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# Optimization of Soil Sampling Design Based on Road Networks – A Simulated Annealing/Neural Network Algorithm

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**Abstract:** In this study, the spatial distribution pattern of the roads, historical samples, digital elevation data, and other available resources were incorporated into the design of a soil-sampling scheme to predict the soil organic matter (SOM) of the northern region of Zhongxiang City, Hubei Province, and simulated annealing (SA) was applied to optimize the sampling design. The sampling points determined after optimization were used to establish a multivariate linear regression model to adequately reproduce the intrinsic link between topographic factors and the SOM at 13 different sampling scales in areas nearby the existing roadways in the study area. The topographic factors included slope, plane curvature, profile curvature, topographic wetness index (TWI), stream power index (SPI), and sediment transport index (STI). A multilayer perceptron (MLP) model was also constructed. Comparison of the accuracy of the multivariate linear regression and MLP models demonstrated the feasibility of an optimized soil sampling design based on the road network. With the optimized sampling design, accurate soil-landscape information can be obtained, and its precision is greater than that of the original sampling scheme before optimization. The optimized sampling design obtained reduces sampling costs, increases sampling efficiency, and provides an effective method for obtaining the spatial distribution pattern of organic matter in soils.

**Keywords:** Soil-landscape Model, Simulated Annealing (SA), Multilayer Perceptron (MLP), Sampling Design Optimization

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## 1. Introduction

The soil sampling design with specific spatial layouts aims to obtain accurate soil attributes over a broad area. It plays an important role in the arable land fertility assessment, precision agriculture, and digital soil mapping. Collecting soil samples in the field requires tremendous work and resources, and it is therefore critical to establish an optimal sampling distribution and the number of total samples. Conventional soil sampling methods can be divided into three broad categories: classical sampling that involves collecting a large number of samples within a specific distribution pattern [1], spatial sampling that uses the spatial autocorrelation of geographic attributes [2], and purposive sampling, which is a non-random method that depends on prior knowledge and data mining technology [3].

Soil sampling design begins from the premise of an appropriate sampling scale, and seeks to ensure that the sample set presents an adequate representation of the entire area. Typically, sampling design can be optimized with expert knowledge approaches, geostatistics, or approaches based on representativeness of sample [4-6]. These methods, however, suffer from limitations such as a dependence on empirical knowledge, second-order stationary assumptions, and quasi-intrinsic assumptions [7].

To reduce the uncertainties caused by the limitations of conventional sampling design optimization methods, auxiliary methods that provide indicators of spatial distribution patterns have been used in the optimization of the soil sampling design. For example, optimization of the soil sampling design can be aided by monitoring the spatial distribution of soil properties

via X-ray diffraction [8]. The design of the sampling scheme can also be optimized by developing a spatial map of soil properties (e.g. soil salinity, clay content and pH) based on the soil conductivity derived from electromagnetic induction [9-10]. Moreover, the representativeness of spatial distributions of soil salinity has been improved using predictive models based on remote sensing data to reduce the number of on-site samples [11]. Models that account for the effects of spatial differences in soils have been employed to assist the sampling design. For example, to balance the accuracy and cost of soil sampling, mathematical diffusion models have been used to determine optimal sampling densities [12]. Analysis of the spatial layout of soil properties has also employed soil environment reasoning models to improve the predicative precision of a limited number of sampling points [13]. Such considerations of the spatial distributions of soil attributes, including cofactors, seek to ensure that the layout of the fewest possible number of sampling points represent the overall environment. In this manner, the optimization of the sampling design is achieved. Topographic features and road networks also have spatial distribution patterns, and can be used as cofactors in the soil sampling design.

It is of significant interest to note that road networks ease the field soil sampling work over large areas. Road networks are characterized by a specific structure and spatial density that have a bearing on the usefulness of the road network as a cofactor in soil sampling design. Moreover, with the continued development of urban-rural integration, the density and spatial layout of road networks are expected to be gradually stabilizes [14]. For field soil sample collection on a countywide scale, the location of the sampling points and the sampling sequence can be roughly determined according to the road layout. However, researches that optimize the soil sampling strategies with the spatial distribution of networks are quite limited.

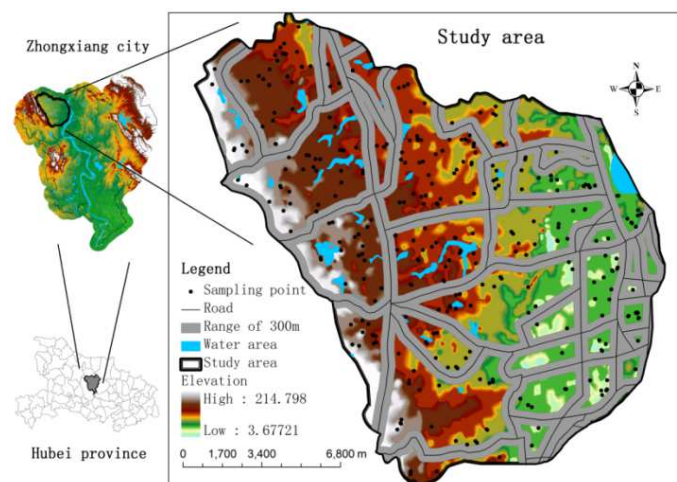
To acquire the soil-landscape information inherent to the

typical soils of a region, several sampling points of high representativeness should be determined in the corresponding region based on the predictions of statistical models. The spatial distributions of soil properties show a continuous change [15]. For a sufficiently dense road network that covers the corresponding soil area, it can be expected that highly representative soil regions exist nearby the existing roadways. The sampling area can thus be established within a prescribed distance from roads, and the optimal layout of the sampling points can be arranged according to the distribution pattern of the road network. Since soil-landscape information remains stable over time, the knowledge and patterns of soil distribution contained in historical soil samples can be utilized. To optimize the soil sampling design and explore the overall soil properties, a soil organic matter (SOM) landscape model can be established to predict the SOM content. The SOM was chosen because SOM has a major impact on soil properties, although its fraction is minimal in soil.

