Physical processes in the damping of electromechanical oscillations of the synchronous machine with magnitude-phase excitation controller

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To cite this article:

Oleg Agamalov. Physical Processes in the Damping of Electromechanical Oscillations of the Synchronous Machine with Magnitude-Phase Excitation Controller. *International Journal of Energy and Power Engineering*. Vol. 2, No. 4, 2013, pp. 164-171. doi: 10.11648/j.ijepe.20130204.14

Abstract: Physical processes the damping of the synchronous machine electromechanical oscillations without excitation control, with proportional automatic voltage regulator (AVR-P), and magnitude-phase excitation controller (MPH-EC), which is responsive to the deviations of the magnitude and phase of the terminal voltage phasor are considered. The advantages of the MPH-EC, compared with the above other structures excitation control are discussed. A calculation example of the small signal stability gain margin at active power of the synchronous machine with the above structures of the excitation controllers for the simplest model "single machine - infinite bus" is examined. From this example follows, that the variable small signal stability gain margin of the MPH-EC exceeds that parameter for AVR-P, and excitation control with power system stabilizer (AVR+PSS) with a some adjustable rotor angle deviation.

Keywords: Synchronous Generator, Terminal Voltage Phasor, Automatic Voltage Regulator, Small Signal Stability Gain Margin, Control by Plant Complex Output

1. Introduction

Currently, in theory and practice of the excitation control of the synchronous machines, the fundamental role played by the feedback on the terminal voltage magnitude [1, 2]. Excitation control is based on the calculation of the scalar mismatch error between the reference (set point) V_{ref} and the measured terminal voltage V_t . The obtained scalar error $\Delta V = V_{ref} - V_t$ is used as the input of a PID controller or it simplified variants (PI, PD) [1-3] for controlling the excitation current I_f of the synchronous machine. The purpose of this regulation is the precise maintaining the synchronous machine terminal voltage V_t according to the setpoint V_{ref} in all possible operating conditions. For this necessary to set the greatest possible value of the proportional gain of the automatic voltage regulator (AVR). However, as has been determined theoretically, and observed in practice [4], in some operating conditions of the synchronous machines this leads to a decrease of the damping component T_D of the electric moment, that is proportional to the rotor speed deviation $\Delta\omega$, and to the

electromechanical oscillations in the event of grid disturbances. Therefore, additionally in excitation control of the synchronous machines are used the feedbacks on the parameters that characterizing the rotor motion: frequency deviation Δf , rotor speed deviation $\Delta\omega$, field current deviation ΔI_f or accelerating power P_a . These additional feedbacks are implemented as stabilizing channels in the automatic excitation regulator of strong action AER-SA in Russia [2], or as separate devices - power system stabilizers (PSS). This greatly complicates the design, subsequent coordination of regulation and stabilization channels, holding of the commissioning works, and operation of the excitation control.

Therefore represents of interest the development of excitation control, which implements a new type of the complex feedback [5-8]. The structure of that feedback both reflects the electromagnetic state, determined by terminal voltage, and electromechanical state, defined by the rotor movement of the synchronous machine. For this necessary to increase the dimension of the mismatch error in such a way that it reflects the deviations of the terminal voltage and rotor angle of the synchronous machine. Corresponds to this requirement, as input of the excitation control, used the

terminal voltage phasor of the synchronous machine. Physical processes in the damping of electromechanical oscillations of the synchronous machine with magnitude-phase excitation controller (MPH-EC), using as input the terminal voltage phasor (complex output of the plant - the synchronous generator), are considered in this article with the following sections. The second section presents the main provisions, used in the MPH-EC development, and it is algorithm. The third section discusses the physical processes of electromechanical oscillations damping for the synchronous machine without excitation control, with proportional excitation controller AVR-P, and magnitude-phase excitation controller MPH-EC. A calculation example of the small signal stability gain margin at active power of the synchronous machine with the above structures of the excitation controllers for the simplest model "single machine - infinite bus" is given in the fourth section. As can be seen from the above example, MPH-EC have the variable small signal stability gain margin at active power, that exceeds the value of that parameter for AER-SA or AVR+PSS with a some adjustable rotor angle deviation. Conclusion summarizes the content of this article, and defines the future directions of the work at MPH-EC.

