

Stereo vision-based relative navigation algorithm for satellites formation flying

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Abstract: Space mission with multiple spacecraft formation is an important means to space operation. A new relative navigation algorithm based on stereo vision is developed aiming at high navigation precision requirement of spacecraft formation flying. It uses stereo vision camera attached on the tracking craft as measurement sensor, gets the relative location of target craft in the tracking craft body reference frame with imaging parallax. Relative motion equation is built in inertial frame, and discretized as the state equation of the system. Measurement information of stereo vision is used as measurement value, and the two-step filter relative navigation algorithm based on Kalman filter is designed to estimate relative navigation state in real time, and finally validated by simulation. The simulation results prove this algorithm can meet the relative navigation precision requirements of formation flying.

Keywords: Formation Flying, Stereo Vision, Relative Navigation, Two-Step Filter

1. Introduction

Formation satellites are termed as several mini satellites form certain flying contrail, and each mini satellite of the distributed satellite constellation works coordinately to accomplish the mission that a single satellite hardly to obtain.

Relative navigation is the precondition of spacecraft rendezvous, accompany and formation flying, especially in short range spacecraft formation flying mission, precision of which will directly affect the precision of navigation and control[1, 2, 3]. Several measure methods frequently are used in Space rendezvous and docking, including: micro-wave rendezvous radar, laser radar, satellite navigation and CCD optical imaging. Vision-based navigation of CCD optical imaging is a highly intelligentized navigation technology widely used in approaching and docking phases of space rendezvous and docking, which is small in volume, light in mass and low in energy consuming[4].

Stereo vision based relative state estimate scheme is addressed in this paper, which estimates the state of target spacecraft relative to the initial one with stereo vision. First, with spacecraft relative motion equation referring to the inertial frame, stereo vision measurement information as measurement equation, simplified stereo vision measurement

error model is built. Second, measurement noise was corrected in real time, and estimate relative position and speed using two-step filter algorithm based on Kalman filter. In the end, numerical simulation as well as validation of this navigation algorithm is made[5-7].

The use of vision system as the navigation and tracking sensor of space assets has become more and more attractive since it is a very efficient choice due to its compact size, low cost and rich information which provides. The nonlinear estimation framework for vision-based target measurement is addressed within this paper where space robot manipulation is considered as reference scenario. The work presented deals with the measurement of relative state parameter of the target including kinematic and dynamic parameters and its size from stereo vision, since the state vector is the basis for navigation and control in formation flying[8, 9].

In this paper, a stereo vision-based relative navigation algorithm for spacecraft formation flying is proposed and analyzed. Measurement information of stereo vision is used as measurement value, which is obtained by using the stereo vision. The relative motion equation in inertial frame is brought into the relative navigation system, to avoid the circular orbit assumption. The simulation results show that the algorithm is fine, can meet the relative navigation precision and stability requirements of formation flying.

2. Principles of Binocular Stereo Vision Measurement and Error Model

Parallel stereo vision model is the usually binocular stereo vision measurement model. Specifically, when the two cameras of the model are located parallelly, it is termed as standard vision model, illustrated in Fig.1. Assume coordination of the camera on both side are $O_l x_{cl} y_{cl} z_{cl}$ and $O_r x_{cr} y_{cr} z_{cr}$, each origin of the camera frame O_l , O_r is the optical center of the camera, axis x_c connecting the optical center, pointing to right camera, distance between two is b , termed as datum line, axis z_c is the light beam of the camera, axis y_c vertical to flat $x_c z_c$.

Assume coordinates of point P in left camera frame is (X_w, Y_w, Z_w) , $d = (u_l - u_r)$ is defined as binocular parallax of point P. If the parameter of the camera and parallax d is obtained, the coordinates of point $P(X_w, Y_w, Z_w)$ are:

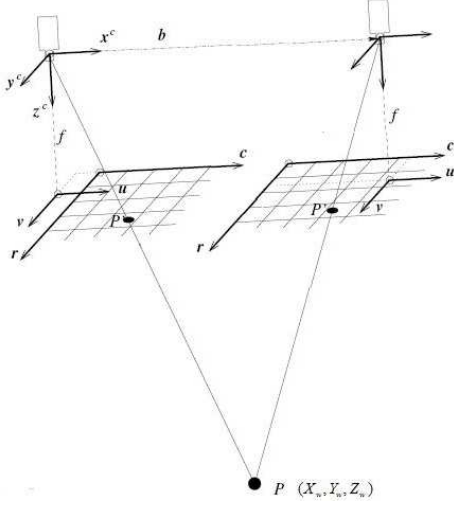


Fig 1. Principle of binocular stereo vision measurement

$$\begin{cases} X_w = \frac{b(u_l - u_0)}{u_l - u_r} \\ Y_w = \frac{bf_l(v_l - v_0)}{f_r(v_l - v_r)} \\ Z_w = \frac{bf_l}{u_l - u_r} \end{cases} \quad (1)$$

Where: u_0 , v_0 , f_l , and f_r are camera parameters, b is base line distance.