In this study, the spatial distribution of the roads, historical samples, digital elevation data, and other available resources were incorporated into the design of a soil-sampling scheme. The simulated annealing (SA) was applied to optimize the sampling design. The sampling points determined after optimization were used to establish a multivariate linear regression model of the soil-landscape. Then, a multilayer perceptron (MLP) model was used to evaluate the predictive accuracy of the regression model, and this predictive precision was, in turn, used to assess the sampling design. The established MLP model was found to adequately reproduce the intrinsic link between topographic factors and the SOM, showing a high predictive precision. The MLP model can make efficient use of available knowledge, and provides strong generalization and nonlinear mapping abilities. Thus, the prediction results of this model can be used to test the SOM of sampling points after optimization.

## 2. Study Area and Methods

### 2.1. Study Area



**Figure 1.** Location of the study area, road networks in the study area, and the spatial distribution of the historical sampling points. The shaded areas are 300-m buffer areas of the roadways.

The study area is located in the northern region of Zhongxiang City, Hubei Province, China ( $31^{\circ}21' - 31^{\circ}33'N$ ,  $112^{\circ}13' - 112^{\circ}27'E$ ), with an area of  $244 \text{ km}^2$ . This location is in central Hubei Province, to the west of the upper Hanjiang River, as shown in Figure 1. The area is of mixed topography including hills, low mountains, and plains. The highest elevation is 215 m, and the elevation gradually decreases from west to east. The 319 historical sampling points shown in Figure 1 are distributed among different terrain and soil types, and were subjected to random sample collection in 2005–2006. The road network has a density of  $0.78 \text{ km} \cdot \text{km}^{-2}$ , which covers the entire study area with a rather uniform distribution.

## 2.2. Methods

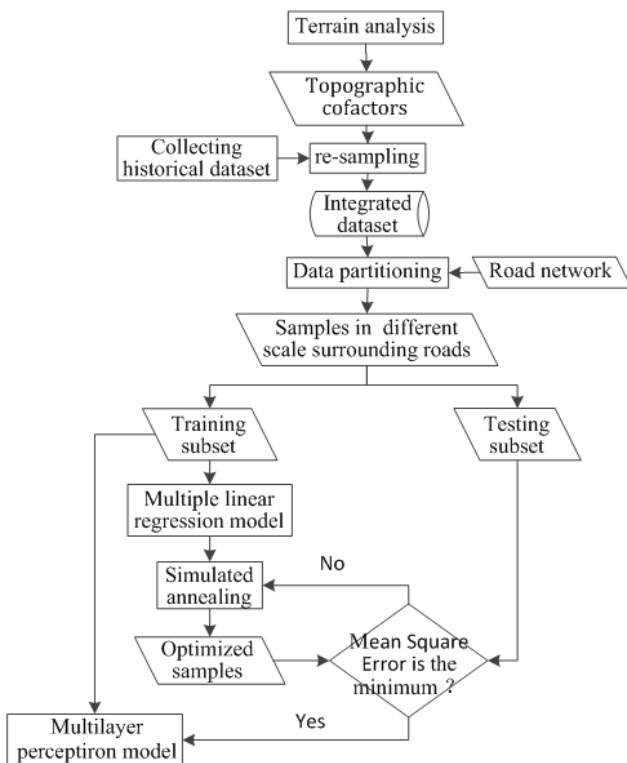


Figure 2. Flowchart of the proposed method.

The development and distribution of soil within the overall landscape result from interactions between numerous soil-forming factors [16]. The historical sampling data, regardless of the rationality of the spatial layout of the sampling points, provides soil-landscape knowledge specific to the region. The basic premise of the soil sampling design method proposed in the present study is as follows (Figure 2). Digital elevation model is used in the terrain analysis to obtain topographic cofactors. Widely distributed historical samples are collected and re-sampled with the topographic cofactors. The integrated dataset is partitioned based on road network. The samples from both sides of the scale's roadways are employed. The soil-landscape relationship is established using multiple linear regressions of the topographic cofactors. Using the precision of the soil-landscape model as the objective function, an SA algorithm is subsequently applied to optimize

the sample set of the spatial layout iteratively until the error of the soil-landscape model is minimized. The initial and optimized data sets are then used to establish the MLP model, and the test data set is used to compare the precision of the model before and after sampling optimization to evaluate the performance of the optimization.