2. Main Provisions and MPH-EC Algorithm

We define the set point of the excitation controller as phasor $\bar{V}_{ref}$ (p. u.), which coincides in the steady-state with the field current I_f (p. u.) or synchronous e.m.f. phasor $\bar{E}_q$ (p. u.). The magnitudes of the set point and terminal voltage phasors are equal $|\bar{V}_{ref}| = |\bar{V}_{t0}|$, (p. u.), but shifted by the steady-state rotor angle δ_{SM0} . Thus, it may be determined the normal complex argument error function NCAEF [5-8] of the excitation control for the steady state of the synchronous machine with the terminal voltage $\bar{V}_{t0} = V_{q0} + jV_{d0}$, and the CAEF increment in the transient, in accordance with the vector diagram, Fig. 1:

Figure 1. Vector diagram of synchronous machine, showing the CAEF increment $\Delta\bar{e}$ by the terminal voltage phasor $\bar{V}_t$.

$$\begin{aligned}\bar{e}_{N0} &= f(\bar{V}_{ref}, \bar{V}_{t0}) = \\ \bar{V}_{ref} - \bar{V}_{t0} &= V_{ref} - (V_{t0} \cos \delta_{SM0} + jV_{t0} \sin \delta_{SM0}) = \\ &= (V_{ref} - V_{q0}) - jV_{d0} = e_{qN} + je_{dN}\end{aligned}\quad (1)$$

where:

$$\begin{aligned}e_{qN} &= V_{ref} - V_{t0} \cos \delta_{SM0} = V_{ref} - V_{q0}, \\ e_{dN} &= -V_{t0} \sin \delta_{SM0} = -V_{d0}.\end{aligned}$$

NCAEF by terminal voltage phasor (1) characterized by the equation $|\bar{V}_{ref}| = |\bar{V}_{t0}|$, (p. u.), and defines the steady state of the inertial element - the rotor of the synchronous machine with the terminal voltage phasor angle $\delta_{SM0} = const$.

In case of violation the steady-state of the synchronous machine, as a result of a disturbance in the power system, and the corresponding terminal voltage phasor $\bar{V}_{t1}$, the transient CAEF $\bar{e}_1 \neq \bar{e}_{N0}$:

$$\begin{aligned}\bar{e}_1 &= f(\bar{V}_{ref}, \bar{V}_{t1}) = \\ &= \bar{V}_{ref} - \bar{V}_{t1} = V_{ref} - (V_{t1} \cos \delta_{SM1} + jV_{t1} \sin \delta_{SM1}) = \\ &= (V_{ref} - V_{q1}) - jV_{d1} = e_q + je_d\end{aligned}\quad (2)$$

which leads to CAEF increment $\Delta\bar{e}$:

$$\begin{aligned}\Delta\bar{e} &= f(\Delta V_t, \Delta\delta_{SM}) = \bar{e}_{N0} - \bar{e}_1 = \\ &= (V_{t1} \cos \delta_{SM1} - V_{t0} \cos \delta_{SM0}) + \\ &+ j(V_{t1} \sin \delta_{SM1} - V_{t0} \sin \delta_{SM0}) = \\ &= (V_{q1} - V_{q0}) + j(V_{d1} - V_{d0})\end{aligned}\quad (3)$$

The CAEF increment $\Delta\bar{e}$ (3), taking into account $|\bar{V}_{t0}| = |\bar{V}_{ref}|$, reflects the increments of the terminal voltage magnitude ΔV_t and rotor angles $\Delta\delta_{SM}$, and generalizes the traditional definition of the error by magnitude terminal voltage, that used in the existing excitation control:

$$\begin{aligned}\Delta\bar{e} &= |\bar{V}_{t0} - \bar{V}_{t1}| = \sqrt{V_{ref}^2 + V_{t1}^2 - 2V_{ref}V_{t1} \cos(\Delta\delta_{SM})} = \\ &= \sqrt{(V_{q1} - V_{q0})^2 + (V_{d1} - V_{d0})^2}, \\ \Delta V_t &= V_{ref} - V_{t1} = V_{t0} - V_{t1} = \sqrt{V_{q0}^2 + V_{d0}^2} - \sqrt{V_{q1}^2 + V_{d1}^2}\end{aligned}\quad (4)$$

