
Modeling and Fuzzy Command of a Wind Generator

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Abstract: A problem of mechanical modeling and robustly stabilization of a wind generator is considered. To overcome the non-linearity of the system, the model of the wind generator is approximated by a Takagi-Sugeno fuzzy model. To stabilize the obtained fuzzy model, two command approaches were developed. They are the fuzzy controller using the parallel distributed compensation (PDC) and the H_∞ controller based-fuzzy observer. Numerical optimization problems using linear matrix inequality (LMI) and convex techniques are used to analyze the stability of the wind generator. Finally, simulation examples illustrating the control performance and dynamic behavior of the wind generator under various command approaches are presented.

Keywords: Modeling, TS-Fuzzy Control, H_∞ Command, LMI Approach, Stability

1. Introduction

Wind energies were well developed and exploited and became competitive thanks to the evolution of the power electronics. Nevertheless, the optimal exploitation of the renewable energy sources encountered many problems which are related mainly to the uncertain variation of the wind speed. To resolve these problems and to improve the penetration rate and the stability level of the connected wind system, several controls are developed focusing this subject. These commands illustrate performance limits such as instability and implementation complexity.

Recently many studies have been devoted to the stability of the non-linear system. Fuzzy control constitutes a preferment command which has attracted an increasing attention because it can offer an effective solution to the control of complex, uncertain and undefined system [1-3]. The well-known Takagi-Sugeno (TS) fuzzy method has become a convenient approach for dealing with a complex system. This approach provides an effective representation of the system with the aid of fuzzy sets, fuzzy rules and a local linear model. The Takagi Sugeno fuzzy model [4] constitutes a productive way to describe and control the dynamics of nonlinear systems [5]. The TS fuzzy dynamics model is a system described by the fuzzy 'if-then' rules which offer local linear representation. The advantages of using this

approach for design control are that the closed loop stability analysis using Lyapunov method becomes easier to apply and the controller synthesis can be reduced to convex problem [6]. Once the nonlinear models are transferred to a fuzzy model, control design can be carried out. Some of them are fuzzy controller using parallel distribution compensation (PDC) and the fuzzy observer-based H_∞ controller. The PDC approach employs multiple linear controllers corresponding to the locally linear plants [7]. Many applications illustrate the effectiveness of the TS models and parallel distribution compensation [4, 8]. Fuzzy observer-based H_∞ controller has been developed in [9, 10]. Stability and aptitude to reject exterior disturbances provided by this command approach were approved in [11].

In this work, the TS-fuzzy approach is used to approximate the nonlinear wind generator model. Two approaches of robust and powerful commands to stabilize the mechanical part of the wind generator are presented. In the first part, a fuzzy controller design uses the concept of PDC [7, 12] is studied. In the second part, a fuzzy observer-based H_∞ controller is developed in order to improve the performance of the system and to minimize the disturbance effect of the wind speed. Sufficient stability conditions are expressed in terms of LMI which can be solved very efficiently using convex optimization techniques [6]. Finally, simulation examples are given to illustrate both stability and robustness analysis of the proposed control systems.

2. Description and Modeling of the Wind Generator

The drive train of the wind turbine generator system consists of the following elements: a blade-pitching

mechanism, a hub with blades, a rotor shaft, a gearbox and generator. The common way to model the drive train is to treat the system as a number of discrete masses connected together by springs defined by damping and stiffness coefficients (Figure 1).

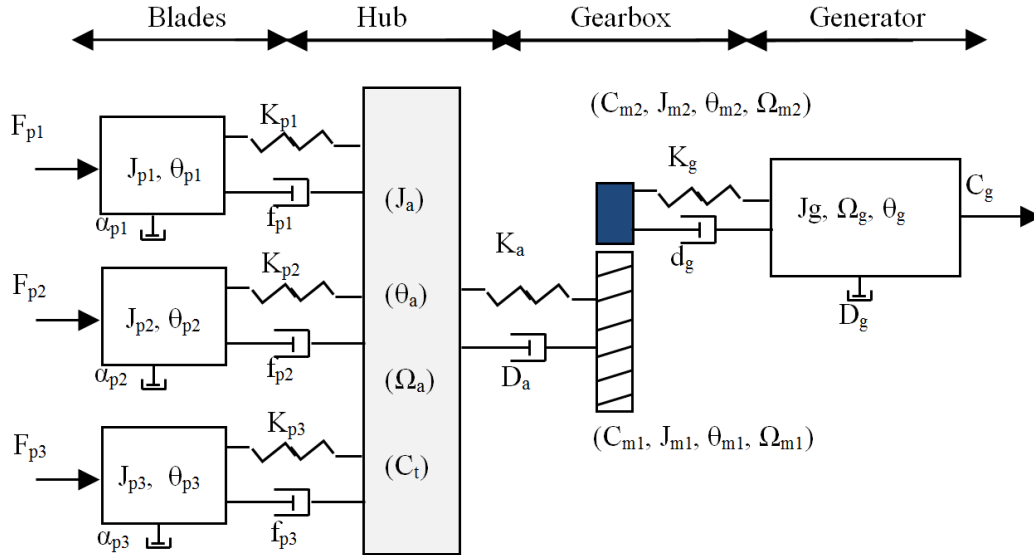


Figure 1. Transmission model of 6 masses connected together.