### 2.2.1. Selection and Acquisition of Topographic Cofactors

The significance of different topographic factors varies among landscapes. We used previous soil-landscape studies [17–18] to select commonly used topographic factors that have major impacts on the actual soil environment. The topographic cofactors chosen to characterize the soil distribution in the study area include elevation, slope, plane curvature, profile curvature [19], topographic wetness index (TWI) [20], stream power index (SPI) [21], and sediment transport index (STI) [22]. Digital elevation model (DEM) raster data with a 30 m resolution were obtained from the international scientific data mirror site maintained by the Computer Network Information Center of the Chinese Academy of Sciences (<http://datamirror.csdb.cn>), and were used to calculate the topographic factors. To provide smooth and continuous data, the above factors were calculated at a 10 m resolution. The topographic factors at the historical sampling points were extracted to ensure that the corresponding topographic factors appropriately represented the surrounding environment.

The soil sampling locations were based on the spatial distribution pattern of the roadways, and all sampling points were required to be at least 300 m away from all railways and roadways [23]. To explore the effects of the sampling scale on the precision of the final results, 13 sampling scales were established according to a 10-pixel increment (i.e., 100 m): 300–400, 300–500, ..., 300–1600 m. The sampling scale is the range over which samples can be obtained. The 300–1600 m scale covers the entire study area. At the same sample scale, overlapping regions between different roads were combined. At each sampling scale, the historical samples served as the initial sample set, and these were randomly divided into the training data set and the test data set in a 2:1 ratio. The training dataset therefore accounted for 2/3 of the initial sample set, and was used to train the model. The remaining was the test dataset used to validate the model.

### 2.2.2. Establishment of the Soil-landscape Model

For each sample set designed using the road network, the SOM content of the historical samples obtained from both sides of the roadways and the topographic factors were employed to establish a multiple linear regression model using Matlab 8.0 (Math Works, Natick, Massachusetts, USA). The mean square error (MSE) was calculated to evaluate the prediction accuracy. In this way, the soil-landscape model was established using the initial data set. This model was then used to optimize the spatial layout of the sampling points surrounding the roadways. Meanwhile, an MLP model was established using Neuro Solutions 6.31 (Neuro Dimension, Gainesville, Florida, USA). MLP is one of the commonly used

feed forward artificial neural network (ANN) types for non-linear function approximation task which learns the pattern of data by several layers with connected perceptrons [24-25]. In this study, the seven selected topographic factors were served as the input layer, and the output layer was the SOM content. In addition, the model incorporates two hidden layers. The conversion function employed by the software is its default hyperbolic tangent function, denoted as Tanh Axon, and the learning algorithm is the Momentum algorithm. The Step Size and Momentum Rate are both software defaults. The termination conditions were a maximum number of iterations of 105 and a threshold value of 10<sup>-4</sup>. Based on the input data, the optimal number of neurons in each hidden layer calculated by the software was 4. Since the weight corresponding to each factor is very important, the weights are continuously optimized during the neural network computation to achieve optimal prediction results. Due to the high uncertainty of the neural network method, the data were trained five times, and the weights obtained during each training session were saved in a separate file. The model corresponding to the weights with the most precise prediction results was selected to build the soil-landscape model.

**2.2.3. Optimization of the Spatial Layout of the Sampling Points**

The historical sample data were used to select highly representative sampling points to achieve the optimization of the spatial distribution of the sampling points. SA is a stochastic computing technique, which employs a combinatorial optimization algorithm that converges to a global optimum while effectively avoiding local optima [26]. The algorithm has no strict requirements for the initial state of the study object. Hence, the SA algorithm can be used to solve complex deterministic combinatorial optimization problems [27-28]. In the past study, SA optimization was used to predict the spatial distribution of soil properties with a minimum number of samples while maintaining a predictive precision that was no smaller than that obtained using the original samples, thereby obtaining an optimal sample layout [27]. Another study used the average Kriging variance as the objective function in the SA algorithm [29]. In this case, the spatial layout of the samples was mainly assessed and optimized via two indicators, the main Kriging variance and the weighted Kriging variance, to obtain an optimum sampling design targeting different soil attributes. In the present study, the SA algorithm was applied, and the minimum

MSE of the SOM prediction was used as the criterion for optimization of the spatial layout of the soil sampling points to obtain the soil-landscape relationship with relatively high precision. The technique is therefore ideal for the present study because the determination of the optimal spatial layout of the sampling points is essentially a problem of combinatorial optimization between the sampling points. Each initial sample set was first optimized using the SA algorithm. The training data set was used to optimize the layout of the sampling points, and the test data set was used to validate the effectiveness of the optimized layout. A random subset of the training set was selected, and one of the remaining sampling points was randomly chosen to replace each point in the subset, one by one, until the sampling point in the subset most suitable for replacement was identified. This point was then replaced by the previously chosen point to form a new subset. Meanwhile, the multiple linear regression model of this data set was established, and the test data set was used to calculate the MSE, which is the objective function in the optimization process. During the iterative process described above, the MSE of each subset was determined based upon that subset's multiple linear regression model, and the MSE values of all subsets were compared. The subset corresponding to the smallest MSE was then accepted. In this way, the optimal sample set with the minimum predictive error in each initial sample set was obtained. The remaining sampling points were redundant points under the principle of the minimum MSE.

**2.2.4. Testing the Sample Layout Following Optimization**

We quantitatively analyzed the extent to which the information contained in the original sample set was contained in the optimized data set, and determined the impact of optimization on the precision of the SOM prediction. The MLP models established using the optimized data and the multiple linear regression models established as described in Subsection 2.2.3 were used to predict the SOM content in the test sample set, and these values were compared with the actual measured values for error analysis. The evaluation indices used for assessing the models are listed in Table 1, the Akaike information criterion (AIC) was used to measure the complexity of the model and its goodness of fit, and the minimum description length (MDL) principle was used to measure the quality of the prediction of the decision attribute set by the condition attribute subset. Lower absolute values for the above two indicators indicate greater model precision.

