
Two Different Loading Directions to Determine the Shear and Longitudinal Modulus of Elasticity

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Abstract: The large-scale abundance of wood in Brazil combined with the advantages of its use stimulate many studies to be encouraged in order to make use of this raw material in a more optimized and adequate form. Compared with concrete and steel, wood presents an excellent relation between mechanical strength and its mass, beauty, low energy consumption for its processing, good thermal insulation and easy workability. Objectifying the best use of wood, this work proposes that the equivalence between longitudinal and transversal modulus of elasticity values with radial (E_{LR} ; G_{LT}) and tangential load application (E_{LT} ; G_{LR}) in the 3 and 4-point bending tests used for their determinations. The test of equivalence used in the analysis of the results for the modulus of elasticity was the Tukey's test, by which the statistical equivalence between values of longitudinal ($E_{LR} \times E_{LT}$) and transversal ($G_{LT} \times G_{LR}$) modulus of elasticity with the radial and tangential load application, respectively. It was concluded that for the species of the hardwood group: Peroba Rosa (*Aspidosperma polyneuron*) with 35 specimens, Eucalyptus Tereticornis (*Eucalyptus tereticornis*) with 33 specimens, Jatobá (*Hymenaea courbaril*) with 28 specimens and Canafistula Peltophorum dubium) with 12 test specimens, tested in this work, there was no significant influence of the direction change of the loads on the values of the calculated modulus of elasticity.

Keywords: Equivalence Test, Hardwoods, Radial Load, Tangential Load, Different Directions

1. Introduction

Wood was always one of the materials of civil construction most used by the human being. The physical and mechanical characteristics and relative abundance of this material enable its application for uses from interior finishes to large structures such as pavilions, roofs and bridges. Wood presents environmental advantages when compared to other building materials (cement, concrete, steel and aluminum), because it is recyclable, renewable, biodegradable and requires low energy needs for its processing [1-4].

In relation to other materials such as concrete, plastic, steel and aluminum, wood has a number of advantages, such as beauty, high mechanical resistance to mass, low energy consumption for its processing, good thermal insulation, easy workability [5].

Getting to know the importance of wood, it is important to carry out studies on obtaining its physical and mechanical characteristics. In the last case, wood can be used even as a fuel substituting the diminishing fossil energy carriers. [6]

Regarding the mechanical characteristics, we have the elasticity modulus that measures the stiffness of the specimens, however, it is necessary to carry out tests with the maximum of accuracy, as an example of this, the definition of the direction of application of the load in the test.

Among the mechanical properties of materials used in the design of a structure, highlights the modulus of elasticity (MOE), enabling the setting to provide displaced and deformations in structural components subjected to the action of the imposed loads (limit state) [7-9].

In Brazil, the design of wood structures is regulated by ABNT NBR 7190 (1997) (Wood Structure Project) [10], where it can be inferred that is possible to obtain the modulus

of elasticity of wood through the 3-point bending test, which can be found in its Annex B as well as the measurements of the specimens used and the test procedure. In this test a specific direction of application of the load is not stipulated, this load can be either in the radial or tangential longitudinal direction.

The Brazilian standard imposes that the deformations (arrows) in the bending test should be a maximum of $L/200$, (L being the length between supports), so that the piece of wood tested does not extrapolate the elastic regime for the plastic.

Icimoto et al. [8], performed tests varying the direction of load application (sides A, B, C and D) on test specimens tested by 3 point bending, as prescribed by the Brazilian standard, for 6 specimens for each species of *Corymbia Citriodora* (hardwood) and *Pinus Elliottii* (conifer), and each test specimen was tested 4 times. The results were compared by analysis of variance and it was found that for these species the position of the load application did not significantly change the values of longitudinal modulus of elasticity, but with an observation that this analysis can not be extended to other species, since wood is an orthotropic material.

Lahr et al. [11] tested some species of the hardwood group: Cedrinho (*Erismia uncinatum*), Peroba Rosa (*Aspidosperma polyneuron*), Eucalyptus Tereticornis (*Eucalyptus tereticornis*), Canafistula (*Cassia ferruginea*), Jatobá (*Hymenaea stilbocarpa*). The 3- and 4-point bending tests were performed with tangential and radial load application to determine the longitudinal and transversal modulus of 20 specimens per species. The results were compared using the Anderson-Darling test, which showed equivalence between the longitudinal and transversal moduli of elasticity $E_{LT} \times E_{LR}$ and $G_{LR} \times G_{LT}$, respectively.

