A research paper on the performance analysis of a Self-mode Locking high power linearly polarised fiber laser

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To cite this article:

Abstract: In this research a design for high power linearly polarized all-fiber linear cavity lasers with self-mode-locking is presented, and a new theoretical model based on a Nonlinear Schrödinger Equation (NLSE) is developed and implemented on the MATLAB platform. For the design of cavity, Polarization Maintaining (PM) fibers for both the gain medium and the Fiber Bragg Gratings (FBGs) is implemented. The FBG pairs are used to select the lasing wavelength and polarization. The fiber lasers incorporate specially designed FBGs to achieve an extinction ratio larger than 23 dB. The proposed configuration is based on Non-Linear Polarization (NPR) using PM Yb-doped active fiber and two matching FBGs to form the laser cavity. The combination of nonlinearity, gain, and birefringence in the cavity made the laser generate mode-locked pulses in the picosecond range and with high average output power. Experimental data and numerical simulations of the self-mode-locking fiber laser are presented. Main parameters affecting mode-locked pulses and its envelope are identified. The model proposed here explains the self-mode-locking mechanism and the source of the pulse envelope. In this model, it is proven that self-phase modulation (SPM) plays an essential role in pulse formation and shaping.

Keywords: Self-Mode-Locking (SML), Polarisation Maintaining (PM), Nonlinear Schrödinger Equation (NLSE), Fiber Bragg Gratings (FBGs), Optical Coupler (OC)

1. Introduction

Fiber lasers have extended their performance capabilities and substitute conventional laser technologies markets because of large number of benefits [1-3]. With the adoption of double-clad fibers and clad-pumping techniques, laser output can be obtained with high power and energy levels at either CW or pulsed regime. Fiber lasers are generally used in those applications which require high peak power and pulse energy. The two most well-established techniques to pulse fiber lasers are Q-switching and mode locking in either active or passive form [4, 5-7].

Mode-Locking of a laser produces ultra-short pulses on the order of picoseconds or femto-seconds. This technique induces a fixed phase relationship between the longitudinal modes of the laser's cavity. Interference between these modes causes the laser light to produce a train of pulses. Locking of mode phases enables a periodic variation in the laser output which is stable over time, and with periodicity given by the round trip time of the cavity [7]. Such a laser is said to be mode-locked or phase-locked. In a real mode-locked laser, the actual pulse width depends on other factors, such as the pulse shape and the overall dispersion of the cavity. Fiber lasers can be mode-locked either in active or passive way. Active methods typically use an external signal to modulate the cavity loss and consequently require the use of bulky modulators and drivers. Passive mode-locking depends on incorporating a SA in the laser cavity. A saturable absorber is an optical component with a certain optical loss, which is reduced at high optical intensities [4].

1.1. Passively Mode-Locked Fiber Lasers

Literature review shows that the most popular Saturable Absorbers in the 1 µm band are Semiconductor Saturable
Absorber Mirrors (SESAMs) [8-14], and Nonlinear Polarization Rotation (NPR) [15-19]. Other modulators such as Single-Wall Carbon Nanotubes (SWCNT) [20-25] and NOLM [26] are also reported. The fastest mode-locked pulse with pulse width 128fs [26] was achieved by combining nonlinear NPR and a nonlinear amplifying loop mirror.

1.2. Self-Pulsed Fiber Lasers

Two kinds of self-pulsing are mainly observed; sustained self-pulsing (SSP) and self-mode locking (SML) [14]. SSP is the emission of laser pulses at a repetition rate associated with relaxation oscillations and observed at specific pumping ranges. Most often, SSP has irregular repetition periods with pulses in microsecond and nanosecond ranges. Alternatively, more interests are into SML with pulse widths in the range of nanosecond down to picoseconds. In SML, the laser signal modulation period corresponds to the cavity round-trip time. Various mechanisms may cause self-pulsing in fiber lasers [28] including ion-pairing [29], re-absorption of laser photons in un-pumped part of fiber [30], scattering processes such as SBS or SRS [31] and Kerr effect [32]. In References [29-32], self pulsing were investigated only experimentally without numerical verification. Recently, Bedyakova et al. studied in [33] the pulsing dynamics of Yb-doped linear fiber laser. The model is based on NLSE and includes both nonlinear and dispersion effects. Numerical simulations show good agreement for power and spectrum measurements. Yet, the model addresses only a narrow time scale of the self-pulsed output.