*Table 1. Overview of the evaluation indices used for assessing the models.*

Evaluation index	Formulas	Annotation
Mean square error (MSE)	$MSE = \frac{1}{n} \sum_{i=1}^n (\hat{y}_i - y_i)^2$	
Normalized mean square error (NMSE)	$NMSE = \frac{\sum_{i=1}^n (\hat{y}_i - y_i)^2}{\sum_{i=1}^n (y_i)^2}$	$n$ is the number of observations; $\hat{y}$ is the predicted value of the SOM; $y$ is the measured value of the SOM
Error (%)	$\%Error = \frac{\sum_{i=1}^n (\hat{y}_i - y_i)}{\sum_{i=1}^n y_i} * 100\%$	

Evaluation index	Formulas	Annotation
Correlation coefficient ( <i>r</i> )	$r = \frac{\sum_{i=1}^n (X_i - \bar{X})(Y_i - \bar{Y})}{\sqrt{\sum_{i=1}^n (X_i - \bar{X})^2} \sqrt{\sum_{i=1}^n (Y_i - \bar{Y})^2}}$	<i>n</i> is the number of observations; <i>X</i> is the value of a particular topographic factor; $\bar{X}$ is the mean value of the topographic factor; <i>Y</i> is the measured value of the SOM; $\bar{Y}$ is the mean value of the SOM
Akaike information criterion (AIC)	$AIC = 2k - 2\ln(L)$	<i>n</i> is the number of observations; <i>k</i> is the number of parameters; <i>L</i> is the likelihood function
Minimum description length (MDL)	$MDL = \frac{1}{2}k\ln(n) - \ln(L)$	

### 3. Results and Discussion

#### 3.1. Multiple Linear Regression Analysis of Topographic Factors Before and After SA Optimization

Table 2 shows the correlation between the topographic factors and the SOM.

**Table 2.** Pearson correlation coefficients between the soil organic matter (SOM) and the topographic factors in the study area.

	SOM	Elevation	Slope	Plan curvature	Profile curvature	Topographic Wetness index	Stream power index	Sediment Transport index
SOM	1							
Elevation	0.47**	1						
Slope	0.01	0.09	1					
Plan curvature	-0.09	-0.04	-0.04	1				
Profile curvature	0.10	0.02	-0.02	-0.60**	1			
Topographic wetness index	0.00	-0.18**	-0.16**	0.02	-0.07	1		
Stream power index	0.04	-0.10	0.20**	0.00	-0.06	0.82**	1	
Sediment transport index	0.05	-0.02	0.14*	0.02	-0.05	0.30**	0.30**	1

\*\**P*<0.01; \* *P*<0.05.

The number of sampling points and the SOM statistics at all sampling scales are listed in Table 3. The distribution patterns of the SOM are observed to be consistent at different sampling scales. The correlation coefficient (*r*) between the number of resampling points and the scale of the sampling area is 0.96, whereas the coefficient of determination of the linear

regression equation (R2) between the two is 0.91. Therefore the number of resampling points increases proportionally with the increasing scale of the sampling area and the ratio of the number of resampling points to the sampling scale is about 1.45 per square kilometer, which allows for comparison of the results obtained at different scales.

**Table 3.** Descriptive statistics of the soil organic matter in the study area with respect to the number of samples at each scale.

Sampling scale (m)	Number of samples	Soil organic matter (g•kg <sup>-1</sup> )						
		Minimum	Maximum	Average	SD*	Variance	Kurtosis	Skewness
300–400	82	9.83	46.54	26.59	8.39	70.33	-0.44	0.31
300–500	126	9.83	49.10	26.57	8.45	71.45	-0.39	0.38
300–600	170	9.76	54.70	26.31	8.80	77.47	-0.16	0.41
300–700	202	7.60	54.70	26.78	8.86	78.53	-0.20	0.33
300–800	222	7.60	54.70	26.97	8.69	75.50	-0.20	0.27
300–900	239	7.60	54.70	27.24	8.69	75.60	-0.28	0.22
300–1000	260	7.60	54.70	27.38	8.54	72.93	-0.27	0.20
300–1100	273	7.60	54.70	27.50	8.47	71.68	-0.25	0.16
300–1200	286	7.60	54.70	27.59	8.41	70.72	-0.25	0.15
300–1300	298	7.60	54.70	27.66	8.43	70.98	-0.16	0.18
300–1400	305	7.60	54.70	27.75	8.40	70.63	-0.15	0.18
300–1500	313	7.60	54.70	27.76	8.37	70.09	-0.15	0.16
300–1600	319	7.60	54.70	27.77	8.39	70.35	-0.19	0.15

\*Standard deviation.

We used the SA algorithm to reduce the number of sampling points. In this process, each time one point is removed, and an MSE value of a multiple linear regression model was obtained. As illustrated in Figure 3, as the sampling scale increases, the

number of sampling points in the initial data set increases, and the MSE gradually decreases, suggesting improved precision in SOM predictions. Also, as the optimization process proceeds (i.e., as the number of sampling points decreases),

the MSE of the multiple linear regression model gradually decreases until reaching a fairly level value. However, after a continued reduction in the number of sampling points, the MSE of the model rises sharply, and graphs of the MSE vs. the number of sampling points exhibit a clear U shape at all sampling scales.