Icimoto et al. [12], seven different species of the hardwood group were studied: Cambará Rosa (*Erismia sp.*), Eucalyptus Grandis (*Eucalyptus Grandis*), Cupiúba (*Goupia Glabra*), Eucalyptus Citriodora (*Corymbia Citriodora*), Ipe (*Tabeluia sp.*), Jatobá (*Hymenaea stilbocarpa*), Angico Rosa (*Anadenanthera falcata*) and one of the group of Conifers: *Pinus Elliottii* (*Pinus Elliottii*). Eight specimens were tested for each species, each specimen was tested 4 times, being a total of 4 different sides of the load application, so that all the faces of the specimen were tested. The results were tested by the least square methods and it was verified non-equivalence between the longitudinal modulus of elasticity with loads applied in different directions for the species studied.

Stolf et al. [13] performed a test to determine the longitudinal modulus of elasticity in three different positions (tangential, radial and radial farther from the core) in the equipment developed by Siqueira (1986), based on the FPL type machine (developed by the forest products laboratory-USA) using a modified Charpy pendulum. The principle of operation is characterized by kinetic energy provided by a pendulum via flexible current with a support at its end. The rupture of the tested piece is obtained by a simple movement of the pendulum. The calculations for stiffness determination were performed according to [14] ASTM D143-52 (ASTM 1981) for each species studied in the

hardwood group: Angelim Saia (*Parkia pendula*) with 13 pieces, *Eucalyptus grandis* with 32 pieces, *Corymbia Citriodora* with 20 pieces and conifers: *Pinus Elliottii* with 35 pieces. The results were tested by Kruskal-Wallis non-parametric hardness analysis, and it was demonstrated that there was no significant change in the values with the load direction variation applied in the test.

2. Material and Methods

Three-point and four-point flexural tests were carried out to determine the values of the longitudinal modulus of elasticity with load application in the radial (E_{LR}), tangential longitudinal (E_{LT}) and transversal elastic modulus with load application in the tests in the radial (G_{LT}) and tangential (G_{LR}) longitudinal directions, remembering that E_{LR} is referring to G_{LT} and E_{LT} referring to G_{LR} , since G is always orthogonal to E .

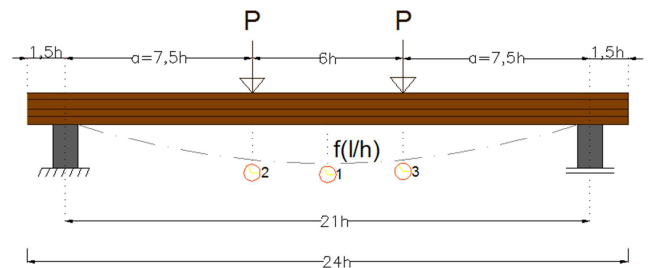
The 3-point bending test performed is prescribed by ABNT NBR 7190 (Wood Structures Design) in Annex B, which shows the dimensions of the specimen as well as the test procedure, and the 4-point bending test according to [15] ASTM D 198-15 (Standard Test Method of Static Tests of Lumber in Structural Sizes) in an adapted manner, since the test pieces were not in structural size.

The species studied were: Peroba Rosa (*Aspidosperma polyneuron*) with 35 specimens, Eucalyptus Tereticornis (*Eucalyptus tereticornis*) with 33 specimens, Jatobá (*Hymenaea courbaril*) with 28 specimens and the Canafistula (*Peltophorum dubium*) with 12 specimens.

The values of E_{LR} , E_{LT} , G_{LT} and G_{LR} were taken into account for the species of the studied hardwood group. These results were compared by means of statistical analysis to prove the equivalence between E_{LR} with E_{LT} and G_{LT} with G_{LR} .