The aerodynamic part is made of three blades, hub, gearbox and generator. This system has six inertias; three blade inertias (J_{p1}, J_{p2} and J_{p3}), hub inertia J_a , gearbox inertia J_m (J_{m1}, J_{m2}) and generator inertia J_g . The elasticity between adjacent masses is expressed by $K_{p1}, K_{p2}, K_{p3}, K_a$ and K_g . The mutual damping between adjacent masses is given by $f_{p1}, f_{p2}, f_{p3}, D_a$ and d_g . There exist torque losses through external damping elements represented by α_{p1}, α_{p2} and α_{p3} . $\theta_{p1}, \theta_{p2}, \theta_{p3}, \theta_a, \theta_m$ and θ_g represent respectively angular positions of the blades, the hub, the gearbox and the generator. $\Omega_{p1}, \Omega_{p2}, \Omega_{p3}, \Omega_a, \Omega_m$ (Ω_{m1}, Ω_{m2}) and Ω_g are respectively the angular velocities of the blades, hub, gearbox and generator. F_{p1}, F_{p2} and F_{p3} are aerodynamic torques acting on each blade. The sum of the blade torques constitutes the turbine torque C_t . C_m (C_{m1}, C_{m2}) and C_g are respectively the gearbox and generator torques. It is assumed that the aerodynamic torque acting on the hub is zero.

In order to simplify the control of the wind generator, we introduce some simplifications on the six masse models. The turbine inertia can be calculated from the combined weight of the blades and the hub. Therefore, the mutual damping and elasticity between the hub and the three blades is ignored ($K_{p1}=K_{p2}=K_{p3}\approx 0$ and $f_{p1}=f_{p2}=f_{p3}\approx 0$). The torque losses of the blades (α_{p1}, α_{p2} and α_{p3}) are ignored because turbine speed is very weak. Moreover, it is assumed that the three blades have uniform weight distribution ($F_{p1}=F_{p2}=F_{p3}=F_p$) and the turbine torque is assumed to be equal to the sum of the torque acting on the various blades. Thus, the turbine can be looked as a large disk with small thickness and the wind system (three blades, hub, gearbox and generator) can be modeled by three masses coupled through a gearbox as indicated by Figure 2.

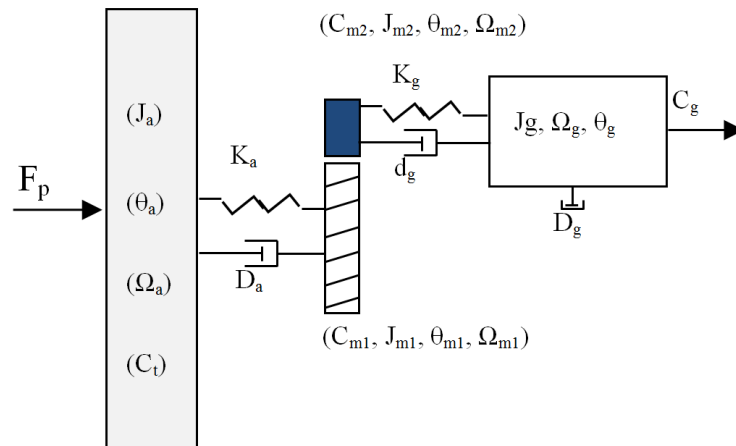


Figure 2. Three-mass model.

In addition, compared with the mechanical characteristics of the blades and the generator, the gearbox inertia and mutual damping with adjacent masses moment of inertia are ignored. Therefore, the complex system can be simplified to be two-mass model through reforming the dynamic system with the equivalent stiffness and damping coefficients. As a consequence, the two-mass model contains two parts which represent the wind turbine and the generator. They are connected by a flexible shaft. This model will be used to investigate the control of the wind turbine.

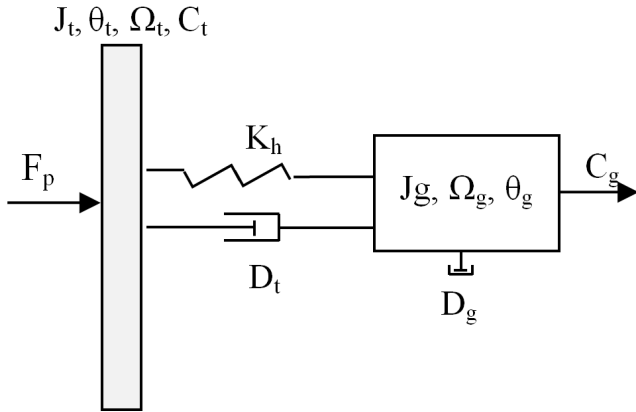


Figure 3. Two-mass model.

Referring to the simplified diagram given by Figure 3 and the Newton's second law for rotational masses, the dynamic system can be formulated with respect to the wind turbine rotor and the electromagnetic generator [13].

$$\begin{cases} j_t \ddot{\theta}_t + D_t(\Omega_t - \Omega_g) + K_h(\theta_t - \theta_g) = C_{aer} \\ j_g \ddot{\theta}_g + D_t(\Omega_g - \Omega_t) + K_h(\theta_g - \theta_t) = -C_g \end{cases} \quad (1)$$

With

- J_t, J_g : turbine and generator inertias [kgm²].
- C_{aer}, C_g : aerodynamic and electromagnetic torques of the turbine and generator [Nm].
- Ω_t, Ω_g : angular speed of the turbine and generator [rd/s].
- θ_t, θ_g : angular displacement of the turbine and generator [rd].
- K_h : elasticity between the turbine and the generator [Nm/rd].
- D_t : damping between the turbine and the generator [Nms/rd].