For excitation control of the synchronous machine the CAEF increment should be regarded as a real function of a complex argument - the terminal voltage phasor that changes in transient:

$$\frac{d(\Delta\bar{e})}{dt} = \frac{\partial(\Delta\bar{e}(\bar{V}_t))}{\partial \bar{V}_t} \frac{d\bar{V}_t}{dt}\quad (5)$$

where $\frac{\partial(\Delta\bar{e}(\bar{V}_t))}{\partial \bar{V}_t}$ - the gradient of the CAEF increment by

the terminal voltage phasor, $\frac{d\bar{V}_t}{dt} = \dot{\bar{V}}_t$ - a derivative of the terminal voltage phasor. Given the vector diagram, Fig. 1, we define the terminal voltage phasor and CAEF increment in transient, in coordinate system $S-Q$ (for the initial steady state):

$$\begin{aligned}
 |\bar{V}_{t0}| &= |\bar{V}_{ref}| \\
 \bar{V}_{t1} &= V_{ts} + jV_{tq} = V_{t1} \cos(\Delta\delta_{SM}) + jV_{t1} \sin(\Delta\delta_{SM}) = \\
 &= V_{t0} e^{j(\Delta\delta_{SM})}, \\
 \tilde{V}_{t1} &= V_{ts} - jV_{tq} = V_{t0} \cos(\Delta\delta_{SM}) - jV_{t0} \sin(\Delta\delta_{SM}) = \\
 &= V_{t0} e^{j(-\Delta\delta_{SM})}, \\
 V_{ts} &= V_{t1} \cos(\Delta\delta_{SM}), V_{tq} = V_{t1} \sin(\Delta\delta_{SM}), \\
 \Delta\bar{V}_t &= \Delta V_{ts} + j(\Delta V_{tq}) = \\
 &= V_{t1} \cos(\Delta\delta_{SM}) - V_{t0} + jV_{t1} \sin(\Delta\delta_{SM}) = \\
 &= V_{t1} \cos(\Delta\delta_{SM}) - V_{ref} + jV_{t1} \sin(\Delta\delta_{SM}), \\
 \Delta\tilde{V}_t &= \Delta V_{ts} - j(\Delta V_{tq}) = \\
 &= V_{t1} \cos(\Delta\delta_{SM}) - V_{t0} - jV_{t1} \sin(\Delta\delta_{SM}) = \\
 &= V_{t1} \cos(\Delta\delta_{SM}) - V_{ref} - jV_{t1} \sin(\Delta\delta_{SM}), \\
 \Delta V_{ts} &= V_{t1} \cos(\Delta\delta_{SM}) - V_{t0} = \\
 &= V_{t1} \cos(\Delta\delta_{SM}) - V_{ref}, \Delta V_{tq} = V_{t1} \sin(\Delta\delta_{SM}), \\
 \Delta\bar{e} &= -\Delta\bar{V}_t = -(\Delta V_{ts} + j(\Delta V_{tq})) = \\
 &= -(V_{t1} \cos(\Delta\delta_{SM}) - V_{t0} + jV_{t1} \sin(\Delta\delta_{SM})) = \\
 &= -(V_{t1} \cos(\Delta\delta_{SM}) - V_{ref} + jV_{t1} \sin(\Delta\delta_{SM})) = \\
 &= V_{ref} - V_{t1} \cos(\Delta\delta_{SM}) - jV_{t1} \sin(\Delta\delta_{SM}) = \\
 &= \Delta e_s + j(\Delta e_q), \\
 \Delta e_s &= V_{ref} - V_{t1} \cos(\Delta\delta_{SM}), \Delta e_q = -V_{t1} \sin(\Delta\delta_{SM}).
 \end{aligned} \tag{6}$$

Non-constant real-valued function of a complex variable(s) is non-analytic, and therefore not differentiable in the accepted sense (Cauchy-Riemann condition). The calculation of the CAEF increment based on the Wirtinger partial derivatives [5-8]. Oriented an output of excitation control in the direction of the antigradient (5) we obtain the following algorithm for MPH-EC:

$$\begin{aligned}
 u &= K \left(V_{ref} - \frac{2 \cos(N\Delta\delta_{SM})}{1 + \cos(2N\Delta\delta_{SM})} V_t \right) = \\
 &= K (V_{ref} - V_t \sec(N\Delta\delta_{SM}))
 \end{aligned} \tag{7}$$

where K - gain of the proportional channel by the magnitude deviation of the terminal voltage phasor $|\Delta V_t|$, and N - gain by rotor angle deviation $\Delta\delta_{SM}$. A more detailed derivation of the magnitude-phase control algorithm is given in [5-9].