It is the key step demarcating camera and corresponding points matching, whose precision is the major factor of binocular stereo measurement. Stereo vision measurement error and precision of demarcating and matching are given by reference[8]:

$$\Delta z = \frac{z^2 \Delta \delta (z - f)}{fb(z - f) + z^2 \Delta \delta - 2zf \Delta \varepsilon - zf \Delta \delta} \quad (2)$$

Where: $\Delta \delta$ is the matching error of the two images, $\Delta \varepsilon$ is demarcating error. For the dimension of both $\Delta \delta$ and $\Delta \varepsilon$ is μm , much less than measurement distance z , the measurement error model can be simplified as follow:

$$\Delta z = \frac{z^2 \Delta \delta}{fb} \quad (3)$$

3. Stereo Vision-Based Relative Navigation Algorithm for Satellites Formation Flying

3.1. Spacecraft Relative Dynamic Equation

The relative dynamic equation could be given refer to the geocentric reference frame, as the relative distance of the spacecraft is much less than the distance between spacecraft and the core of earth.

$$\begin{cases} \dot{x} = v_x \\ \dot{y} = v_y \\ \dot{z} = v_z \\ \dot{v}_x = -\frac{\mu}{r_c^3} \left(x - 3 \frac{xx_c + yy_c + zz_c}{r_c^2} x_c \right) + f_x \\ \dot{v}_y = -\frac{\mu}{r_c^3} \left(y - 3 \frac{xx_c + yy_c + zz_c}{r_c^2} y_c \right) + f_y \\ \dot{v}_z = -\frac{\mu}{r_c^3} \left(z - 3 \frac{xx_c + yy_c + zz_c}{r_c^2} z_c \right) + f_z \end{cases} \quad (4)$$

Where μ is G-force constant, x , y , z and v_x , v_y , v_z are the location and speed coordinates of target spacecraft refer to initial one in inertial frame, x_c , y_c , z_c are the location coordinates of the initial spacecraft in inertial frame, $r_c = \sqrt{x_c^2 + y_c^2 + z_c^2}$ is the distance between initial craft and core of the earth, f_x , f_y , f_z are accelerates of disturbance and thrust.

3.2. Relative Navigation Measurement Model

Stereo vision measurement technique can be used in target and tracker relative location measurement, but light disturbing may cause stereo matching errors, which will reduce navigation precision. So the measurement of location information is added at where light disturbing is weaker.

Stereo vision measurement equation:

$$Z_{str} = AX(k) + v_{sr}(k)$$

Location measurement equation:

$$Z_{ang} = Ar_i + v_{ang}(k), \quad i = 1, 2$$

Where

$$Z_{ang} = \frac{1}{\sqrt{f_i^2 + \mathcal{X}_i^2 + \mathcal{Y}_i^2}} \begin{bmatrix} -\mathcal{X}_i \\ -\mathcal{Y}_i \\ f \end{bmatrix},$$

$$r_i = \frac{1}{\sqrt{(x-X_i)^2 + (y-Y_i)^2 + (z-Z_i)^2}} \begin{bmatrix} x-X_i \\ y-Y_i \\ z-Z_i \end{bmatrix}$$

x, y, z are coordinates of target in tracking spacecraft body frame, X_i, Y_i, Z_i are coordinates of camera in tracking spacecraft body frame, A is conversion matrix from tracking spacecraft body to inertial frame.