2. System Model

2.1. Purposed Configuration of Fiber Laser

The schematic of the proposed Self Mode-Locked (SML) all-PM fiber laser, with all fiber connections fusion spliced, is shown in Figure 2.1. The fiber laser was pumped by a fiber-coupled laser diode at 975 nm wavelength. Laser diodes of 10 W and 25 W were used and which have a multi-mode output fiber. In some configurations, the laser diode was connected to a low pass filter to pass pump wavelength and attenuate longer back-reflected wavelengths that can burn the laser diode. Though the filter introduced around 10% loss to the input pump power, it provided protection to the laser diode at high power levels.

The fiber laser cavity consists of an active fiber spliced between a FBG pair. Both active fiber and FGB fiber are of PM type. The FGB pair is formed of two gratings; one end of the highly reflective FGB is spliced to the laser diode or the filter and the other end is co-spliced (where both PM fibers axes are parallel to each other) to the active fiber. The other FGB is used as the cavity output coupler with reflectivity value ranges from 7% up to 82%. In order to select polarization, the output coupler grating is cross-spliced (where the slow axes of both PM fibers are perpendicular to each other) to the active fiber. Most of the laser modules have a PM APC-pigtail co-spliced to the output coupler FGB for reducing back reflection. In most cases, the pump diodes are operated continuously.

2.2. Active Fibers

Two types of double-clad PM type active fibers are used in this research, Ytterbium (Yb3+) and Erbium-Ytterbium co-doped (Er3+/Yb3+). Ytterbium ions are one of the most versatile ions to be doped in silica-based fibers. It offers several advantages of wide absorption band from 850 nm to 1070 nm. It can be also pumped with wide selection of solid-state laser diodes (850 nm, 980 nm, 1047 nm and 1064 nm). In addition, ytterbium co-doped fibers have impressive emission spectra in the range from 970 to 1200 nm. In the research, all of our Yb-doped active fibers are pumped with 975 nm laser diodes with an emission in the 1 µm band.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Er3+/Yb3+-doped active fiber (6/125)</th>
<th>Yb3+ doped active fiber (10/125)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fiber part number</td>
<td>Nufern PM-EYDF-6/125-HE</td>
<td>Nufern PLMA-YDF-10/125</td>
</tr>
<tr>
<td>Fiber type</td>
<td>PM (PANDA), Double-clad</td>
<td>PM (PANDA), Double-clad</td>
</tr>
<tr>
<td>Core diameter/Cladding diameter</td>
<td>6µm/125µm</td>
<td>10µm/125µm</td>
</tr>
<tr>
<td>Mode field diameter</td>
<td>6.7 µm</td>
<td>11µm</td>
</tr>
<tr>
<td>Core N.A.</td>
<td>0.18</td>
<td>0.075</td>
</tr>
<tr>
<td>Birefringence</td>
<td>0.00034</td>
<td>0.0003</td>
</tr>
<tr>
<td>Cladding absorption @975nm</td>
<td>0.89 dB/m</td>
<td>5 dB/m</td>
</tr>
</tbody>
</table>
One of the most important parameters for active fiber is the absorption per meter at the pump wavelength. Most of the active fiber data sheets list the absorption per meter at 915 nm wavelength. The ratio between the absorption at 975 nm and 915 nm could be estimated from the absorption spectra. The absorption coefficient at 975 nm is about three times the one at 915 nm for Yb3+ while for Er3+/Yb3+ co-doped fiber, the ratio varies from 5-7 [39-40]. This coefficient is important to estimate the length of the active fiber needed to build an efficient cavity. A minimum of 10-12 dB absorption of a gain fiber is required to build an efficient laser. The main specifications for active fibers used in the research are shown in both Table 2.1.

Fiber Bragg Gratings (FBGs) inscribed on a PM fiber are used in this research to build fiber laser cavities with a linearly polarized output. When the PM fiber is exposed to UV-light for grating inscription, the resulting index modulation gives rise to two spectrally separated Bragg reflective peaks because of fiber’s birefringence [41]. In order to provide both polarization and wavelength selection, the fast axes wavelength of the high reflection (HR) FBG is matched to the slow axis wavelength of the output coupler FBG. The maximum mismatch allowed between both wavelengths is around 30-40 pm. The high isolation between the two FBG axes is a key factor to have a laser output with high extinction ratio. In order to maintain high isolation, the FBGs 3dB bandwidth should not exceed the Bragg wavelength separation of the PM fiber. Writing FBG with a broader bandwidth will lower the isolation and may lead to dual polarization operation. On the other hand a too narrow bandwidth will make the wavelength matching difficult. In terms of splicing, high reflection FBG is co-spliced (where both PM fibers are spliced with both their slow axes are parallel to each other) to one end of the active fiber. The output coupler FBG is cross-spliced (where both PM fibers are spliced with their slow axes are perpendicular to each other) to the other end of the active fiber.