3. Physical Processes in the Damping of Electromechanical Oscillations of the Synchronous Machine with Different Structures of the Excitation Control

3.1. Non-Regulated Synchronous Machine

As it is known, that for non-regulated synchronous machine, the main factor that mitigated it electromechanical oscillations is their damping or asynchronous moment. So, in transient the full electric power of the synchronous machine is given as [1, 10]:

$$\begin{aligned}
 P_e &= P_{eS} + P_{eD} = \\
 &= \frac{E'_q V_b}{x'_\Sigma} \sin \delta - \frac{V_b^2 (x_\Sigma - x'_\Sigma)}{2x_\Sigma x'_\Sigma} \sin 2\delta + K_D \frac{d(\Delta\delta)}{dt}
 \end{aligned} \tag{8}$$

where: P_e, P_{eS}, P_{eD} - electric power, and it synchronous and damping components, E'_q - transient synchronous e.m.f., V_b - bus voltage, x'_Σ - total transient inductance, δ - rotor angle, x_Σ - total tie inductance, K_D - damper gain. On the assumption, that the turbine power is constant $P_t = const$, the rotor angle deviation is determined based on the 2nd Newton's law as:

$$\begin{aligned}
 T_j \frac{d^2(\Delta\delta)}{dt^2} &= P_t - P_e = P_t - (P_{eS} + P_{eD}) = \\
 P_t - \left(\frac{E'_q V_b}{x'_\Sigma} \sin \delta - \frac{V_b^2 (x_\Sigma - x'_\Sigma)}{2x_\Sigma x'_\Sigma} \sin 2\delta + K_D \frac{d(\Delta\delta)}{dt} \right) &= 0
 \end{aligned} \tag{9}$$

where T_j - the mechanical inertia constant of the unit. Then:

$$\begin{aligned}
 T_j \frac{d^2(\Delta\delta)}{dt^2} + K_D \frac{d(\Delta\delta)}{dt} + \\
 + \left(\frac{E'_q V_b}{x'_\Sigma} \cos \delta_0 - \frac{V_b^2 (x_\Sigma - x'_\Sigma)}{x_\Sigma x'_\Sigma} \cos 2\delta_0 \right) \cdot \Delta\delta &= 0
 \end{aligned} \tag{10}$$

with the characteristic equation:

$$\begin{aligned}
 T_j p^2 + K_D p + \\
 + \left(\frac{E'_q V_b}{x'_\Sigma} \cos \delta_0 - \frac{V_b^2 (x_\Sigma - x'_\Sigma)}{x_\Sigma x'_\Sigma} \cos 2\delta_0 \right) &= 0
 \end{aligned} \tag{11}$$

and it roots:

$$p_{1,2} = \frac{-K_D \pm \sqrt{K_D^2 - 4T_j \left(\frac{E'_q V_b}{x'_\Sigma} \cos \delta_0 - \frac{V_b^2 (x_\Sigma - x'_\Sigma)}{x_\Sigma x'_\Sigma} \cos 2\delta_0 \right)}}{2T_j} \tag{12}$$

that defines the rotor motion. After reaching the some deviation $\Delta\delta$, arising due to the acceleration power $\Delta P = P_e - P_t$, the rotor angle deviation begins to decrease,

i.e. $d(\Delta\delta)/dt < 0$. Therefore on the section A_1A_2 of the angular characteristic $P_{eD} < 0$, and the acceleration power will decline more rapidly than under the action only the synchronizing component P_{es} , Fig. 2 [10]:

Figure 2. Damping of the electromechanical oscillation for non-regulated synchronous machine.