According to eq.1, the model of the conversion system is written as:

$$\begin{cases} \frac{d(\Omega_t)}{dt} = \frac{K_h}{j_t} \theta_s - \frac{D_t}{j_t} (\Omega_t - \Omega_g) + \frac{C_{aer}}{j_t} \\ \frac{d(\Omega_g)}{dt} = \frac{K_h}{j_g} \theta_s + \frac{D_t}{j_g} (\Omega_t - \Omega_g) - \frac{C_g}{j_g} \end{cases} \quad (2)$$

And θ_s is the torsion angle of the blades. It is given by:

$$\theta_s = \theta_t - \theta_g \quad (3)$$

By differentiating equation (3) with respect to time and

organizing equation (2) in term of Ω_t and Ω_g , the overall model of the wind generator system can be given as follow:

$$\begin{bmatrix} \dot{\theta}_s \\ \dot{\Omega}_t \\ \dot{\Omega}_g \end{bmatrix} = \begin{bmatrix} 0 & 1 & -1 \\ -\frac{K_h}{j_t} & -\frac{D_t}{j_t} & \frac{D_t}{j_t} \\ \frac{K_h}{j_g} & \frac{D_t}{j_g} & -\frac{D_t}{j_g} \end{bmatrix} \begin{bmatrix} \theta_s \\ \Omega_t \\ \Omega_g \end{bmatrix} + \begin{bmatrix} 0 \\ \frac{C_{aer}(V,\beta)}{j_t} \\ -\frac{C_g(V,\beta)}{j_g} \end{bmatrix} \quad (4)$$

With $x(t) = \begin{bmatrix} \theta_s \\ \Omega_t \\ \Omega_g \end{bmatrix}$ is the vector of the variables of state and

$z = \begin{bmatrix} V \\ \beta \end{bmatrix}$ is the input vector and C_g is the electromagnetic torque of the generator.

According to [14], the aerodynamic torque C_{aer} is a nonlinear function. It depends on the wind speed V and pitch angle β . It is given by:

$$C_{aer}(V, \beta) = \frac{0.5 * C_p(\lambda, \beta) \rho \pi R^2 V^3}{\Omega_t} \quad (5)$$

With:

$$\lambda = \frac{G.V}{R.\Omega_g} \quad (6)$$

We assume that $z_0 (V_0, \beta_0)$ is an equilibrium point. So we would like to find the linear system when C_{aer} (4) is close to $z_0 (V_0, \beta_0)$. Then the nonlinear system may be approximated by:

$$C_{aer}(V, \beta) = C_{aer,\beta}(z_0)\beta + C_{aer,V}(z_0)V \quad (7)$$

In addition, the electromagnetic torque of the machine is a nonlinear function. It depends on the angular velocity Ω_g and the operating speed Ω_f . It is approximated since [15], by:

$$C_g = D_g(\Omega_g - \Omega_f) \quad (8)$$

With D_g is the damping between the generator and the nacelle [Nms/rd].

It is better to use the mechanical representation instead of the electric representation. With this intention, we introduce the variable β in order to obtain a command which was independent on the activation terms. It is supposed that the blade speed, around a value β_d placed in a linear area, can be written as [15]:

$$\dot{\beta} = -\frac{1}{\tau_\beta} \beta + \frac{1}{\tau_\beta} \beta_d \quad (9)$$

Where τ_β is the constant time of the blade movement.

Then, replacing C_{aer} and C_g by their expressions given by (8) and (9) in (4), we obtain the increased dynamic model of the wind generator. It can be expressed by [16]:

$$\begin{cases} \dot{x}(t) = A(z)x(t) + B_1 u(t) + B_2 V \\ y(t) = Cx(t) \end{cases} \quad (10)$$

With:

$$A(z) = \begin{bmatrix} 0 & 1 & -1 & 0 \\ -\frac{K_h}{J_t} & -\frac{D_t}{t} & \frac{D_t}{J_t} & \frac{C_{aer,\beta}(z_0)}{J_t} \\ \frac{K_h}{J_g} & \frac{D_t}{J_g} & -\frac{(D_t+D_g)}{J_g} & 0 \\ 0 & 0 & 0 & -\frac{1}{\tau_\beta} \end{bmatrix}; B_1 = \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & \frac{D_g}{J_g} \\ \frac{1}{\tau_\beta} & 0 \end{bmatrix}; B_2 = \begin{bmatrix} 0 \\ \frac{C_{aer}(z_0)}{J_t} \\ 0 \\ 0 \end{bmatrix}; x(t) = \begin{bmatrix} \theta_s \\ \Omega_t \\ \Omega_g \\ \beta \end{bmatrix} \quad u = \begin{bmatrix} \beta_d \\ \beta \end{bmatrix}$$

$$y = \Omega_g \text{ and } C = [0 \quad 0 \quad 1 \quad 0]; z = \begin{bmatrix} V \\ \beta \end{bmatrix}$$

2.1. TS Fuzzy Model

The objective of this approach is to approximate the nonlinear system by linearized sub-systems. It has been used as an alternative to classical models to capture dynamic performances under different operating conditions and in different functioning zones.