2.3. Fiber Laser Assembly

Fiber laser assembly consists of two procedures, fiber splicing and fiber routing. Different types of splicing points and recoating types involved in assembly will be discussed in this section. Two types of splices were implemented as shown in the laser schematic in Figure 2.1. The first is between multimode fiber and PM fiber (The point between the laser diode output or the bandpass filter (BPF) and the HR FBG). This type of splicing can be performed with an Ericson FSU-975 arc fusion splicer. The second type is between two PM fibers using a Fujikura FSM-20PMII arc fusion splicer. It has a program to splice two PM fibers at any desired angle. In the proposed laser module, the PM fiber splicing has two orientations; co-splicing or cross splicing. On the other side, cross-splicing of two PM fibers, is splicing the two PM fibers with their slow axes are perpendicular to each other.

3. Numerical Modelling of All-PM Mode-Locked Fiber Laser

3.1. Nonlinear Pulse Propagation in Fiber

The performance of picoseconds and femtosecond mode-locked fiber lasers particularly in terms of pulse energy, peak power and pulse quality is controlled by the nonlinearities, dispersion and the gain of the fiber. In order to analyze the pulse formation and stabilization inside optical fiber, it is useful to introduce two length scales, known as the dispersion length LD and the nonlinear length LNL [38].

Based on the definition of dispersion and nonlinear length, two regimes for fiber and pulse interaction can be explained as:

a) Dispersion dominant regime: In this regime, the fiber length L << LNL but L ~ LD. The pulse evolution is governed by group velocity dispersion (GVD) and the nonlinear effects play a minor role.

b) Non-linearity regime: In this regime the fiber length L ~ LD but L ~ LNL. The dispersion has negligible effects compared to nonlinear term.

When the fiber length L is longer or comparable to both LD and LNL, dispersion and nonlinearity both act together as the pulse propagates along the fiber. The interplay of the dispersion and nonlinear effects can lead to a different behaviour [42] compared with the expected from dispersion or nonlinear alone [42, 43]. Nonlinear effects in optical fibers are particularly important when considering the propagation of short pulses (from 10 ns to 10 fs). The intensity-dependent refractive index of silica gives rise to three effects: Self-Phase Modulation (SPM) [44], Cross-Phase Modulation (XPM) [42, 44] and Four-Wave Mixing (FWM). More insight into some of the fiber non-linearities such as SPM, XPM and NPR will be discussed in the following sections.

The Nonlinear Polarization Rotation (NPR) can be treated as a kind of artificial saturable absorption to achieve the passive mode locking in a fiber laser [45]. The evolution of the two polarization components will be tracked by a column matrix for the electric field and a 2×2 matrix for the resonator elements. The electric field 2×1 field vector is given by [45].

3.2. Numerical Modelling

Nonlinear Schrödinger Equation (NLSE) comes in a variety of forms based on the system being studied. Its generalized time domain form can be represented in [38]. The derivation of NLSE starting from Maxwell equation is illustrated in details in [35]. The time-domain Coupled NLSE (CNLSE) for high birefringence fiber is given in [46].

Split Step Fourier Method is one of the powerful
methods to solve NLSE is known as split-step Fourier method (SSFM) which is the technique of choice for solving NLSE due to its easy implementation and speed compared to other methods especially time-domain finite-difference method [47, 48]. It assumes that mathematical terms due dispersion and nonlinearity can act separately and independently over short piece of fiber. The SSFM is an iterative process that determines the field solution for spatial steps of h. This performed for each step for the entire length of the fiber. The procedure during one step is illustrated in Figure 3.1. The fiber of length L is divided into \( sL = \frac{L}{h} \) steps of length h [48]. The field propagation \( A(jh, t) \) per spatial step h at the step \( jh \) \((j=1, 2, sL)\) for the entire fiber length can be represented by the following relation:

\[
A(jh, t) = \mathcal{F}^{-1} \left\{ \exp \left( i\phi \right) \mathcal{F} \left\{ \frac{hN}{j} A((j-1)h, t) \right\} \right\} \tag{3.21a}
\]

where \( A((j-1)h, t) \) is the field solution from the previous step. The operation of nonlinear operator occurs in the middle of the step. It is the first operator to act on \( A(jh, t) \). The effect of dispersion is determined in the frequency domain. The field solution is Fourier transformed, operated on and then back transformed to give solution \( A(jh, t) \) at step \( jh \). The field solution contains both intensity and phase information.