Braking power imbalance reduces the kinetic energy of the rotor on the section A_1A_2 . With use the areas method, the decrease of the kinetic energy is determined as proportional to the area $A_1A_2a_1$. At the point A_2 , where $P_e = P_t$, due to the reduction of the rotor kinetic energy on the section A_1A_2 , the rotor speed is $\omega_{A_2} < \omega_0$. Therefore, further the rotor angle decreasing relative to the initial value as $\Delta\delta'$. At the section $A_2A_3A_4$ we have $P_e < P_t$, and the rotor begins to accelerate. In the point A_4 the rotor speed $\omega_{A_4} = \omega_0$ that leads to the subsequent rise of the rotor angle, as shown in Fig. 2. So, as indicated in [10], the dynamic angular characteristic of the synchronous machine in transient at section A_1A_4 is below than for it static angular characteristics due to the damping torque $P_{eD} = K_D(d(-\Delta\delta)/dt)$. Accordingly, when the rotor angle returns to the initial value δ_0 , the electric power is $P_e < P_t$ by the value P_{eD} . This leads to an earlier acceleration of the rotor in the point A_2 , and equalization of it kinetic energy deviations during oscillations (i.e. the equality of the acceleration and deceleration areas) already at the smaller value the rotor angle deviation $\Delta\delta' < \Delta\delta$. As a result of the subsequent oscillations $\Delta\delta \rightarrow 0$ in the synchronous machine with the damper windings.

3.2. Synchronous Machine with AVR-P

Next, consider the physical process of the electromechanical oscillations in the regulated synchronous machine with the proportional AVR (AVR-P). It is known [1, 2, 10], the positive effect of the proportional excitation control of the synchronous machine consists in the increasing the synchronizing component of the electrical power due to the increase of their synchronous e.m.f. $E_q \approx I_f$ at transients. At the same time, as noted in references [1, 2, 10] the fast-acting proportional excitation control due to the great feedback gain $K_{0V} > 50$ in accordance with the law:

$$V_f = V_{f0} + K_{0V}(V_{ref} - V_t) \quad (13)$$

can lead to the oscillatory instability of a synchronous machine, Fig. 3:

Figure 3. Damping of the electromechanical oscillation for synchronous machine with AVR-P.

After first swing $\Delta\delta$, the rotor angle return to the steady state value δ_0 on the section A_1A_2 . AVR-P reacting to the terminal voltage drop, increases the field current $I_f \sim E_q$. Herewith, the acceleration power is $\Delta P = P_e - P_t \neq 0$ (point A_2). Power equality will be achieved at the point A_3 , and the equality of the acceleration and deceleration areas at the point A_4 . As a result of this delay and powers disparities for the rotor angle δ_0 in point A_2 , the rotor angle deviation at point A_4 will be greater than the initial deviation $\Delta\delta' > \Delta\delta$. Due to the rotor angle deviation $\Delta\delta'$, and the corresponding it the terminal voltage increases, AVR-P will

reduce the field current $I_f < I_{f0}$. Therefore, the subsequent increase in the rotor angle to the initial steady-state value $\delta = \delta_0$ corresponds to larger accelerating power at point A_5 . The powers equality $P_e = P_t$ will be achieved only at a point A_6 . Therefore, the acceleration area will be equalized at the larger rotor angle deviation $\Delta\delta'' > \Delta\delta' > \Delta\delta$ at point A_7 . As a result, the moving point of the angular characteristics $P_e = f(\delta)$ describes the unwinding spiral, which determines the unstable oscillatory mode of the synchronous machine. The resulting damping moment depends on the initial operation mode and parameters of the synchronous machine and grid. With small initial steady state rotor angle δ_0 , the synchronization component $\partial P_e / \partial \delta$ of the electrical power is significant, which leads to higher values of the rotor speed deviation (slip) at the electromechanical oscillations, and thus a large positive damping component of the electrical power. With a large initial steady state rotor angle δ_0 , the synchronization component $\partial P_e / \partial \delta$ of the electrical power is negligible, so the amplitude of the electro-mechanical oscillations is small, and therefore is small the positive damping component of the electric power, i.e. the probability of the oscillatory instability is higher. To suppress the oscillatory instability currently used the structure of the excitation control with AVR and power system stabilizer (PSS) in which additionally implemented feedbacks by parameters of the synchronous machine electromechanical state (rotor speed, frequency, accelerating power). Additional feedbacks are needed for biasing the phase lag between the field current $I_f(t)$ (e.m.f. $E_q(t)$) and the rotor angle $\delta(t)$ for positive damping moment of the excitation control, i.e. so that with a decrease in the rotor angle to $\delta(t) = \delta_0$ at the first swing of the electromechanical oscillations is provided the condition $P_e < P_t$.

