Study of Higgs Phenomenology in the Next-to-Minimal Supersymmetric Standard Model (NMSSM)

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Abstract: The theoretical and phenomenological aspects of the Next-to-Minimal Supersymmetric Standard Model (NMSSM) is reviewed. The model includes an additional gauge singlet S which generates the μ - term dynamically and the μ - problem in MSSM is solved. The different masses of seven Higgs bosons and the bounds of the mass parameters have been discussed.

Keywords: NMSSM, MSSM, Gauge Singlet S , μ - Problem, Mass Parameters

1. Introduction

Supersymmetry[1,2] is one of the most appealing concepts of Physics beyond the Standard Model(SM). The main motivation of Supersymmetry is to stabilize the hierarchy[3] between the electroweak and the GUT or Plank scale. In the Standard Model (SM), the Higgs boson mass gains radiative corrections which depend quadratically on the cut-off scale of the theory, threatening to generate a mass which is far too large to explain electroweak symmetry breaking. The supersymmetry ensures that the contribution of new supersymmetric particles exactly cancel the quadratic divergence of their Standard Model partners, removing the sensitivity of the Higgs mass to the cut off scale in a natural way. In this way Supersymmetry stabilizes the Higgs mass at a phenomenologically acceptable scale (below TeV). The MSSM contains a μ - parameter in the superpotential where μ is a dimensionful parameter. It enters the Higgs potential with the soft scalar masses to determine the vacuum expectation value of the Higgs fields. This parameter has to be adjusted by hand to a value at the electroweak scale, in order to provide the correct pattern of electroweak symmetry breaking. This is a problem of the model and is called μ -problem[4]. In the NMSSM[5,6,7] an additional gauge singlet S (the complex scalar component of a chiral superfield $\hat{S}$) is introduced which generates the μ -term dynamically, i.e. an effective μ -term arises spontaneously and the adjustment by hand drops out. The effective μ -parameter may then naturally be expected to be

of the electroweak scale, $\mu = \lambda \langle S \rangle$. In this sense the NMSSM is a natural extension of the MSSM.

The superpotential for the NMSSM is given by

$$W_{NMSSM} = W_{YUK} + \lambda S H_u H_d + \frac{k}{3} S^3 \quad (1)$$

Where W_{YUK} gives the Yukawa couplings for the Standard Model fermions. Without the k term the superpotential would have a $U(1)'$ symmetry, so called Peccei-Quinn symmetry[8]. This additional symmetry would alter the phenomenology completely. The role of the k term is to break this $U(1)'$ symmetry. The k term is introduced trilinear such that k is dimensionless. However, there remains a discrete Z_3 symmetry[9,10] which is moreover broken spontaneously. In principal this leads to the domain wall problem. Introducing additional, but suppressed terms, the Z_3 symmetry can be broken without changing phenomenology at the electroweak scale. It is assumed that the domain wall problem is circumvented in this way without any modifications except far beyond the electroweak scale. Thus NMSSM provides a lot of new phenomenological aspects which is absent in SM [11] and MSSM[12].

However, the Higgs bosons in MSSM and NMSSM are given in the table below

Table 1. Higgs bosons in MSSM and NMSSM.

Model	Symmetry	Superpotential	CP-even	CP-odd	Charged
MSSM	-	$\mu H_u H_d$	H_1^0, H_2^0	A^0	$H^\pm$
NMSSM	Z_3	$\lambda S H_u H_d + \frac{k}{3} S^3$	H_1^0, H_2^0, H_3^0	A_1^0, A_2^0	$H^\pm$

The paper is organized as follows: Section 2 gives the expressions of the Higgs potential in NMSSM. Tadpole conditions are discussed in section 3. The expressions of the masses of Higgs scalars in NMSSM is given in section 4. In section 5 various parameter constraints have been discussed. The conclusions are given in section 6.