**3.3. Simulation Model**

The fiber laser cavity (Figure 3.2(a) is divided into the sections and modeled as shown in Figure 3.2(b). The proposed simulation model considers the following:

1. NLSE is used to simulate the laser cavity
2. Two sections of single mode fiber (SMF) are included in the cavity modelling (on which FBG is written).
3. Any FBG in the laser represents Spectral filtering component.
4. The OC-FBG acts also as an output coupler.

Following the approach in [49, 50], the operator, \( C \), describing the round trip for the linear cavity can be represented as follows:

\[
C = FG e^{i\phi}FR_{HR}FG e^{i\phi}FR_{OC} \tag{3.21b}
\]

Where, \( F \) and \( G \) represent the propagation through the SMF and the gain fiber. \( \phi \) is a cavity related phase shift. RHR and ROC are the reflectivity of the HR and OC FBGs respectively. Each component model will be explained as follows:

*a) Fiber Sections*

In the simulation, the pulse propagation through SMF and gain fiber represented by \( F \) and \( G \) are solved by NLSE [38] using a split-step Fourier method. The gain saturation model is given in Eq. (3.22), where \( g0 \) is the small signal gain coefficient (related to dopant concentration), \( E \) is the instantaneous pulse energy and \( Esat \) is the gain saturation energy which is pump-power dependent. For the non-gain single mode fiber, saturated gain factor \( g \) is set to zero to eliminate the influence of the gain effect.

\[
g = \frac{g0}{1 + \frac{E}{Esat}} \text{ and } Tz = \frac{2}{\Delta n} \tag{3.22}
\]

If two polarizations are included in the cavity simulation, NLSE is replaced by CNLSE. The model assumes equal gain for the two polarizations and the high Birefringence fiber Jones matrix [51] is given as:

\[
T = M_{H1-H2} = \begin{pmatrix} e^{-i(2\pi \Delta n L)/\lambda} & 0 \\ 0 & e^{i(2\pi \Delta n L)/\lambda} \end{pmatrix} \tag{3.23}
\]

Where \( L \) is the length of the fiber, \( \Delta n \) is the fiber birefringence and \( \lambda \) is the operating wavelength. Other components of the round-trip model like gain, saturable absorption, mirrors, etc., usually do not distinguish between the two polarization components. The output signal after gain fiber \([52, 53]\) will be:

\[
\begin{pmatrix} E_{out}^x \\ E_{out}^y \end{pmatrix} = \sqrt{G} \cdot \begin{pmatrix} e^{-i(2\pi \Delta n L)/\lambda} & 0 \\ 0 & e^{i(2\pi \Delta n L)/\lambda} \end{pmatrix} \begin{pmatrix} E_{in}^x \\ E_{in}^y \end{pmatrix} \tag{3.24}
\]

Regarding the SSFM, the nonlinear operator should be changed to:
The cavity phase shift, $\varphi$ induced from the gain fiber section and represents the polarization rotation, is expressed as shown in Eq. (3.26).

$$\varphi = \varphi_n + \varphi_{NL} = \frac{2\pi n L}{\lambda_0} + \gamma yb L_{rb} |A|^2$$  \hspace{1cm} (3.26)

where $n$ is the birefringence of the PM fiber, $L_{rb}$ and $\gamma yb$ are the length and nonlinear coefficient of the gain fiber respectively. $\lambda_0$ is the center wavelength. The first term in Eq. (3.26) represents the linear birefringence of the PM fiber [54, 55] while the second is a nonlinear phase shift proportional to the intra-cavity field power. This term in the model is part of the pulse phase shift evolution and rotation that plays a major role in the performance of the SML laser. If two m polarizations are included in the cavity simulation, NLSE should be replaced by CNLSE. At such a case, a new cavity phase shift for each polarization will be introduced as:

$$\varphi_n = \frac{2\pi n L_{rb}}{\lambda_0}$$  \hspace{1cm} (3.27a)

$$\varphi_{NL} = \gamma yb L_{rb} |A|^2$$  \hspace{1cm} (3.27b)

c) FBG (Spectral filtering components and Output coupler)

Both HR-FBG (RHR) and OC-FBG (ROC), their reflectivity spectra are modeled with a Gaussian function with a bandwidth of 0.2 nm and center wavelength $\lambda_0$ of 1064 nm. The output is taken at the 50% OC-FBG. The filter function is represented in frequency domain [52] as shown in Eq. (3.28). That is the reason to apply FFT for the input signal before applying to filter section. At the filter output, IFFT operation is applied to the output signal.

$$SF(f) = \exp\left(-2\ln\frac{2}{\Delta f^2}\right)$$  \hspace{1cm} (3.28)

where $SF(f)$ is the filter transfer function in frequency domain and $\Delta f$ is the filter’s 3dB bandwidth.