3.3. Synchronous Machine with MPH-EC

For the qualitative analysis we neglect the moment at damping windings of synchronous machine, which is always positive $P_{ed} > 0$, and assume that the field current I_f is determined only by the excitation control, i.e. the voltage, applied to the field winding V_f . The excitation control law with MPH-EC is:

$$\begin{aligned} V_f &= V_{f0} + K_\Sigma \left(V_{ref} - \frac{2 \cos(N\Delta\delta)}{1 + \cos(2N\Delta\delta)} V_t \right) = \\ &= V_{f0} + K_\Sigma (V_{ref} - V_t \sec(N\Delta\delta)) \end{aligned} \quad (14)$$

In accordance with (14), the measured terminal voltage deviation ΔV_t of synchronous machine additionally corrected as a function of the rotor angle deviation $\sec(N\Delta\delta_{SM})$, where N - the gain by $\Delta\delta$. At the same setpoint $\Delta V_{ref} = 0$ equation (14) in the increments is:

$$\Delta V_f = K_\Sigma \frac{2 \cos(N\Delta\delta)}{1 + \cos(2N\Delta\delta)} \Delta V_t = K_\Sigma \sec(N\Delta\delta) \Delta V_t \quad (15)$$

and it is possible to determine the feedback gain of the excitation control by the terminal voltage phasor as follows:

$$K_F = K_\Sigma \frac{2 \cos(N\Delta\delta)}{1 + \cos(2N\Delta\delta)} = K_\Sigma \sec(N\Delta\delta) \quad (16)$$

The magnitude and sign of the gain K_F depends on the argument $(N\Delta\delta)$. If:

$$(N\Delta\delta) > \pi/2 \Rightarrow \Delta\delta_L > \pi/2N \quad (17)$$

then changes the sign of K_F , according to the function graph $\sec(N\Delta\delta_{SM})$, Fig. 4:

Figure 3. Graph of the function $2 \cos(N\Delta\delta) / (1 + \cos(2N\Delta\delta)) = \sec(N\Delta\delta)$.

Equations (15, 16) with inequality (18) are defines a significant positive impact of MPH-EC on the synchronizing component of the electrical power due to non-linear increase of the synchronous e.m.f.

$\Delta E_q \approx \Delta I_f \approx \Delta V_f = K_\Sigma \sec(N\Delta\delta) \Delta V_t$ in transients at $\Delta\delta < \Delta\delta_L$. It should be noted the "concavity" of characteristics, shown in Fig. 4. That corresponds to a

slight increase of the gain K_F at a small rotor angle deviation (for example, with a planned increase in the synchronous machine power), and its intense increase at significant rotor angle deviation up to $\Delta\delta_L$.

Now consider the impact of the MPH-EC on the synchronous machine stability, Fig. 5:

Figure 4. Damping of the electromechanical oscillations for synchronous machine with MPH-EC.

Suppose, that as a result of the disturbance in the power system, the rotor angle deviation occurs $\Delta\delta \rightarrow \Delta\delta_L$, where the value $\Delta\delta_L = 18^\circ$ el. on the Fig. 5, defined for $N=5$. The excitation control equations (14, 15) are determining an increase of the static angular characteristics in 1.05 times for section A_0A_1 according to a predetermined value $N=5$. At $\Delta\delta_L = 18^\circ$ el., in accordance with (16, 17), the sign of the gain K_F changes. This leads to the de-excitation of the synchronous machine, and the transition to point A_2 . Arisen braking power imbalance leads to a reduction of the rotor kinetic energy on the section A_2A_3 with a simultaneous increase of the e.m.f. $\Delta E_q \approx \Delta I_f \approx \Delta V_f = K_\Sigma \Delta V_t$, as a result of the terminal voltage deviation relative to the setpoint, and decreasing of the rotor angle deviation $\Delta\delta < \Delta\delta_L$. The equality of acceleration and deceleration areas will be achieved at a point A_3 at a smaller deviation $\Delta\delta'$. With further increase in the rotor angle $\Delta\delta''$ on the section A_3A_4 under the accelerating power imbalance, for point A_4 corresponds to less braking power imbalance due to the previous de-excitation action of MPH-EC, depending on the rotor angle deviation $\Delta\delta'$, i.e. $\Delta\delta'' < \Delta\delta' < \Delta\delta$. Thus, MPH-EC provides such phase relation between the