Results shown in Figure 3 indicates that when restricting sampling points to areas surrounding the roadways, the precision of the obtained soil-landscape model after sampling

design optimization is superior to that before optimization at a given sampling scale. For sampling points set nearby roadways, there exists an optimal spatial layout design for which the precision of the obtained SOM prediction model is relatively high. Because the number of sampling points increases as the sampling scale increases, the knowledge of the soil covered by the SOM prediction model is more comprehensive, and, thus, the predictive precision is improved.

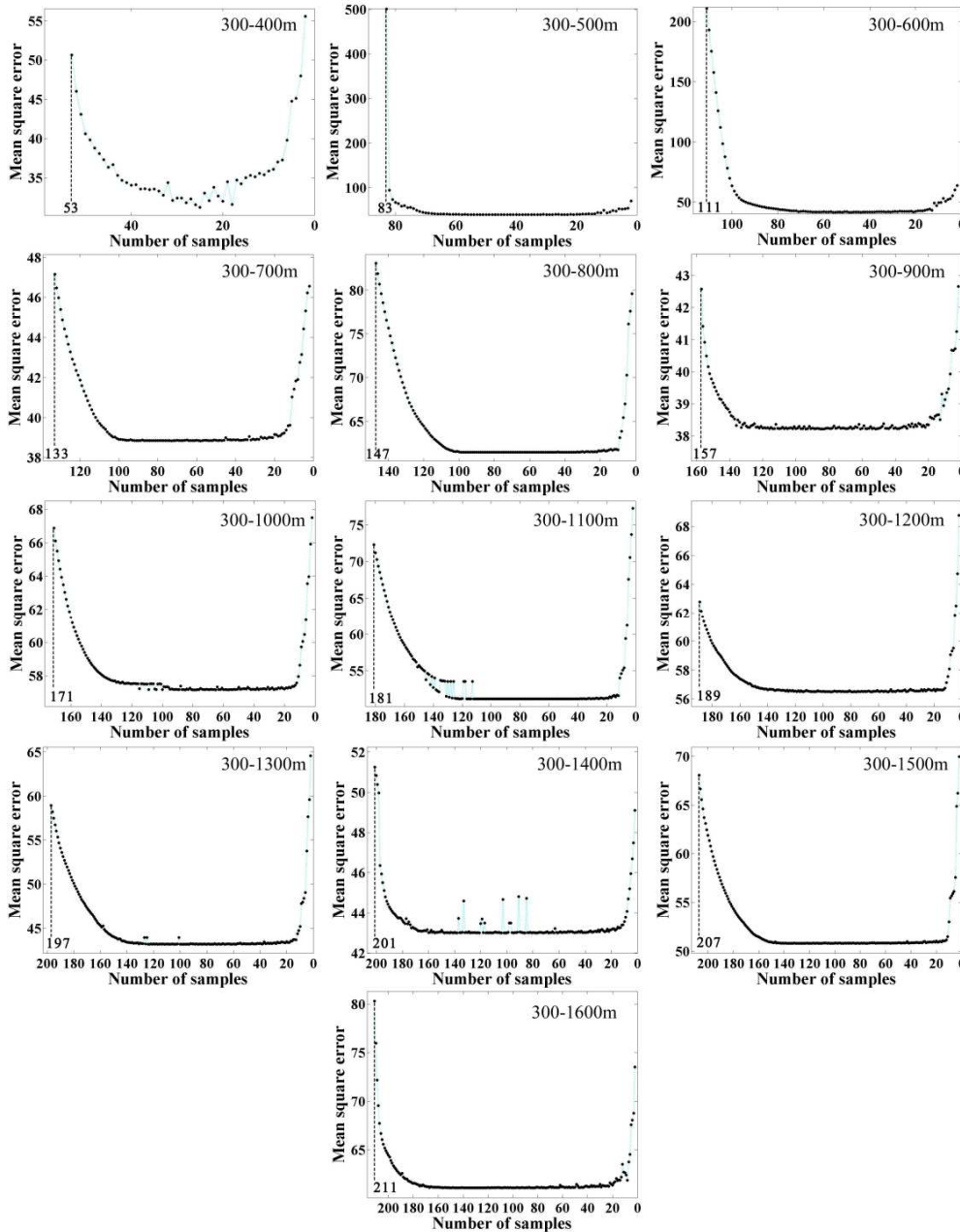


Figure 3. MSE values of the SOM predictions versus the number of samples during the process of optimization at different sampling scales.

We examined the effects of sampling design optimization at different sampling scales by applying multiple linear regressions to the initial sample set and the sample set after SA optimization at each sampling scale. Table 4 compares the coefficients of these models. Different topographic factors characterize different aspects of the landscape, and, thus, the

nature and magnitude of the impact on the SOM differ among different factors. Sample layout determines the representativeness of the sampling points. The integrity of the soil information contained in the sample sets collected at different scales varied, and the resulting soil-landscape models exhibit significant differences.

**Table 4.** Coefficients of multiple linear regression models for optimized and non-optimized sampling points at different sampling scales.