3.3. Two-Step Filter Relative Navigation Algorithm for Satellites Formation Flying

Due to maneuvering of the target spacecraft in formation and disturbance of complex space rays, matching of corresponding points may have an error of several pixels, which will accelerate rapidly with further distance. Considering that single image can provide more stable orientation measurement without big error, a two-step filter algorithm based on Kalman filter is developed: Firstly, get first step filter with orientation measurement and intermediate state estimation with Kalman filter algorithm; secondly, correct the intermediate state with the stereo vision measurement, and obtain the second step filter result. During the second filter, considering the error of the stereo vision measure system is in direct ratio with the square of distance, in order to improve the navigation precision of the filter algorithm, we utilize the relative state estimation to update the measurement noise square matrix, the arithmetic flow chart is shown in the Fig. 2:

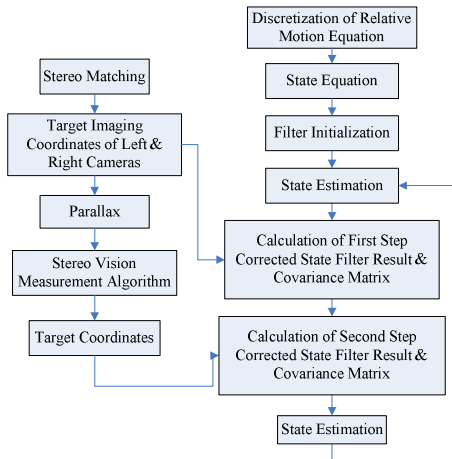


Fig 2. Relative navigation algorithm sequence chart

The algorithm in detail is as follows:

(1) Initialization of filter: providing the filter initial value $\hat{X}(0|0), P(0|0)$

(2) Deduce calculation: $k = 1, 2, \dots$

State estimation:

$$\hat{X}(k|k-1) = \Phi \hat{X}(k-1|k-1)$$

$$P(k|k-1) = \Phi P(k-1|k-1) \Phi^T + \Gamma Q(k-1) \Gamma^T$$

Stereo vision measurement estimation:

$$\hat{Z}_{stereo}(k|k-1) = H_s \hat{X}(k|k-1)$$

Orientation measurement estimation:

$$\hat{Z}_{ang}(k|k-1) = h_{ang}[\hat{X}(k|k-1), k]$$

(3) First-step correction of state using orientation measurement.

Calculating measuring error and covariance matrix:

$$\mathcal{E}_{ang}(k) = Z_{ang}(k) - \hat{Z}_{ang}(k|k-1)$$

$$S_{ang} = H_{ang} P(k|k-1) H_{ang}^T + R_{ang}$$

Calculating the filter gain:

$$K_{ang}(k) = P(k|k-1) H_{ang}^T(k) S_{ang}^{-1}(k)$$

Calculating the state filter value with first-step correction and the covariance matrix:

$$\bar{X}(k|k) = \hat{X}(k|k-1) + K_{ang}(k) \mathcal{E}_{ang}(k)$$

$$\bar{P}(k|k) = (I - K_{ang}(k) H_{ang}(k)) P(k|k-1)$$

(4) Second step correction of state with the stereo vision measurement.

Calculating measuring error and covariance matrix:

$$\mathcal{E}_{stereo}(k) = Z_{stereo}(k) - \hat{Z}_{stereo}(k|k-1)$$

$$S_{stereo} = H_{stereo} P(k|k-1) H_{stereo}^T + R_{stereo}$$

Calculating the filter gain:

$$K_{stereo}(k) = P(k|k-1) H_{stereo}^T(k) S_{stereo}^{-1}(k)$$

Calculating the state filter value and covariance matrix with the second step correction:

$$\hat{X}(k|k) = \bar{X}(k|k) + K_{stereo}(k) \mathcal{E}_{stereo}(k)$$

$$\bar{P}(k|k) = (I - K_{stereo}(k) H_{stereo}(k)) \bar{P}(k|k)$$

4. Numerical Simulation

Assume the matching error of two figures $\Delta\delta$ is zero average white-noise, the error variance is 0.5 pixels and each is $7.4 \mu\text{m}$, the focal distance of camera is $f = 8\text{cm}, 12.5\text{cm}$,

the baseline is combination of 0.5m and 1m, then the relationship of measurement error Δz and distance Z is shown as Fig.3.