The description of the nonlinear system in terms of ‘‘If-Then’’ rules combined with a mathematical description of non-linear systems is called a Takagi-Sugeno fuzzy model. The concept of sector nonlinearity provided means for exact approximation of nonlinear systems by fuzzy blending of set locally linearized sub-systems. The TS system is defined as follows:

If $z_1(t)$ is F_{i1} and... and $z_p(t)$ is F_{ip} then [17]:

$$\dot{x}(t) = \frac{\sum_{i=1}^M w_i(z(t))(A_i x(t) + B_i u(t))}{\sum_{i=1}^M w_i(z(t))} = \sum_{i=1}^M \mu_i(z(t))(A_i x(t) + B_i u(t)) \quad (11)$$

Where:

$$\mu_i(z(t)) = \frac{w_i(z(t))}{\sum_{i=1}^M w_i(z(t))}, w_i(z(t)) = \prod_{j=1}^p F_{ij}(z_j(t)) \text{ and } w_i(z(t)) \geq 0 \text{ When } t \geq 0.$$

The output signal is obtained by the same technique:

$$y(t) = \sum_{i=1}^M \mu_i(z(t)) C_i x(t) \quad (12)$$

The term $\mu_i(z(t))$ determines the activation terms of the associated local models. According to the functioning zone of the system, these terms indicate the contribution of the local model. They allow a progressive passage of a local model to another and they depend on the state vector. They can be in triangular or Gaussian forms. They satisfy the conditions given in [17].

$$\begin{cases} \sum_{i=1}^M \mu_i(x(t)) = 1 \\ 0 < \mu_i(x(t)) \leq 1 \end{cases} \quad (14)$$

2.2. TS Fuzzy Description of the Wind Generator

We consider the TS fuzzy models based on the nonlinear sectors [18, 19] to represent the nonlinear model of the wind

$$\text{If } \beta \text{ is } F_1^1 \text{ and } V \text{ is } F_2^1 \text{ then } \begin{cases} \dot{x}(t) = A_1 x(t) + B_1 u(t) + B_{21} w \\ y = C_1 x(t) \end{cases}$$

$$\text{If } \beta \text{ is } F_1^1 \text{ and } V \text{ is } F_2^2 \text{ then } \begin{cases} \dot{x}(t) = A_2 x(t) + B_1 u(t) + B_{22} w \\ y = C_2 x(t) \end{cases}$$

$$\text{If } \beta \text{ is } F_1^2 \text{ and } V \text{ is } F_2^1 \text{ then } \begin{cases} \dot{x}(t) = A_3 x(t) + B_1 u(t) + B_{23} w \\ y = C_3 x(t) \end{cases}$$

Where $x(t) \in \mathfrak{R}^n$ is the state vector, M is the number of rules ‘‘If-Then’’, F_{ij} represent the corresponding fuzzy set. They are the degree of membership of $z_i(t)$, $i = \{1, \dots, p\}$, $u(t) \in \mathfrak{R}^m$ is the control input vector, $y(t) \in \mathfrak{R}^q$ is the output vector. $A_i \in \mathfrak{R}^{n \times n}$, $C_i \in \mathfrak{R}^{q \times n}$ and $B_i \in \mathfrak{R}^{n \times m}$ are system matrices of appropriate dimension. $z_1(t) \dots z_p(t)$ are non-linear functions of the state variables. They are called as premise variables.

The inferred system states are governed by:

system composed of a turbine, a driving shaft and an induction machine. This approach based on the transformation of the scalar functions and the bornitude of the continuous variables V and β . These variables are limited as given by the following equations.

$$V_{min} \leq V \leq V_{max} \text{ and } \beta_{min} \leq \beta \leq \beta_{max}$$

According to the model given by the equation (10), the system has two non linearities depending on V and β . To linearize this model, we will use the presentation of TS previously presented. For those non-linearities, the base comprises four rules ‘If-Then’. Thus, the nonlinear wind system is represented by the following fuzzy model:

If β is F_1^2 and V is F_2^2 then
$$\begin{cases} \dot{x}(t) = A_4x(t) + B_1u(t) + B_{24}w \\ y = C_4x(t) \end{cases}$$

Then the inferred system is given by:

$$\begin{cases} \dot{x}(t) = \sum_{i=1}^4 \mu_i(z(t))((A_i x(t) + B_1 u(t) + B_{2i} w)) \\ y = \sum_{i=1}^4 \mu_i(z(t)) C_i x(t) \end{cases} \quad (15)$$

Where $\mu_i(z(t))$ are activation terms of the subsystems. They are given by:

$$\begin{cases} \mu_1(z) = F_1^1(\beta)F_2^1(V) \\ \mu_2(z) = F_1^1(\beta)F_2^2(V) \\ \mu_3(z) = F_1^2(\beta)F_2^1(V) \\ \mu_4(z) = F_1^2(\beta)F_2^2(V) \end{cases} \quad (16)$$

$$A_1 = A_2 = \begin{bmatrix} 0 & 1 & -1 & 0 \\ -\frac{K_h}{J_t} & -\frac{D_t}{J_t} & \frac{D_t}{J_t} & \frac{C_{aer,\beta 1}}{J_t} \\ \frac{K_h}{J_g} & \frac{D_t}{J_g} & -\frac{(D_t+D_g)}{J_g} & 0 \\ 0 & 0 & 0 & -\frac{1}{\tau_\beta} \end{bmatrix}; A_3 = A_4 = \begin{bmatrix} 0 & 1 & -1 & 0 \\ -\frac{K_h}{J_t} & -\frac{D_t}{J_t} & \frac{D_t}{J_t} & \frac{C_{aer,\beta 2}}{J_t} \\ \frac{K_h}{J_g} & \frac{D_t}{J_g} & -\frac{(D_t+D_g)}{J_g} & 0 \\ 0 & 0 & 0 & -\frac{1}{\tau_\beta} \end{bmatrix}$$

$$B_{21} = B_{23} = \begin{bmatrix} 0 \\ C_{aer,V1} \\ J_t \\ 0 \\ 0 \end{bmatrix}; B_1 = \begin{bmatrix} 0 & 0 \\ 0 & D_g \\ 0 & J_g \\ \frac{1}{\tau_\beta} & 0 \end{bmatrix}; B_{22} = B_{24} = \begin{bmatrix} 0 \\ C_{aer,V2} \\ J_t \\ 0 \\ 0 \end{bmatrix}; C = [0 \quad 0 \quad 1 \quad 0]$$