deviations of e.m.f. E'_q (field current ΔI_f), and the rotor angle $\Delta\delta$ of the synchronous machine, that would as the rotor angle move towards to the initial value "from above" $\delta_+ \rightarrow \delta_0$, the electric power of the synchronous machine was less than the corresponding turbine power $P_{ei} < P_{ti}$ for the angle $\delta_0 < \delta_i < \delta_+$. Conversely, with an increase the rotor angle to the initial value "from bottom" $\delta_- \rightarrow \delta_0$, the electrical power of the synchronous machine is greater $P_{ej} > P_{tj}$ for rotor angle $\delta_- < \delta_j < \delta_0$. As a result, on the angular characteristics $P_e = f(\delta)$ the moving point describes a convergent curve that defines the decaying oscillation mode of the synchronous machine.

4. The Calculation of the Small Signal Stability Gain Margin at Active Power of the Synchronous Machine with Different Structures of the Excitation Control

Consider the impact of different excitation control structures on small signal stability gain margin at active power for the model "single machine – infinite bus" with the parameters in p. u.: $x_d = 1.9$; $x_T = 0.1$; $x_L = 0.17$; $U_{10} = 1.0$; $P_{10} = 0.85$; $Q_{10} = 0.264$; $x'_d = 0.38$.

4.1. For non-regulated synchronous machine the transmission power limit is determined thru e.m.f.:

$$\begin{aligned} \dot{E}_{q0} &= \dot{U}_{10} + \frac{Q_{10}(x_d + x_T)}{U_{10}} + j \frac{P_{10}(x_d + x_T)}{U_{10}} = \\ &= 1.528 + j1.7 = 2.286e^{j48.05^\circ} \end{aligned}$$

Busbar voltage the receiving system:

$$\begin{aligned} \dot{U}_0 &= U_{10} - \frac{Q_{10} \cdot x_o}{U_{10}} - j \frac{P_{10} \cdot x_o}{U_{10}} = \\ &= 0.955 - j0.145 = 0.966e^{-j8.633^\circ} \end{aligned}$$

Full rotor angle of the synchronous machine: $\delta_0 = 48.05^\circ + 8.633^\circ = 56.683^\circ$. The angular power characteristic:

$$P_0 = \frac{2.286 \cdot 0.966}{2.0 + 0.17} \sin 56.683^\circ = 0.85$$

which coincides with a predetermined active power of a synchronous machine. The transmission power limit at $\delta_0 = 90^\circ$:

$$P_L = \frac{E_{q0} U_0}{x_d \Sigma} = \frac{2.286 \cdot 0.966}{2.17} = 1.018.$$

Thus, the small signal stability gain margin of the unregulated synchronous machine:

$$K_{SM} = \frac{1.018 - 0.85}{0.85} \cdot 100\% = 19.77\%. \quad (18)$$

4. 2. For excitation control with AVR-P the transmission power limit is determined at constant transient e.m.f. $E'_q = \text{const}$ [1, 2], where:

$$E'_q = U_{10} + \frac{Q_{10}(x'_d + x_T)}{U_{10}} + j \frac{P_{10}(x'_d + x_T)}{U_{10}} = 1.127 + j0.408 = 1.2e^{j19.9^\circ}$$

The full rotor angle is: $\delta'_0 = 19.9 + 8.635 = 28.533^\circ$. In the steady state:

$$P_0 = \frac{E'_0 U_0}{x_{d\Sigma}} \sin \delta'_0 = \frac{1.2 \cdot 0.966}{0.38 + 0.1 + 0.17} \sin 28.533^\circ = 0.85$$