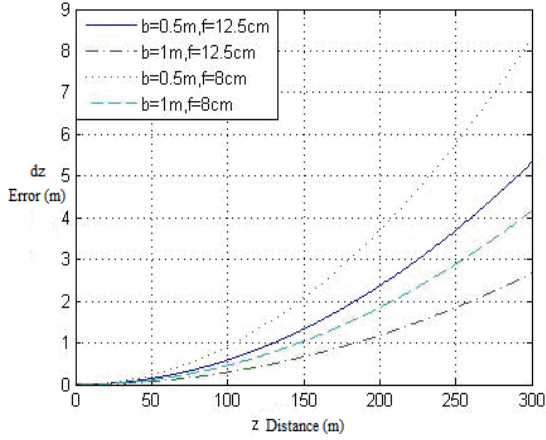
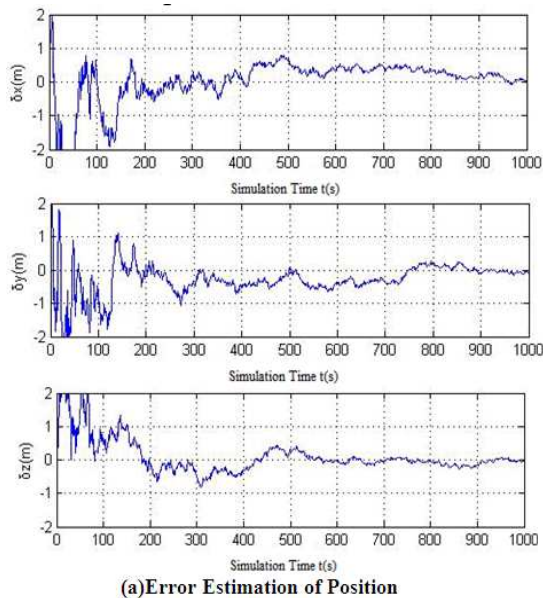


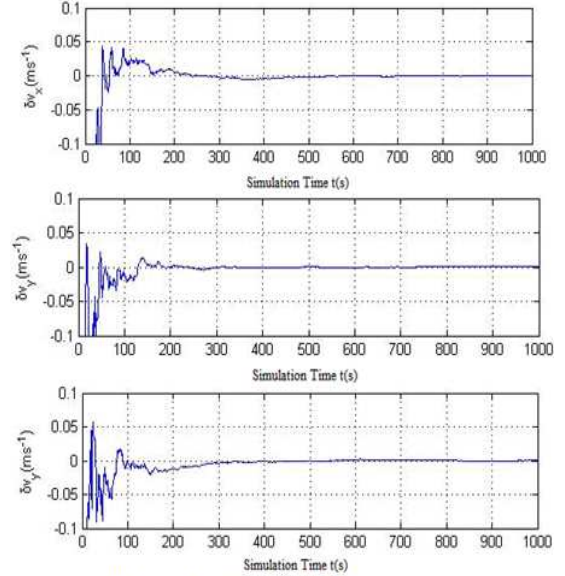
Fig 3. The relationship of the measure error and distance Z

According to Fig. 3, the error accelerates rapidly with further distance, which can be reduced by selecting proper focal distance and baseline. The baseline can not be too long considering the view field of camera.

Assume the initial orbital parameters of major spacecraft in formation flying are: semi-major axis of orbit 20182km, orbit eccentricity 0.001105, orbit inclination 50° , right ascension of ascending node 10.31° , argument of perigee 45.72° , mean anomaly 134.4° ; the initial orbital parameters of assistant spacecraft are: semi-major axis of orbit 20181.8km, orbit eccentricity 0.0011, orbit inclination 50.2° , right ascension of ascending node 10.315° , argument of perigee 45.713° , mean anomaly 134.3° . Now we just take disturbance of earth's take J_2 into account when we calculate the true relative position and velocity of two spacecrafts.



(a)Error Estimation of Position



(b)Error Estimation of Velocity

Fig 4. Relative state estimation

Discretizing the relative movement equation in inertial frame as the state equation of the system, the relative position and velocity estimation of two spacecrafts can be obtained by using Kalman filter.

Define that the estimations of relative position errors are Δx , Δy , Δz , the estimations of relative velocity errors are Δv_x , Δv_y , Δv_z . Based on the above simulation condition, the initial state errors of position and velocity are 7m and 0.2 m/s , and the simulation result of 1s sampling cycle is show as Fig. 4.

According to above figures, the initial filter error is bigger while the position error constringes to about 1m in 100s and the convergence of velocity error is rapidly. According to the process of entire simulation, relative position error is no more than 1% of real value which meet the demand of relative navigation parameter of formation flying. At the same time, the different initial simulation inputs are given, and there are same similar results. It shows that the algorithm has enough stability, can be used in spacecraft formation flying.

5. Conclusion

This paper researched the relative navigation algorithm based on the binocular stereo vision in the spacecraft formation flying mission. Measurement of relative state for the leader-follower spacecrafts in the formation flying is obtained by using the stereo vision, which simplifies the stereo vision measurement error model and updates the measurement error in real time. The relative motion equation in inertial frame is brought into the relative navigation system, avoiding the circular orbit assumption. According to numerical simulation, it shows that this algorithm has high precision, which can meet the requirements of the relative navigation in spacecraft formation flying.

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