With:

$$C_{aer,\beta 1} = C_{aer,\beta}(\beta = \beta_1), C_{aer,\beta 2} = C_{aer,\beta}(\beta = \beta_2)$$

$$C_{aer,V2} = C_{aer,V}(V = V_2), C_{aer,V1} = C_{aer,V}(V = V_1)$$

3. Stabilisation of the Wind Generator

3.1. By Fuzzy Controller: Parallel Distribution Compensation

The concept of this command, named parallel distributed compensation (PDC), is used to stabilize the fuzzy system. It employs linear controllers corresponding to the locally linear plant model. The general diagram of the PDC is given by Figure 4.

The general structure of the PDC is given by [20]: If $z_1(t)$ is M_1 and $z_2(t)$ is M_2, \dots , and z_p is M_p then $u(t) = -K_j x(t)$, $j=1, 2, \dots, M$. Consequently the overall PDC fuzzy controller is represented by:

$$\dot{x}(t) = \sum_{i=1}^4 \sum_{j=1}^4 \mu_i(z(t))(\mu_j(z(t)) (A_i - B_1 K_j)x(t) + B_{2i} w) \quad (19)$$

The fuzzy controller design consists in determining the local feedback gain K_j ($j=1, 2, 3, 4$) for the corresponding parts of TS models so that the zero equilibrium of the closed loop fuzzy systems was globally stable. We apply the quadratic stability theorem of the global system, yields the following results [9]: the equilibrium of the closed loop system (19) is globally stable, if there is a common positive definite matrix P which satisfies the following conditions:

With F_i^j are the degrees of membership function of the activation terms. They are given by:

$$\begin{cases} F_1^1(\beta) = \frac{\beta - \beta_1}{\beta_2 - \beta_1} \\ F_1^2(\beta) = \frac{\beta_2 - \beta}{\beta_2 - \beta_1} \\ F_2^1(V) = \frac{V - V_1}{V_2 - V_1} \\ F_2^2(V) = \frac{V_2 - V}{V_2 - V_1} \end{cases} \quad (17)$$

With $V_1=V_{min}, V_2=V_{max}, \beta_1=\beta_{min}$ and $\beta_2=\beta_{max}$.

For $i = \{1 \dots 4\}$, the matrices A_i, B_1, B_{2i} and C are given by:

$$u(t) = -\frac{\sum_{j=1}^4 w_j(z) K_j x(t)}{\sum_{j=1}^4 w_j} = -\sum_{j=1}^4 \mu_j(z(t)) K_j x(t) \quad (18)$$

Where K_j are the feedback gain matrices for the subsystems.

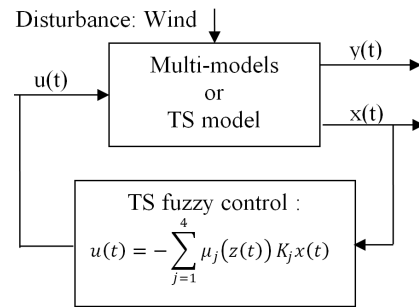


Figure 4. General diagram of parallel distributed compensation.

By substituting (18) into (15), we get the overall closed loop fuzzy controlled systems as follows:

$$\begin{cases} -XA_i^T - A_iX + B_iM_i + (B_iM_j)^T > 0 \\ -XA_i^T - A_iX - XA_j^T - A_jX + M_j^T B_i^T + B_iM_j + M_i^T B_j^T + B_jM_i \geq 0 \end{cases} \quad (20)$$

The objective of the command is in finding K_1, K_2, K_3 and K_4 and $P > 0$ that satisfy the conditions presented by equation 20. An approach to design a stable fuzzy controller for the wind generator is to transform the condition in equation 20 into convex problem [1, 21-23]. The solution of the stable PDC controller design problem via linear matrix inequalities (LMI) for the system leads to:

$$K_j = M_jX^{-1} \text{ with } P = X^{-1} \quad (21)$$

If the solution of the LMI (eq. 20) is found, it means that local state feedback gains K_j ($j=1, 2, 3$ and 4) provide quadratic stability of the closed loop TS fuzzy systems. Hence, using matlab toolbox, the controller parameters are found to be:

$$K_1 = \begin{bmatrix} -4225 & -1645 & 2225 & -208 \\ -1 \cdot 10^8 & -10^7 & 77 \cdot 10^4 & -992 \cdot 10^2 \end{bmatrix} \quad K_2 = \begin{bmatrix} -4225 & -1645 & 2225 & -208 \\ -1 \cdot 10^8 & -1.05 \cdot 10^7 & 77 \cdot 10^4 & -992 \cdot 10^2 \end{bmatrix}$$

$$K_3 = \begin{bmatrix} -4225,5 & -1644,85 & 2265 & -208,35 \\ -1,08 \cdot 10^8 & -1.05 \cdot 10^7 & 77,04 \cdot 10^4 & -992,1 \cdot 10^2 \end{bmatrix} \quad K_4 = \begin{bmatrix} -4225,45 & -1644,82 & 2265 & -208,32 \\ -1,065 \cdot 10^8 & -1.05 \cdot 10^7 & 77,05 \cdot 10^4 & -992,1 \cdot 10^2 \end{bmatrix}$$

Table 1. Parameters of the wind system.