2. The Higgs Potential in NMSSM

The Higgs fields of the NMSSM consists of the usual two Higgs doublets as in the MSSM together with an extra Higgs singlet,

$$H_u = \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix}, H_d = \begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix}, S \quad (2)$$

$$V_{Soft} = m_{H_u}^2 |H_u|^2 + m_{H_d}^2 |H_d|^2 + m_S^2 |S|^2 + [\lambda A_\lambda S H_u H_d + \frac{1}{3} k A_k S^3 + h.c.] \quad (6)$$

where g and g' being the gauge couplings of $SU(2)_L$ and $U(1)$ interactions respectively. The Higgs potential contains seven parameters: λ and k from the superpotential and $A_k, A_\lambda, m_{H_u}, m_{H_d}$ and m_s from the soft supersymmetry breaking terms.

3. Tadpole Conditions

Let us expand the potential about the VEVs represented by v_u, v_d, v_s and the phases θ and φ . The parameterization of the scalar fields is as follows:

$$H_d = \begin{pmatrix} \frac{1}{\sqrt{2}}(v_d + h_d + i a_d) \\ H_d^- \end{pmatrix}, H_u = e^{i\theta} \begin{pmatrix} H_u^+ \\ \frac{1}{\sqrt{2}}(v_u + h_u + i a_u) \end{pmatrix}, S = \frac{1}{\sqrt{2}} e^{i\varphi} (v_s + h_s + i a_s) \quad (7)$$

Where we have taken the vacuum-expectation values v_u, v_d, v_s to be real and non-negative. The values v_u, v_d and v_s will take the values for which the potential V in equation(3) has a global minimum. In the parameterization (7) the vacuum denoted by $\langle \rangle$ precisely means

$$\langle H_d \rangle = \begin{pmatrix} \frac{v_d}{\sqrt{2}} \\ 0 \end{pmatrix}, \langle H_u \rangle = e^{i\theta} \begin{pmatrix} 0 \\ \frac{v_u}{\sqrt{2}} \end{pmatrix}, \langle S \rangle = e^{i\varphi} \frac{v_s}{\sqrt{2}} \quad (8)$$

The condition for the scalar potential to have an extremum at the vacuum is that the first derivatives with respect to the Higgs fields evaluated at the vacuum vanishes

$$0 = \frac{1}{v_d} \langle \frac{\partial V}{\partial h_d} \rangle = m_{H_d}^2 - R_\lambda \frac{v_u v_s}{v_d} + \frac{g^2 + g'^2}{8} (v_d^2 - v_u^2) + \frac{|\lambda|^2}{2} (v_u^2 + v_s^2) - \frac{R}{2} \frac{v_u v_s^2}{v_d} \quad (9)$$

$$0 = \frac{1}{v_u} \langle \frac{\partial V}{\partial h_u} \rangle = m_{H_u}^2 - R_\lambda \frac{v_d v_s}{v_u} + \frac{g^2 + g'^2}{8} (v_d^2 - v_u^2) + \frac{|\lambda|^2}{2} (v_d^2 + v_s^2) - \frac{R}{2} \frac{v_d v_s^2}{v_u} \quad (10)$$

$$0 = \frac{1}{v_s} \langle \frac{\partial V}{\partial h_s} \rangle = m_s^2 - R_\lambda \frac{v_d v_u}{v_s} + R_k v_s + \frac{|\lambda|^2}{2} (v_d^2 + v_u^2) + |k|^2 v_s^2 - R v_d v_u \quad (11)$$

$$0 = \frac{1}{v_u} \langle \frac{\partial V}{\partial a_d} \rangle = \frac{1}{v_d} \langle \frac{\partial V}{\partial a_u} \rangle = I_\lambda v_s - \frac{1}{2} I v_s^2 \quad (12)$$

$$0 = \frac{1}{v_s} \langle \frac{\partial V}{\partial a_s} \rangle = I_\lambda \frac{v_d v_u}{v_s} + I_k v_s + I v_d v_u \quad (13)$$

The extra singlet is allowed to couple only to the Higgs doublets of the model, and consequently the couplings of the new fields to gauge bosons will only be manifested via their mixing with the other Higgs fields.

