the only way to transfer heat from the plate to environment.

When the SMA plate is heated, the energy balance is expressed as:

\[ E_i = E_{sma} + E_{pvc} + E_{wire} + E_{con} + E_{ph} \]  \hspace{1cm} (4)

\[ E_i = I^2 \lambda_{wire} \frac{h_{wire} L_{wire}^2}{4\pi} t \]  \hspace{1cm} (5)

\[ E_{sma} = \int_{T_s}^{T_f} C_{sma}\rho_{sma}l_{sma} dwdT(t) \]  \hspace{1cm} (6)

\[ E_{pvc} = \int_{T_s}^{T_f} C_{pvc}\rho_{pvc}l_{pvc} dwdT(t) \]  \hspace{1cm} (7)

\[ E_{wire} = \int_{T_s}^{T_f} C_{wire}\rho_{wire}l_{wire} \frac{\pi d_{wire}^2}{4} dT(t) \]  \hspace{1cm} (8)

\[ E_{con} = \int_{T_s}^{T_f} h_{w} l_{con} 2(d + w)(T_f - T_s) dt \]  \hspace{1cm} (9)

where \( E_i, E_{sma}, E_{pvc}, E_{wire}, E_{con}, \) and \( E_{ph} \) denote electric energy, the heat change of SMA, the heat change of PVC tube, the heat change of copper wire, conduction energy between plate and water, and transformation latent heat of SMA, respectively; \( i \) denotes heating current through copper wire; \( \lambda_{wire} \) denotes electric resistivity of the copper wire; \( c_{wire}, c_{sma} \) and \( c_{pvc} \) denote the thermal capacities of copper wire, SMA plate and PVC tube, respectively; \( \rho_{wire}, \rho_{sma} \) and \( \rho_{pvc} \) denote the densities of copper wire, SMA plate and PVC tube, respectively; \( l_{wire}, l_{sma} \) and \( l_{pvc} \) denote the effective lengths of copper wire, SMA plate and PVC tube, respectively; \( d \) and \( w \) denote the depth and width of the SMA plate, respectively; \( T_s \) denotes the environment temperature; \( T_f, T_{f1} \) and \( T_{f2} \) denote the final temperatures of SMA plate, PVC tube and enamel-insulated copper wire respectively during the martensite reverse transformation process. \( t_s \) and \( t_f \) denote the start moment and finish moment of the heating process, respectively; \( h_w \) denotes the equivalent convective heat transfer coefficient.

The cooling process of SMA plate is a natural convective phenomenon. The energy exchange during the cooling process is given by:

\[ 0 = E_{sma} + E_{pvc} + E_{wire} + E_{con} + E_{ph} \]  \hspace{1cm} (10)

\[ E_{sma} = \int_{T_s}^{T_f} C_{sma}\rho_{sma}l_{sma} dwdT(t) \]  \hspace{1cm} (11)

\[ E_{wire} = \int_{T_s}^{T_f} C_{wire}\rho_{wire}l_{wire} \frac{\pi d_{wire}^2}{4} dT(t) \]  \hspace{1cm} (12)

\[ E_{pvc} = \int_{T_s}^{T_f} C_{pvc}\rho_{pvc}l_{pvc} dwdT(t) \]  \hspace{1cm} (13)

\[ E_{con} = \int_{T_s}^{T_f} h_{w} l_{con} 2(d + w)(T_f - T_s) dt \]  \hspace{1cm} (14)

For the sake of convenience, we consider \( h_w \) as a constant in both heating and cooling processes. From Eq. (4) to Eq. (14), the energy exchange can be estimated in both heating and cooling processes. However, it is difficult to obtain an accurate result through an analytic calculation, so we conduct a simulation to obtain the actuation time of the SMA plate in both heating and cooling processes.