Symbol	Quantity	Value
K_h	Elasticity of driving shaft	$1.566 \times 10^6 \text{Nm}^{-1}$
D_r	Damping factor shaft-nacelle	$3029.5 \text{Nmsrad}^{-1}$
D_g	Damping factor IG-gearbox	$15.993 \text{Nmsrad}^{-1}$
J_g	Inertia of IG	5.9kgm^2
J_p	Inertia of blades	830000kgm^2
ρ	Air density	1.225kgm^{-3}
R	Blade radius	30.3m
$\tau\beta$	Time constant of the blade movement	100ms
P	Rated power of the IG	1MW
p	Pole pair number of the IG	3
λ_{opt}	Optimal specific speed	7
C_{pmax}	Coefficient of maximal power	0.48
γ	Desired level disturbance attenuation	0.6
$C_{aer,\beta1}$	Aerodynamic torque corresponding to the pitch angle β_1	723980Nm
$C_{aer,\beta2}$	Aerodynamic torque corresponding to the pitch angle β_2	376070Nm
$C_{aer,v1}$	Aerodynamic torque corresponding to the wind speed V_1	106440Nm
$C_{aer,v2}$	Aerodynamic torque corresponding to the wind speed V_2	85370Nm

The choice of the wind speed profile is arbitrary. For that, we consider a sinusoidal form of a wind speed which varies between 17 and 32km/h. The main objective is to test and analyze the performance of the PDC controller.

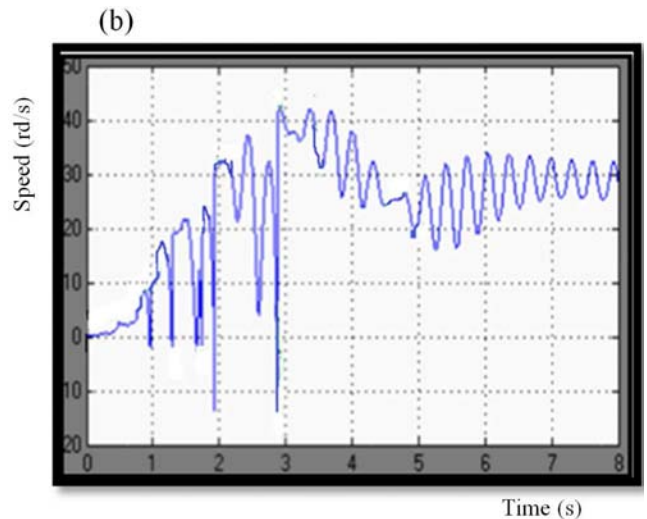
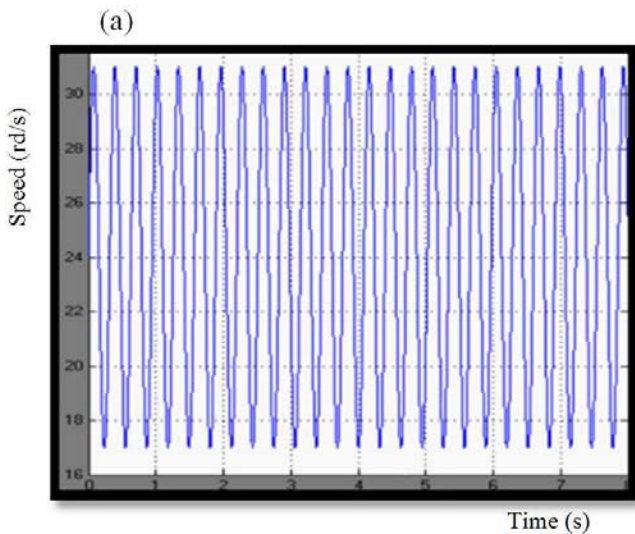


Figure 5. Wind profile and speed variation of the IG.

We notice that the form of the wind speed generates disturbances on the machine speed according to Figure 5a. The generator speed is not stable and oscillates (Figure 5b). These oscillations can cause vibrations and harmful effects

on the driving shaft. The PDC controller is insufficient and does not allow a stability of the overall system. To overcome this problem, we will use another preferment command which is able to eliminate the oscillatory effect on the operating of the overall system.

3.2. By Fuzzy Observer-Based H_∞ Controller

The approach is to develop a robust command which permits to obtain robustness stability in analytical way.

$$\begin{cases} \hat{\dot{x}}(t) = A_i \hat{x}(t) + B_1 u(t) + B_{2i} w(t) - L_i (y(t) - \hat{y}(t)) \\ \hat{y}(t) = C_i \hat{x}(t) \end{cases} \quad (22)$$

Where L_i is the observer gain for the i^{th} observer rule. The overall fuzzy observer is represented as follows:

$$\begin{cases} \hat{\dot{x}}(t) = \sum_{i=1}^4 \mu_i(\hat{z}(t)) (A_i \hat{x}(t) + B_1 u(t) + B_{2i} w(t) - L_i (y(t) - \hat{y}(t))) \\ \hat{y}(t) = \sum_{i=1}^4 \mu_i(\hat{z}(t)) C_i \hat{x}(t) \end{cases} \quad (23)$$

Where $\hat{x}(t) \in \mathcal{R}^n$ and $\hat{y}(t) \in \mathcal{R}^h$ are respectively the estimated state and output vector.