The tree-level Higgs potential[10] is composed of three parts,

$$V = V_F + V_D + V_{Soft} \quad (3)$$

With,

$$V_F = |\lambda S|^2 (|H_u|^2 + |H_d|^2) + |\lambda H_u H_d + k S^2|^2 \quad (4)$$

$$V_D = \frac{g^2 + g'^2}{8} (|H_d|^2 - |H_u|^2)^2 + \frac{1}{2} g^2 |H_u^+ H_d|^2 \quad (5)$$

Where the introduced abbreviations are

$$R = \text{Re} [\lambda k^* e^{i(\theta-2\varphi)}] \quad (14)$$

$$I = \text{Im} [\lambda k^* e^{i(\theta-2\varphi)}] \quad (15)$$

$$R_\lambda = \frac{1}{\sqrt{2}} \text{Re}[\lambda A_\lambda e^{i(\theta+\varphi)}] \quad (16)$$

$$I_\lambda = \frac{1}{\sqrt{2}} \text{Im}[\lambda A_\lambda e^{i(\theta+\varphi)}] \quad (17)$$

$$R_k = \frac{1}{\sqrt{2}} \text{Re}[k A_k e^{i3\varphi}] \quad (18)$$

$$I_k = \frac{1}{\sqrt{2}} \text{Im}[k A_k e^{i(\theta+\varphi)}] \quad (19)$$

These conditions are called tadpole conditions in the sense that the conditions make the tadpole diagrams vanish if we set the Higgs fields to their VEVs. Here R and I are dimensionless parameters and $R_\lambda, R_k, I_\lambda$ and I_k have the dimension of mass.

From eqⁿ (12) and (13), the following two conditions are obtained-

$$\left. \begin{aligned} I_\lambda &= -\frac{1}{2} I v_s \\ I_k &= -\frac{3}{2} I \frac{v_d v_u}{v_s} \end{aligned} \right\} \quad (20)$$

$$M_{H_{2,1}}^2 = \frac{1}{2} \left\{ M_Z^2 + \frac{1}{2} k v_s (4k v_s + \sqrt{2} A_k) \pm \sqrt{\left[M_Z^2 - \frac{1}{2} k v_s (4k v_s + \sqrt{2} A_k) \right]^2 + \cot^2 \beta_s [2\lambda^2 v_s^2 - M_A^2 \sin^2 2\beta]^2} \right\} \quad (25)$$

Where $v = \sqrt{v_u^2 + v_d^2} = 246 \text{ GeV}$, $\tan \beta = \frac{v_u}{v_d}$, $\tan \beta_s = \frac{v_s}{v}$ and negative value for A_k being preferred.

It can be noted that the heavy CP-odd Higgs boson A_2 is degenerate with the heaviest CP-even Higgs boson H_3 .

Moreover,

$$M_{H_1}^2 + M_{H_2}^2 = M_Z^2 + \frac{1}{2} k v_s (4k v_s + \sqrt{2} A_k) \quad (26)$$

The sum of the two lightest scalars, is independent of the

$$m_{H_d}^2 = \frac{(g^2 + g'^2)}{8} (v_u^2 - v_d^2) - \frac{1}{2} \lambda^2 v_u^2 + \frac{1}{2} (\sqrt{2} A_\lambda + k v_s) \lambda v_s \frac{v_u}{v_d} - \frac{1}{2} \lambda^2 v_s^2 \quad (27)$$

$$m_{H_u}^2 = \frac{(g^2 + g'^2)}{8} (v_d^2 - v_u^2) - \frac{1}{2} \lambda^2 v_d^2 + \frac{1}{2} (\sqrt{2} A_\lambda + k v_s) \lambda v_s \frac{v_d}{v_u} - \frac{1}{2} \lambda^2 v_s^2 \quad (28)$$

$$m_s^2 = -k^2 v_s^2 - \frac{1}{2} \lambda^2 v^2 + k \lambda v_u v_d + \frac{1}{\sqrt{2}} \lambda A_\lambda \frac{v_u v_d}{v_s} - \frac{1}{\sqrt{2}} k A_k v_s \quad (29)$$