For the two polarization simulations, PM FBG will be modeled with a reflectivity matrix with two wavelengths [67, 68] and spectral filtering component as

$$\begin{pmatrix} r_1 & 0 \\ 0 & r_2 \end{pmatrix}$$  \hspace{1cm} (3.29)

$r_1$ and $r_2$ is the reflectivity of both PM FBG axes.

d) Initialization Pulse

The simulation is initialized by small amplitude Gaussian pulse of FWHM of 1ns. For the two polarization simulation, two Gaussian pulses will be used to represent each polarization as shown in Eq. (3.30).

$$\begin{pmatrix} g_{out,n} \\ g_{out,o} \end{pmatrix} = \begin{pmatrix} r_1 & 0 \\ 0 & r_2 \end{pmatrix} \begin{pmatrix} g_{in,n} \\ g_{in,o} \end{pmatrix}$$  \hspace{1cm} (3.30)

### 3.4. Simulation Parameters & Results

<table>
<thead>
<tr>
<th>Gain fiber</th>
<th>SM fiber</th>
<th>FBGs</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fiber Length (L)=10 m</td>
<td>Fiber Length (L)=0.25 m</td>
<td>HR-FBG reflectivity (RHR)=0.99</td>
</tr>
<tr>
<td>2nd order dispersion ($\beta_2$)=0.024 ps2/m</td>
<td>2nd order dispersion ($\beta_2$)=0.024 ps2/m</td>
<td>OC-FBG reflectivity (ROC)=0.5</td>
</tr>
<tr>
<td>Nonlinear coefficient ($\gamma$)=0.0016 W-1 m-1</td>
<td>Nonlinear coefficient ($\gamma$)=0.0016 W-1 m-1</td>
<td>FBG 3dB BW ( $\Delta\lambda$3dB)=0.2 nm</td>
</tr>
<tr>
<td>Small signal gain (go)=0.1 m-1</td>
<td>Small signal gain (go)=0</td>
<td>Center wavelength ($\lambda_0$)=1064 nm</td>
</tr>
<tr>
<td>Saturation energy (Esat)=2 nJ (Pump parameter)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Gain bandwidth ($\Delta\omega_{g}$)= 45 nm</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Birefringence ($\Delta n$)=3 x10-4</td>
<td>Birefringence ($\Delta n$)=3 x10-4</td>
<td>-</td>
</tr>
</tbody>
</table>
The numerical simulation starts with a 1 ns Gaussian pulse as an initial condition and we examine the output after 10000 round trips. In one round-trip, the propagation of the optical pulses is solved in every section of the laser. After one round-trip through the laser cavity, the resulted pulse from simulation was used as the input for the next round-trip calculation. The outcome results of the proposed model are studied at different conditions. The model is first tested without adding the phase shift parameter to verify its role in pulse formation. The simulation output without and with this term is shown in Figure 3.3(a) to (e) and overall linewidth after mode-locking is shown in figure 3.4.

The figure 4.8 shows the line-width ranging from 1063.995nm to 1064.005nm. This shows a very very precise line-width at 1064nm of 0.01nm wide. In this research when the iteration time is made 4000 times the pulse width becomes 0.01nm.

4. Conclusions

The mode-locking mechanism for the proposed laser can be explained using NPR. The laser is designed such that PM-FBG pair selects one polarization which is amplified by the cavity. However, a small component of the other orthogonal polarization can also evolve inside the cavity. The walk-off between the two orthogonal polarizations accumulates while propagating along the cavity. Thus the propagating light will be elliptically polarized and its rotation becomes intensity dependent. When the elliptically polarized light reaches the OC-FBG, the light component aligned with fast axis will only pass it. Thus the laser output is linearly polarized. The PM-FBG pair in the laser cavity acts as a polarizer through which intensity-dependent rotation is transformed into intensity dependent transmission. This serves as a fast artificial SA and generates mode-locked output pulses.

Acknowledgements

I would like to express my gratitude to my supervisor lecturer omnath acharya for his unreserved support and guidelines.

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