The stabilization of the generator speed is essentially a disturbance rejection problem. Thus, a robust control using H_∞ technique is well adopted to resolve this kind of control problem. It is assumed that the fuzzy systems are locally controllable. Hence, a fuzzy controller with the following rules can be used.

If $\hat{z}_1(t)$ is F_{i1} and... $\hat{z}_p(t)$ is F_{jp}
Then $u(t) = K_j \hat{x}(t)$, for $j=1$ to 4.

Hence, the fuzzy control is given by [9]:

$$u(t) = \sum_{j=1}^4 \mu_j(\hat{z}(t)) K_j \hat{x}(t) \quad (24)$$

With K_j are the controller gains.

Let use a new variable which present the estimation error. It is given by:

$$e(t) = \hat{x}(t) - x(t) \quad (25)$$

The closed loop fuzzy model of the wind system integrating the TS model (15), the fuzzy observer (23) and the controller (24) became:

$$\begin{pmatrix} \dot{\bar{x}}(t) \\ \dot{\bar{z}}(t) \end{pmatrix} = \sum_{i=1}^4 \sum_{j=1}^4 \mu_j(z(t)) \mu_i(z(t)) \begin{pmatrix} \bar{A}_{ij} & \bar{B}_i \\ \bar{C} & 0 \end{pmatrix} \begin{pmatrix} \bar{x}(t) \\ w(t) \end{pmatrix} \quad (26)$$

With:

$$\bar{A}_{ij} = \begin{pmatrix} A_i + B_1 K_j & B_1 K_j \\ 0 & A_i + L_i C \end{pmatrix}; \bar{B}_i = \begin{pmatrix} B_{2i} \\ 0 \end{pmatrix}; \bar{C} = (C \ 0)$$

The general diagram of the fuzzy observer-based H_∞

According to the TS system represented by equation 12, some state variables are un-measurable. Hence, it was obligatory to synthesize an observer which make possible to estimate those variables (θ_s and β). The design of fuzzy observer obliges that the local models of the system should be locally observables, and is obtained by interpolation of several Luenberger observer. The observer is introduced as follows:

If $\hat{z}_1(t)$ is F_{i1} and... $\hat{z}_p(t)$ is F_{ip} , then for $i=1 \dots 4$, the observer states are governed by [24]:

controller is given by Figure 6.

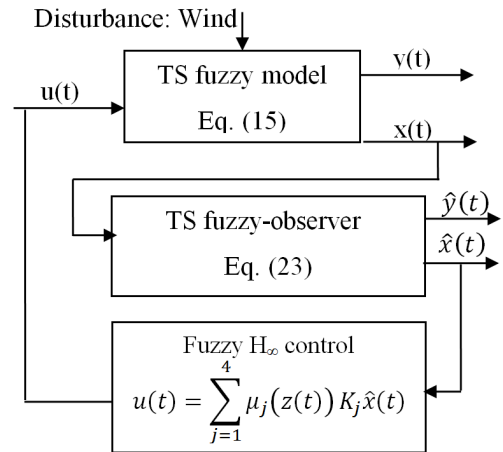


Figure 6. General diagram of the H_∞ command with fuzzy observer.

For the formulation of the main result, we recall the following theorem and definition.

Definition: given a scalar $\gamma > 0$, system (26) is stable with H_∞ disturbance attenuation γ if it is exponentially stable with:

$$\int_0^\infty z^T(t) z(t) - \gamma^2 w^T(t) d(t) < 0 \quad (27)$$

γ is the desired level disturbance attenuation [6].

Theorem: the system (26) is stable with H_∞ disturbance attenuation γ , if there are symmetrical matrices $X > 0, Y > 0, Q_i > 0, P_i, M_i$ and J_i which satisfy the following linear matrix inequalities for $i < j = \{1, 2, 3, 4\}$ [6]:

$$X A_i^T + A_i X + B_1 M_i + M_1^T B_1^T + \gamma^{-2} B_{2i} B_{2i}^T < P_i \quad (28)$$

$$X(A_i + A_j)^T + (A_i + A_j)X + B_1(M_i + M_j) + (M_i + M_j)^T B_1^T + \gamma^{-2}(B_{2i} B_{2i}^T + B_{2j} B_{2j}^T) < P_i + P_j \quad (29)$$

$$A_i^T Y + Y A_i + C^T J_i^T + J_i C < Q_i, i = 1, 2, \dots, m \quad (30)$$

$$\begin{bmatrix} P_1 & \dots & 0 & X C^T \\ \vdots & \ddots & P_m & X C^T \\ C X & C X & -I & \end{bmatrix} < 0 \quad (31)$$

With the controller and observer gains are given by:

$$\begin{cases} K_i = M_i X^T \\ L_i = Y^T J_i \end{cases} \quad (32)$$

By applying the above theorem and the LMI optimization toolbox in matlab, to solve the equations 29-32, with four fuzzy rules, we obtain set feasible solutions. Hence, the controller parameters are:

$$K_1 = 10^6 \begin{bmatrix} 0.0273 & 0.0000 & -0.0001 & -0.0000 \\ 2.1542 & 0.0042 & -0.0042 & 0.0000 \end{bmatrix} \quad K_2 = 10^6 \begin{bmatrix} 0.0275 & 0.0000 & -0.0001 & 0.0000 \\ 2.1543 & 0.0042 & -0.0042 & 0.0000 \end{bmatrix}$$

$$K_3 = 10^6 \begin{bmatrix} 0.1096 & 0.0002 & -0.0002 & 0 \\ 2.1504 & 0.0042 & -0.0042 & 0 \end{bmatrix} \quad K_4 = 10^6 \begin{bmatrix} 0.1022 & 0.0002 & -0.0002 & 0 \\ 2.15043 & 0.0042 & -0.0042 & 0 \end{bmatrix}$$