The transmission power limit:

$$P'_L = \frac{E'_0 U_0}{x'_{d\Sigma}} = \frac{1.2 \cdot 0.966}{0.65} = 1.783$$

which corresponds to a small signal stability gain margin:

$$K_{AVR-P} = \frac{1.783 - 0.85}{0.85} \cdot 100\% = 109.7\%. \quad (19)$$

4. 3. For excitation control with AVR+PSS, at the highest possible gain by terminal voltage deviation, we can define the small signal stability limit by taking $U_{SM} = \text{const}$ [1, 2]:

$$U_{SM} = U_{10} + \frac{Q_{10} x_T}{U_{10}} + j \frac{P_{10} x_T}{U_{10}} = 1.026 + j0.085 = 1.029e^{j4.736^\circ}$$

The full rotor angle in this case

$$\delta_{U_{SM}} = 4.736^\circ + 8.633^\circ = 13.369^\circ$$

In the steady state:

$$P_0 = \frac{U_{SM} U_0}{x_T + x_o} \sin \delta_{U_{SM}} = \frac{1.029 \cdot 0.966}{0.1 + 0.17} \sin 13.369^\circ = 0.85$$

The transmission power limit:

$$P''_L = \frac{U_{SM} U_0}{x_T + x_L} = \frac{1.029 \cdot 0.966}{0.27} = 3.68$$

which corresponds to a small signal stability gain margin:

$$K_{AVR+PSS} = \frac{3.68 - 0.85}{0.85} \cdot 100\% = 333\%. \quad (20)$$

4. 4 For excitation control with MPH-EC (14, 15) the transmission power limit we define, based on the dependence of the gain K_F , and therefore, the transient e.m.f. as a function of the rotor angle deviation

$E'_q = f(\sec(N\Delta\delta))$. Then, for different variations of the rotor angle, and the previously defined system parameters, we can calculate the variable transmission power limit as:

$$P'_{MF} = \frac{E'_0 U_0}{x'_{d\Sigma}} \sec(N\Delta\delta) = \frac{1.2 \cdot 0.966}{0.65} \sec(N\Delta\delta) = 1.783 \sec(N\Delta\delta)$$

and variable small signal stability gain margin:

$$K_{MF} = \frac{1.783 \sec(N\Delta\delta) - 0.85}{0.85} \cdot 100\% \quad (21)$$

The obtained values of the variable small signal stability gain margin by the active power for a considered example with $N = 5$ shown in the table 1:

Table 1. The values of the variable small signal stability gain margin by the active power for synchronous machine with MPH-EC.

$\Delta\delta,^\circ \text{ el}$	2	4	6	8	10	12	14	16
$K_{MF},\%$	113	123	142	174	226	319	513	1107

Comparing the results of the calculations, we see that an excitation control with AVR-P, compared with the case of the unregulated synchronous machine, increases the small signal stability gain margin by 90 %, and an excitation control with AVR+PSS by 223 %. Excitation control with MPH-EC is characterized by variable small signal stability gain margin by the active power that intensity increases with rotor angle deviations, and for $\Delta\delta > 14^\circ \text{ el}$. is greater than for AVR+PSS. Increased of the transmission power limit, and small signal stability gain margin is caused by that AVR+PSS wholly or AVR-P partly eliminates the influence of synchronous machine impedance on it. MPH-EC, as previously discussed in section 3, in the transient creates the effect of the negative differential resistance of the synchronous machine, reducing the voltage drop across with an increasing the stator current (power), and the rotor angle deviation. Thus achieving a variable small signal stability gain margin, exceeding the value for AVR+PSS with some adjustable value $\Delta\delta_{SM}$.

5. Conclusions

Algorithm and physical processes of damping the electromechanical oscillations of the synchronous machine for an excitation control with MPH-EC with complex input signal: the terminal voltage phasor, are considered. Parameters of given signal are used for regulating the terminal voltage magnitude, and for damping of electromechanical oscillations of the synchronous machine. That improves the transient and small-signal stability, minimizes the influence of the electromagnetic noise, improves reliability, and reduces the operating cost of excitation control as a result of the minimum set of the input signals, that are used (only phasors of the setpoint and terminal voltage).

In order to determine the effectiveness of the proposed excitation control system structure in practice is necessary to examine its robust properties, by setting the structured and unstructured uncertainties in the models of the excitation system of the synchronous generator, and the power grid, which is the next step of the work.

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