4.2. Relationship Between Curvature and Phase Transformation of SMA Plates

Many constitutive equations of SMA have been put forward to describe the mechanical and thermodynamical characteristics of SMA, including Tanaka’s model [37], the first constitutive model of SMA, and Liang’s [38] and Brinson’s [39] models, both of which are revised versions of Tanaka’s model. However, these models describe the stretching motion of SMA wires, not the bending motion of SMA plates. Therefore, we adopt a simplified model to describe the bending motion of SMA plates, with regard to which some basic facts are taken into consideration. Firstly, SMA plates are very light and the actuation frequency of SMA plates is relatively low (about 1 Hz), so the inertia force can be neglected. Secondly, considering the constitutive model of SMA plates is absent, we take the curvature of SMA plates as the characteristic parameter of the bending motion. The relationship between the curvature and the phase
transformation of SMA plates is described as [40, 41]

\[
k_{SMA} = (1 - \xi)k_{max}
\]  

(15)

where \( \xi \) denotes the martensite volume fraction which represents the degree of the martensite phase transformation. 
\( k_{max} \) denotes the trained maximum curvature, while \( k_{SMA} \) denotes the curvature in phase transformation. When \( \xi \) equals to 1, the phase transformation has not yet started, and the curvature is zero, while \( \xi \) equals to 0, the phase transformation has finished, and the curvature has reached the predefined one. So, \( \xi \) is defined as:

\[
\xi(T) = \frac{\xi_a}{1 + e^{a(T-T_0)}} + \xi_b
\]  

(16)

In the cooling process of SMA, the parameters of Eq. (16) are:

\[
T_0 = \frac{M_s + M_f}{2}
\]  

(17)

\[
\alpha = \frac{\beta}{A_f - A_s}
\]  

(18)

In the heating process of SMA, the parameters of Eq. (16) are:

\[
T_0 = \frac{A_s + A_f}{2}
\]  

(19)

In Eqs. (17) – (20), \( M_s, M_f \) denote the starting and finishing temperatures of martensite phase transformation; \( A_s, A_f \) the starting and finishing temperatures of austenite phase transformation, respectively; \( \beta \) is determined empirically. In Eq. (16), \( \xi_a \) and \( \xi_b \) are constants.

5. Swim by the Pectoral Fins

In this test, the wire-driven caudal fin is kept still. The pectoral fins are controlled by the two parameters \( \delta_1 \) and \( \delta_e \) in one movement circle. The horizontal plane was set as the initial position of the fins, thus the original values of \( \delta_1 \) and \( \delta_e \) are both 0°. When the power stroke adduction begins, the fin was vertical. We control the feathering angle \( \delta_e = 90^\circ \) and the flapping angle \( \delta_1 \) increasing quickly from 0° to the maximum. The water was pushed posteriorly, thus generating thrust and moving the fish forward. The recovery stroke abduction begins with a quick feathering motion. The feathering angle is controlled from 90° to 0° so as to reduce the adverse water resistance. Furthermore, using the pectoral fins, the robot fish can swim backward by reversing the fin movement. The pectoral fin motion pattern is fixed and the swimming speed is controlled by the frequency. Results are shown in Figure 6.

Figure. 6. The relationship between frequency and velocity.
From the results, there is discrepancy in forward swimming speed and backward swimming speed. One reason is that the vortex drag of the fish at the two ends is different. The tail is more slender, meaning less vortex drag when swimming forward. Therefore, the forward speed is higher than the backward speed. The proposed model predicts the pectoral fin propulsion reasonably well. Among all the tests, the maximum forward speed of the robot using pectoral fins is 145 mm/s and the maximum backward speed is 115 mm/s.

6. Conclusion and Concluding Remarks

This paper outlines Koi Carp simulation system, and the motion pattern of flexible pectoral fin in retreating. We find that the motion pattern of the pectoral fin is very complex, which was very difficult to obtain the kinematic patterns of the pectoral fin. Likewise, we demonstrate the angle of the foundation of marked fin rays motion in retreating and the correspondence analysis of the surface area of the pectoral fin. Finally, five motion pattern of pectoral fin are extracted from the 3D grid graph. As the future works could adopt the same simulation system to analyze more maneuvers of flexible pectoral fins, for instance, relaxation, expansion, bending, cupping, and undulation which are very educational and significant to mimic a flexible pectoral fin and butterfly-inspired underwater.

References

[8] Jaromie Mohd Jani a, b, ft, Martin Leary a, Aleksandar Subic a, Mark A. Gibson c, A review of shape memory alloy research, applications and opportunities, Materials and Design 56 (2014) 1078–1113.