The renormalization group equations for λ , k and top Yukawa coupling h_t are related to the gauge couplings and are given by

$$16\pi^2 \frac{dg_i^2}{dt} = b_i g_i^2 \quad (30)$$

$$16\pi^2 \frac{dh_t^2}{dt} = h_t^2 \left[\lambda^2 + 6h_t^2 - \frac{16}{3} g_3^2 - 3g_2^2 - \frac{13}{15} g_1^2 \right] \quad (31)$$

$$16\pi^2 \frac{d\lambda^2}{dt} = \lambda^2 \left[4\lambda^2 + 2k^2 + 3h_t^2 - 3g_2^2 - \frac{3}{5} g_1^2 \right] \quad (32)$$

$$16\pi^2 \frac{dk^2}{dt} = 6k^2 [\lambda^2 + k^2] \quad (33)$$

Here, $b_1 = \frac{33}{5}$, $b_2 = 1$, $g_1 = \sqrt{\frac{5}{3}} g'$, $g_2 = g$ and $t = \log \frac{Q^2}{M_{GUT}^2}$ where Q is the renormalization scale.

Only one of the three imaginary parts I, I_λ, I_k is physical, when complex parameters are introduced, they must be chosen to satisfy the tadpole conditions (20).

4. The Mass of Higgs Scalars

In the NMSSM seven Higgs bosons are created: 3 CP-even (H_1^0, H_2^0, H_3^0), two CP-odd (A_1^0, A_2^0) and two charged ($H^\pm$). Their tree level masses are given below [10]

$$M_{H^\pm}^2 = M_A^2 + M_W^2 - \frac{1}{2} (\lambda v)^2 \quad (21)$$

$$M_{A_2}^2 = M_A^2 \left(1 + \frac{1}{4} \cot^2 \beta_s \sin^2 2\beta \right) \quad (22)$$

$$M_{A_1}^2 = -\frac{3}{\sqrt{2}} k v_s A_k \quad (23)$$

$$M_{H_3}^2 = M_A^2 \left(1 + \frac{1}{4} \cot^2 \beta_s \sin^2 2\beta \right) \quad (24)$$

coupling λ and M_A^2 .

5. Parameter Constraints

There are seven parameters in the Higgs potential- λ and k from the superpotential and $A_\lambda, A_k, m_{H_d}, m_{H_u}, m_s$ from the soft supersymmetry breaking terms. The field values at v_u, v_d and v_s are given by the following equations [10]

Values of λ and k in the perturbative regime at the GUT scale is given by $\frac{\lambda}{2\pi} \leq 1, \frac{k}{2\pi} \leq 1$. But λ and k are reduced to small values at the electroweak scale and their combined approximate bound is given by [10]

$$\lambda^2 + k^2 \leq 0.5 \quad (34)$$

λ must not become too small. If λ becomes too small then the phenomenological constraints on μ require v_s to be large and the link with the other Higgs VEVs is lost. A small value of $\tan \beta$ is favoured and it is kept $t \leq 10$. v_s is expected to vary from $3v$ to $15v$.

The value of A_k is determined from the requirement of vacuum stability. Positive and large value of A_k destabilizes the vacuum and the mass squared of the lightest pseudoscalar becomes negative. The soft SUSY breaking term containing A_k is a cubic coupling proportional to S^3 , so the effect of varying

A_k is only communicated through the singlet contribution of the Higgs fields. The heavy Higgs bosons and one of the lighter scalars are very insensitive to the choice of A_k .

A_λ is also constrained by vacuum stability and its natural value is approximately $\mu \tan\beta$.

6. Conclusions

The present paper investigates the Higgs sector of the Next-to-Minimal Supersymmetric Standard Model. In this model the μ problem of MSSM is solved by introducing a new singlet Higgs field S . The expressions of the Higgs boson masses have been introduced and it provides a nice insight into the mass hierarchies. The present paper also throws light into the tadpole condition. The MSSM limit can be regained by letting λ and $k \rightarrow 0$ while keeping μ, A_λ and A_k fixed. The bounds of the mass parameters have been discussed. The requirement of vacuum stability provides useful bounds on the mass parameters. The lightest Higgs boson in the NMSSM is heavier than the one of the MSSM due to additional terms in the tree level Higgs potential proportional to λ^2 ; the additional contribution is $\Delta m_h^2 = \frac{\lambda^2}{g^2} M_z^2 \sin^2 2\beta$. It is obvious that the upper bound on the mass of the lightest Higgs boson is expected to be larger than that in the MSSM.

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