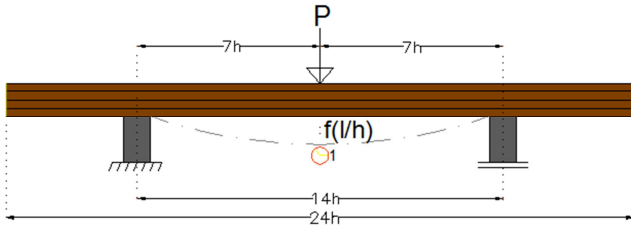
All tests were carried out on the Laboratory of Wood and Wood Structures (*Laboratório de Madeira e de Estruturas de Madeira-LaMEM*), at the São Carlos Engineering School (EESC), University of São Paulo (USP).

Initially, the four-point bending test was performed, based on ASTM D 198-15 (Standard Test Method of Static Tests of Lumber in Structural Sizes) for determination of modulus of elasticity in bending (E), expressed by equation 1. The arrow always limited to $L/200$ so that it does not exceed the limit of proportionality required in the Brazilian standard.



Source: author's collection.

Figure 1. Representation of the 4-point bending test with its respective comparator clocks.



Source: author's collection.

Figure 2. Representation of the 3-point bending test with its respective comparator clock.

The arrows were measured by comparator clocks located only in the middle of the span (point 1 for 3-point bending test) and besides the middle of the span at the two points of load application (points 2 and 3 for 4-point bending test), P is the value of the applied loads, a is the distance from the load to the nearest support, L the length of the gap between supports ($21h$ in the 4-point bending test and $14h$ in the 3-point test), can be seen in Figures 1 and 2.

The procedures for the two different tests performed to obtain E and G , which are the 4-point bending and the 3-point bending tests are described ahead.

2.1. Four-point Bending Test

The test specimens tested in 4-point bending followed the scheme of figure 1. According to the equation of the elastic line for this situation (equation 1), the appropriate formulations were used for the arrow at each required point.

$$v(x) = \frac{P \cdot a}{6 \cdot E \cdot I} (3 \cdot L \cdot x - 3 \cdot x^2 - a^2) \quad (1)$$

In equation 1, $v(x)$ is the arrow value at a given position, x is the position of the arrow analyzed, P is the value of the applied loads, a is the distance from the load to the nearest support, L the length of the span between supports, E the longitudinal modulus of elasticity and I is the moment of inertia.

It can be seen that in the central region between the loads, pure bending is generated when this type of test is performed, the total arrow in the center (point 1) was found according to equation 2.

$$v(1) = \frac{4117,5 \cdot P}{E \cdot b} \quad (2)$$

Where P is the value of the applied loads, E the longitudinal modulus of elasticity found in the 4-point bending test and b is the value of the cross-section base of the specimen.

Equation 3 represents the calculation of the arrow at load application points 2 and 3.

$$v(2) = v(3) = \frac{3826,25 \cdot P}{E \cdot b} \quad (3)$$

Where, $v(2)$ and $v(3)$ are the arrows in positions 2 and 3 respectively, P is the value of the applied loads, E the longitudinal modulus of elasticity and b the value of the cross-sectional base of the specimen.

Getting to know the value of the total arrow in the middle of the span, the average between the two arrows at load application points 2 and 3 was subtracted from the total arrow, resulting in equation 4, which represents the relative arrow caused only by the flexion in the middle of the span [$v(1rel)$].

$$v(1rel) = \frac{281,25 \cdot P}{E \cdot b} \quad (4)$$

Which, $v(1rel)$ is the arrow in position 1 relating only to flexure, P is the value of the applied loads, E the longitudinal modulus of elasticity and b the value of the cross-sectional base of the specimen.

By isolating the only unknown value (E) from equation 4, we obtain equation 5. With this consideration the real E is found for any specimen.

$$E = \frac{281,25 \cdot P}{v(1rel) \cdot b} \quad (5)$$

2.2. Three-Point Bending Test

After the 4-point bending test, another test is performed, this time the simple 3-point bending test for the determination of G , which is shown in figure 2 presented before.

The 3-point bending test was performed as prescribed by ABNT NBR 7190 (1997) in its appendix B (determination of the properties for the structural design), but with a span between supports of $14h$, in order to have the arrow with shear influence, allowing G to be found, since the real E has already been determined.