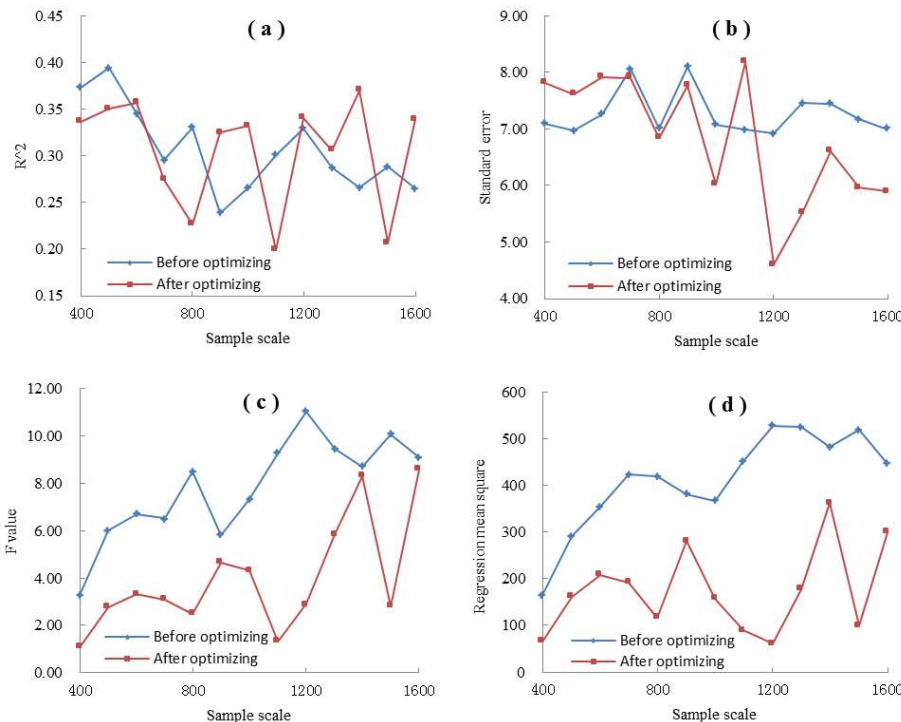
Sampling scale (m)	Constant		Elevation		Slope		Plan curvature		Profile curvature		Topographic wetness index		Stream power index		Sediment transport index	
	<i>a</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>a</i>	<i>b</i>
300–400	4.94	13.39	0.32	0.22	0.81	1.17	14.94	21.83	20.13	22.62	0.70	0.70	-0.52	-0.67	0.00	0.65
300–500	2.38	7.22	0.36	0.27	1.27	0.39	-3.14	-10.65	-7.81	18.94	0.58	0.90	-0.45	-0.34	0.14	-0.76
300–600	6.68	6.42	0.34	0.31	-0.03	0.97	-9.30	-0.86	-9.08	17.60	0.20	-0.47	0.10	0.93	-1.01	-1.57
300–700	10.51	7.39	0.32	0.28	-0.15	1.22	2.76	-15.38	7.00	-3.74	0.05	1.00	-0.06	-1.23	0.05	0.16
300–800	6.05	13.36	0.35	0.21	0.27	0.59	3.63	-10.56	3.18	2.10	0.06	0.39	0.04	-0.16	0.04	-1.31
300–900	9.45	8.02	0.28	0.34	0.07	-0.15	-3.94	-10.87	2.59	0.10	0.36	0.17	-0.06	0.01	-0.37	-1.10
300–1000	10.62	12.13	0.28	0.27	-0.02	-0.79	-1.37	-2.32	6.21	3.58	0.18	-0.07	0.12	-0.03	-0.07	1.32
300–1100	7.88	17.34	0.32	0.19	0.01	-0.44	1.22	-6.88	0.00	16.10	0.11	0.10	0.09	0.06	-0.03	-0.79
300–1200	9.26	11.72	0.31	0.21	-0.07	0.52	0.38	-3.46	7.00	4.99	0.11	1.41	0.10	-1.69	0.02	0.16
300–1300	7.62	15.08	0.32	0.22	-0.13	-0.78	-2.19	1.42	7.73	-2.37	0.11	0.16	0.13	-0.04	0.19	-0.25
300–1400	11.59	8.13	0.28	0.29	-0.43	0.31	-1.28	-7.77	7.25	-4.28	0.10	0.31	0.07	-0.13	0.02	-1.02
300–1500	10.49	16.83	0.30	0.19	-0.60	-0.17	-0.04	-4.90	9.40	-0.35	-0.16	-0.04	0.36	0.04	0.17	0.06
300–1600	11.60	12.79	0.27	0.26	-0.25	-0.37	1.41	-11.59	7.10	0.72	0.07	0.03	-0.05	0.26	0.40	-0.62

*a*: the value before optimizing; *b*: the value after optimizing.

### 3.2. Optimization Results of the Spatial Layout of the Sampling Points

We compared the regression models obtained at different sampling scales before and after optimization by performing analysis of variance (ANOVA). Figures 4(a) and (b) show that when the sampling scale is 300–1100 m or is less than 300–800 m, the coefficient of determination (R<sup>2</sup>) and standard error of the regression models after optimization of the sampling point layout are similar or less significant (i.e., lower R<sup>2</sup> and higher standard error) than those before optimization. At all the other sampling scales, R<sup>2</sup> and the standard error of the regression models after optimization are better than those before optimization. Figures 4(c) revealed that, before

optimization, the models at all sampling scales are statistically significant (P<0.05). After optimization, the models obtained at sampling scales 300–400 m and 300–1100 m are not statistically significant (P = 0.43 and P = 0.25, respectively), whereas, at sampling scales of 300–500 m, 300–800 m, and 300–1200 m, the models are all statistically significant (P = 0.02, P = 0.02, and P = 0.01, respectively). Figures 4(d) shows that, regression mean square of the regression models after optimization of the sampling point layout in different sample scale are less than those before optimization. Statistics shown in Figure 4 implies that sampling design optimization improves the precision of the regression model in most cases.