The observer gains are given by:

$$L_1 = \begin{bmatrix} -0.6766 \\ -1.367 \\ -0.65416 \cdot 10^3 \\ 0.5244 \end{bmatrix}; \quad L_2 = \begin{bmatrix} -0.5749 \\ -1.1588 \\ -0.5488 \cdot 10^3 \\ 0.3478 \end{bmatrix}; \quad L_3 = \begin{bmatrix} -0.5442 \\ -1.1062 \\ -0.52 \cdot 10^3 \\ 0.475 \end{bmatrix}; \quad L_4 = \begin{bmatrix} -0.6043 \\ -1.2213 \\ -0.57274 \cdot 10^3 \\ 0.3947 \end{bmatrix}$$

Figure 7 represents the variation curve of the generator speed. A stabilization of the generator speed around 30rd/s is ensured. The proposed control minimizes the generator speed ripple and maintains stability of the system during wind disturbances. Thus, this result demonstrates the performances of the command which is insensitive to the disturbance coming from the variation of the wind speed. The command seems a powerful technique for the disturbance rejection. In addition, the generator speed follows its reference with an error equal to 8%.

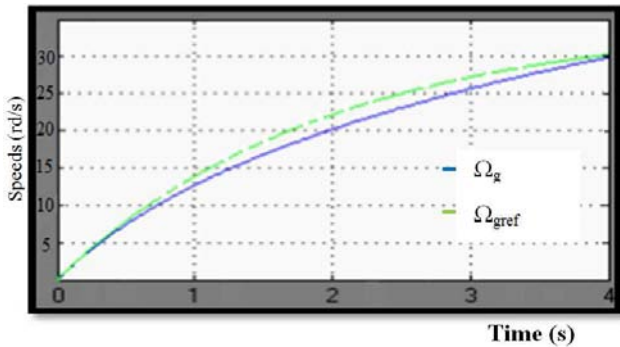


Figure 7. Variation curve of the generator speed (measure and reference).

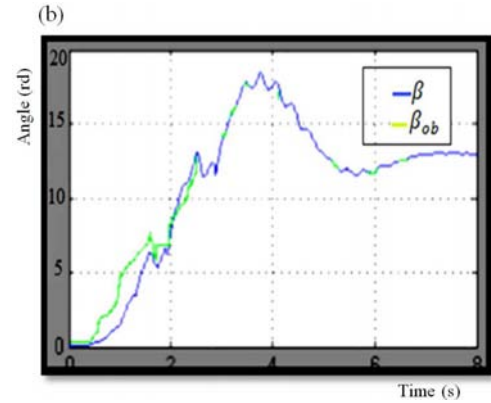


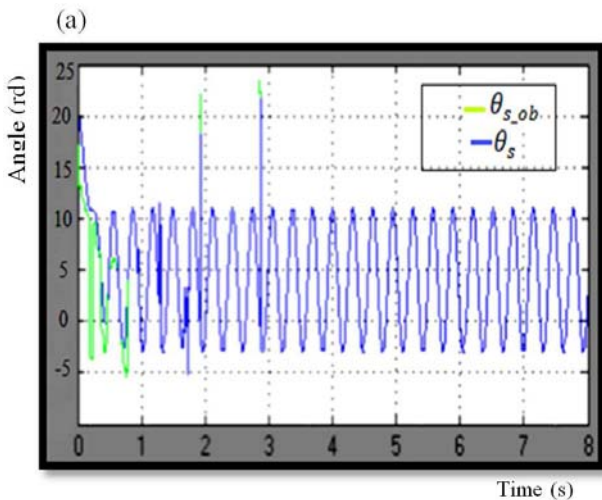
Figure 8. Variation of the state variables of the system: (a): torsion angle; (b): pitch angle.

Curve 8 represents the variation of the state variables of the TS fuzzy system. Figure 8a represents the estimated and measure angle torsion of the driving shaft. Figure 8b represents the variation of the pitch angle of the blades. The measured and estimated values are confused justifying consequently the performances of fuzzy observer-based H_∞ controller.

4. Conclusion

In this paper, an approach of modeling and control of a nonlinear system based-wind generator is discussed. In the first part, a TS fuzzy model is used to approximate the dynamics of wind generator composed of a turbine, a driving shaft and an induction machine. In the second part, two command approaches are developed around the complex system in order to stabilize the mechanical model and to minimize the generator speed ripple. Numerical optimization problems using linear matrix inequality and convex techniques are used to design the controller and the observer parameters.

Stability results for closed model based fuzzy controller using the concept of PDC have been examined assuming that all of the system states are measurable. The generator speed



curve shows that the fuzzy controller can't stabilize the response of system when the wind speed varies. The proposed command scheme using fuzzy observer-based H_∞ controller illustrates some good performances. It minimizes the generator speed ripple, maintains stability of the system during wind disturbances and permits the attenuation of the external disturbances. The obtained results illustrate the effectiveness of this approach to stabilize the nonlinear system. Moreover, they showed the ability of the command to reject the disturbances and make possible to obtain a stable wind generator without oscillations. Therefore, we consider that the fuzzy observer-based H_∞ controller is appropriate for the nonlinear system control with external disturbances.

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