The Virtual Force Method (MFV) is used on the structural model of static bending at three points, aiming to find the expression for the calculation of the displacement below, the point of application of the force (equation 6), considering, therefore, the portion of the bending and shear stresses.

$$v(1) = \frac{P \cdot L^3}{48 \cdot E \cdot I} + \frac{3 \cdot P \cdot L}{10 \cdot G \cdot A} \quad (6)$$

Which, $v(1)$ is the arrow in the middle of the span, P is the applied point force, E is the longitudinal modulus of elasticity or Young's modulus, I is the moment of inertia of the cross section, G is the transversal modulus of elasticity, A is the cross-sectional area, L the useful length of the beam (distance between supports), b is the measurement of the base and h the height of the cross section respectively and A the value of the area.

Since the real E value has already been determined in the 4-point bending test, and that $L = 14h$, the only unknown value to be determined is G , thus turning into equation 7.

$$G = \frac{126 \cdot P \cdot h \cdot E \cdot I}{A(30 \cdot E \cdot I \cdot v(1) - 1715 \cdot P \cdot h^2)} \quad (7)$$

3. Results and Discussion

Tables 1 and 2 show the mean values for the longitudinal

and transverse elastic tests with radial (E_{LR} e G_{LT}) and tangential (E_{LT} and G_{LR}) load, respectively. The equivalence between the values of the elastic moduli by the Tukey's test is confirmed by a value marked with the same letter in the level of 5% of reliability. In these tables the coefficient of variation (C. V.) can be seen for each group of test specimens tested.

Table 1. Equivalence analysis Through the Tukey's test for the results of E_{LT} and E_{LR} , with tangential and radial load application respectively in the tests.

E_{LT} e E_{LR}-Unity (MPa)				
Medium Values	E_{LT}	C. V.	E_{LR}	C. V.
P. Rosa	10651 A	0,225	10870 A	0,153
E. Tereticornis	15610 A	0,146	15453 A	0,146
Jatobá	21237 A	0,283	21282 A	0,266
Canafistula	14788 A	0,160	14801 A	0,160

Table 2. Equivalence analysis Through the Tukey's test for the results of G_{LT} e G_{LR} , with radial and tangential load application respectively in the tests.

G_{LR} e G_{LT}-Unity (MPa)				
Medium Values	G_{LR}	C. V.	G_{LT}	C. V.
P. Rosa	243 A	0,225	238 A	0,203
E. Tereticornis	473 A	0,239	487 A	0,172
Jatobá	534 A	0,213	514 A	0,194
Canafistula	423 A	0,138	423 A	0,157

The results of Table 1 for the values of longitudinal modulus of elasticity with tangential and radial load application indicate through the Tukey equivalence test that for all species tested there were equivalence for their respective modules (E_{LR} x E_{LT}), thus indicating that there is no need to perform the test with a load in a specific direction. This conclusion can be extended to Table 2, which for the transversal modulus of elasticity with radial and transverse loading, the values of the modulus were equivalent for all species tested (G_{LT} x G_{LR}), thus reaffirming there is no need for the application of the load in the bending test in an specific direction

Tables 1 and 2 diverge from the one presented by the study [12], where the change of direction of the load was preponderant for the tests, calling attention to the Jatobá species that in the present paper obtained equivalence between the different modulus with the change of load direction.

In the work [7, 11, 13], it was concluded that the change of direction of the load in the test to obtain the longitudinal modulus of elasticity did not influence to a significant change, thus being in agreement with the results verified in this present work.

4. Conclusions

The results of this study permit us to conclude:

1. According to Tables 1 and 2, which statistical analysis was used by Tukey's method, the load application position in the bending tests does not interfere in the results of the transversal and longitudinal elastic modulus of elasticity for the wood of the hardwood group tested, as well E_{LR} x E_{LT} and G_{LT} x G_{LR} being equivalent to each other.
2. Based on the results, it's important to state that the

bending test can be procedure in any direction to the grain, which facilitates the execution of the test.

3. The present work suggests that more studies should be carried out in the objectifying to have greater certainty about the non-influence of the direction of the load in the tests to obtain the longitudinal and transverse modulus of elasticity, since for the same species (Jatobá) there were divergent values in the literature.

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