**Figure 4.** Statistics of the multiple linear regression models at different sampling scales before and after optimization.

The predictive precisions and the numbers of samples of the regression models obtained at different scales before and after optimization are shown in Figure 5. Figure 5(a) demonstrates that, at the sampling scales 300–500 and 300–600 m, the precisions of the models before optimization are relatively low, as indicated by the rather large MSE values. At sampling scales greater than or equal to 300–700 m, the predictive precisions of the models before optimization significantly improve, with MSEs values smaller than 119.52 g·kg<sup>-1</sup>. The MSE of the multiple linear regression model obtained using the original sample set is large, indicating that the precision of the SOM prediction is relatively low. After SA optimization of

the sampling point layout, the MSEs of the models are no greater than 62.47 g·kg<sup>-1</sup>, and the predictive precision of the model after SA optimization is greater than that before optimization for all sampling scales. From Figure 5(b), the number of samples after SA optimization in each sampling scale is less than that before SA optimization. These results indicate that the SOM prediction of the model after optimization is closer to the actual measurements than the prediction of the model before optimization. Hence, SOM models with relatively high predictive precision can be obtained when limiting sampling points to areas surrounding the roadways after SA optimization.

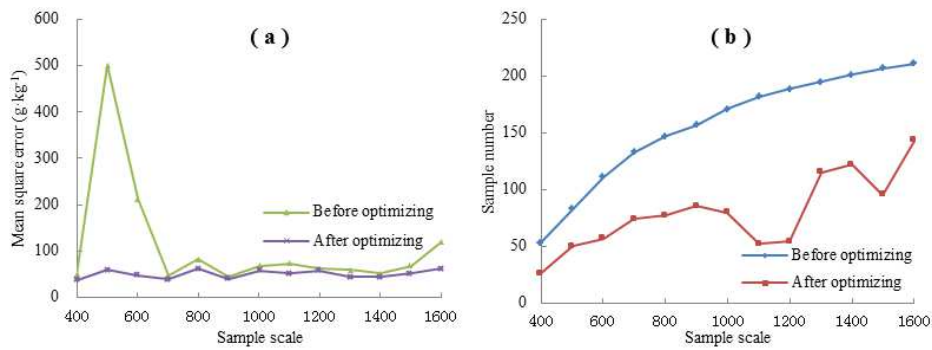


Figure 5. Comparison of the predictive precision and the number of samples of the regression models at different sampling scales before and after optimization.

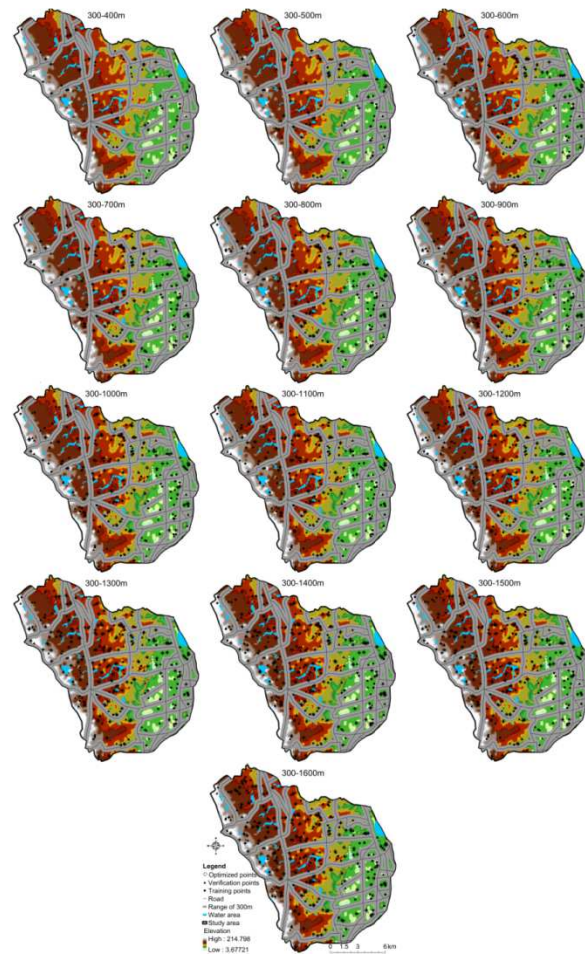


Figure 6. Comparison of the spatial layouts of the sampling points obtained before and after optimization at different sampling scales.



The comparisons of the spatial layouts of the sampling points before and after optimization at different sampling scales show that the sample points removed in the optimization are mainly located in low-elevation regions, valleys, and steep slopes (Figure 6). After optimization, the number of sampling points is substantially reduced, and this will notably decrease the workload and cost of the soil survey.

**3.3. Precision of the SOM Prediction**

MLP models were separately established using the training data set and sample set after SA optimization, and the test data set was then used to quantitatively assess the precision of the SOM prediction by the sampling points before and after optimization. Table 5 lists the values for the evaluation indices given in Table 3 obtained for all MLP models established using the original sample set before and after optimization at the different sampling scales surrounding the roadways. The NMSE values are all less than or equal to 0.49, the values of r

are all greater than or equal to 0.71, the Error values are all less than or equal to 17.5%, and the absolute values of the AIC and MDL both first increase with the increasing sampling scale, and then begin to decrease at sampling scales greater than 300–1300 m. For MLP models established using optimized sampling points, the NMSE values, r values, and error values are all superior to those obtained before sampling optimization because points that have a negative effect on the predictive precision of the model are excluded during the optimization. Moreover, the absolute values of the AIC and MDL remain less than or equal to 336.19 and 308.75, respectively, which are smaller than those obtained before optimization for all sampling scales. In addition, these results indicate that the established MLP models can adequately reproduce the intrinsic link between the topographic factors and the SOM, and the predictive precision is relatively high. The prediction results of the MLP model can be used to evaluate the accuracy of the SOM prediction after sampling optimization.

*Table 5. Precision of the multilayer perceptron model at different sampling scales.*

Sample scale (m)	Number of samples		NMSE		r		Error (%)		AIC		MDL	
	a	b	a	b	a	b	a	b	a	b	a	b
300–400	53	26	0.04	0.02	0.98	0.99	3.8	2.4	-150.96	-27.87	-151.80	-49.01
300–500	83	50	0.12	0.09	0.94	0.95	8.0	4.7	-203.04	-91.63	-191.10	-94.13
300–600	111	57	0.26	0.01	0.86	0.99	13.5	2.2	-273.96	-273.74	-253.73	-272.52
300–700	133	74	0.29	0.10	0.84	0.95	15.7	6.4	-295.41	-198.06	-270.03	-189.40
300–800	147	77	0.28	0.10	0.85	0.95	13.2	4.5	-362.32	-220.78	-334.09	-210.98
300–900	157	86	0.34	0.09	0.81	0.95	15.9	7.3	-391.44	-259.82	-361.34	-246.87
300–1000	171	79	0.32	0.13	0.83	0.94	14.1	7.0	-485.73	-206.84	-453.20	-196.31
300–1100	181	52	0.40	0.03	0.77	0.99	15.4	4.4	-456.90	-175.53	-422.74	-176.92
300–1200	189	54	0.46	0.11	0.74	0.94	16.7	3.9	-451.46	-105.50	-416.07	-105.81
300–1300	195	115	0.31	0.28	0.83	0.85	14.6	8.9	-536.92	-262.63	-500.35	-241.40
300–1400	201	122	0.34	0.25	0.81	0.87	15.5	11.4	-513.67	-291.55	-476.53	-268.63
300–1500	207	95	0.42	0.40	0.76	0.78	17.1	9.1	-504.65	-293.39	-466.66	-270.47
300–1600	211	143	0.49	0.31	0.71	0.83	17.5	11.1	-479.17	-336.19	-440.64	-308.75

a: the value before optimizing; b: the value after optimizing.

For all MPL models, an increasing sampling scale introduces an increasing number of sampling points into the optimization process. Hence, the representativeness of the points selected from the historical samples must be improved. Both before and after optimization, the errors increase slowly with the increasing sampling scale. We used the MLP model with relatively high predictive precision to test the precision of the sampling points before and after optimization, and found that, after optimization, all indicators improved. This suggests that the sample set after optimization can represent the original sampling points, and be used to establish a soil-landscape model with a relatively high predictive precision.

**4. Conclusion**

This paper proposed a method for designing optimized soil sampling layouts in areas residing within a confined distance from existing roadways using the SA algorithm and historical sample data. The sampling scale nearby the roadways can be selected according to different precision requirements. The

method was applied to a study area in the northern part of Zhongxiang City, Hubei Province, China. The SA algorithm was applied to optimize the historical sampling points, and MLP models with relatively high predictive precision were used to test the representativeness of the sample layout after optimization. The results show that, at all sampling scales, after SA optimization of the historical sampling points nearby the roadways, the number of sampling points was reduced on average by 49.2%, and SOM prediction of a relatively high precision was obtained, where the MSE of the SOM prediction was reduced by an average of over 48.8%. As the sampling scale increases, the predictive precision of the optimized sampling points gradually stabilizes, and the percentage error is less than or equal to 11.4%. Thus, the proposed approach conveniently and efficiently acquires a sampling design based on the spatial layout of the road network in the study area that includes highly representative sampling points while fully utilizing historical sample data to save the sampling costs and improve the sampling efficiency. The resulted sampling layout can be used as a reference for soil sampling in subsequent studies, and may be adjusted according to actual conditions to

achieve rational use of sampling resources while reducing the workload of the investigators.

Although the sampling design optimization method that targets areas surrounding roadways proposed in this study has yielded satisfactory results, several issues must be further examined. For example, the regression model selected to examine the relationship between the SOM and topographic features is a multiple linear regression model, and, for optimization of the sampling layout, the objective function used in the SA algorithm is the MSE. In addition, the parameters used to establish the MLP model for data testing (e.g., the number of hidden layers, training rules, and termination conditions) are set to the recommended default values provided by Neuro Solutions 6.31. The sensitivity of the SA algorithm to data quality also requires further exploration. In addition, experimental studies must be conducted to verify the applicability and efficiency of the proposed method for spatial sampling design targeting soil in other geological areas and in large-scale soil sampling.

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