

Econometric Analysis of Local Government Investment Efficiency and the Debt Risk Based on the DSGE Model

Zhi-qi Zhu¹, Ke Gao², Tao Wang², Nan Bai³

¹Tianjin University of Finance and Economics, Tianjin, P. R. China

²Central University of Finance and Economics, Beijing, P. R. China

³Renmin University of China, Beijing, P. R. China

Email address:

zhuzhiqi12345@163.com (Zhi-qi Zhu), gkfly@126.com (Ke Gao), manutdwangtao@126.com (Tao Wang), 99536157@qq.com (Nan Bai)

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Abstract: This paper examines the relationship between the efficiency of government investment and the debt risk from a theoretical perspective. By building a DSGE model, we introduced the impact of government financial investment, and investigated the change of debt risk under different government investment efficiency. From the model, we observed a obvious reverse effect between the government investment efficiency and debt risk. Finally, according to research conclusions, we put forward some Suggestions.

Keywords: DSGE Model, Local Government Debt, Government Investment Efficiency, Government Debt Risk

1. Introduction

In response to the impact of the economic crisis in 2008, the Chinese government launched an emergency 4 trillion investment plan and with the loose monetary policy. The central government had supported local government to increase investment and financing platform to issue bonds. This investment-driven way would smooth economic fluctuations. These measures made our country's economy was the first to stabilize and rise. Also, these measures made up the short board of the infrastructure construction in our country. However, with the stabilization of China's economy, the policy had also caused two more serious problems. First, the local government could not directly borrow. By establishing financing platforms and other means of curve financing, local government obtained higher cost of funds, while leaving a large number of debt outside the budget supervision. Second, there was a partial pursuit of local government GDP growth phenomenon. There were a large number of low returns, low positive externalities of investment. It is also worth noting that there are some interaction mechanisms between these two problems.

In 2015, the Ministry of Finance estimated that Chinese government's debt ratio rose to 41.5%, lower than the

standard 60% (the Treaty of Maastricht). With the fiscal policy becoming the mainstay of steady growth, the budget deficit rate increased from 2.2% to 3% in 2016. Therefore, it is necessary to clarify the relationship between government investment efficiency and debt risk. In this paper, we hope to establish the DSGE model to analyze the mechanism of government expenditure efficiency and the debt risk.

2. DSGE Model and Analysis

This paper constructs a closed DSGE model, which includes households, firms, central bank, and the financial sector. Assuming that families are free to choose consumption, labor supply and government bond holdings to achieve intertemporal maximization. Manufacturers are intermediate goods manufacturers and final product manufacturers, their goals are to pursue cost minimization and profit maximization. Intermediate goods manufacturers are in a monopolistic competitive market, and the final products are in a completely competitive market. The interest rate rule is formulated by the central bank, and the financial rules are formulated by the government.

A. Households

The utility function of the representative household is:

$$E_t \sum_{k=0}^{\infty} \beta^k [ln(\tilde{C}_{o,t+k} - h\tilde{C}_{o,t+k-1}^*) - \chi \frac{N_{o,t+k}^{1+\eta}}{1+\eta}]$$

Here h is the consumption habit, χ is the weight parameter of labor supply, \tilde{C}_t is composed of public goods and private goods consisting a group of consumer bundle, The equation is as follows:

$$\tilde{C}_t = (\kappa_c^{\frac{1}{v}} C_{o,t}^{\frac{v-1}{v}} + (1 - \kappa_c)^{\frac{1}{v}} C_{G,t}^{\frac{v-1}{v}})^{\frac{v}{v-1}}$$

Here κ_c is the proportion of private goods consumption, v is the substitution elasticity between public goods consumption and private goods consumption. Budget constraint conditions:

$$(1 + \tau_t^c)C_{t,o} + I_{t,o} + \frac{B_{o,t}}{P_t} = (1 - \tau_t^n) \frac{W_{o,t}}{P_t} N_{o,t} + [(1 - \tau_t^k)r_t^k u_t + \tau_t^k \delta(u_t)] K_{o,t-1} + R_{t-1} \frac{B_{o,t-1}}{P_t} + TR_{o,t} + DIV_{o,t}$$

Household income comes from after-tax wages, after-tax capital gains, after-tax bond income, transfer payments and corporate dividends. Households spend mainly on consumption, investing and buying government bonds. Where u_t is the capital utilization, δ is the depreciation, τ is the tax rate. The form of the capital accumulation equation is as follows:

$$K_{o,t} = (1 - \delta(u_t))K_{o,t-1} + [1 - S_t(\frac{I_{o,t}}{I_{o,t-1}})]I_{o,t}$$

According to Christiano (2005) settings, we assume that the form of investment adjustment costs are as follows:

$$S_t = \frac{\kappa_i}{2} [\frac{I_{o,t}}{I_{o,t-1}} - 1]^2$$

According to Leeper (2010), we set the depreciation form as follows:

$$\delta(u_t) = \delta_0 + \delta_1(u_t - 1) + \frac{\delta_2}{2}(u_t - 1)^2$$

By maximizing the utility function, the First Order Condition (FOC) of the variable can be obtained:

$$\lambda_{o,t} = (\tilde{C}_t - h\tilde{C}_{t-1}^*)^{-1} \frac{\kappa_c^{\frac{1}{v}}}{1 + \tau_t^c} (\frac{\tilde{C}_{o,t}}{C_{o,t}})^{\frac{1}{v}}$$

$$\lambda_{o,t} = E_t \frac{\beta \lambda_{o,t+1} R_t}{\pi_{t+1}}$$

$$q_t = E_t \frac{\lambda_{o,t+1}}{\lambda_{o,t}} \beta [(1 - \tau_{t+1}^k)r_{t+1}^k u_{t+1} + \tau_{t+1}^k \delta(u_{t+1}) + q_{t+1}(1 - \delta(u_{t+1}))]$$

$$1 = q_t(1 - S_t - \frac{\partial S_t}{\partial I_{o,t}} I_{o,t}) - E_t \beta \frac{\lambda_{o,t+1}}{\lambda_{o,t}} q_{t+1} \frac{\partial S_{t+1}}{\partial I_{o,t}} I_{o,t+1}$$

$$q_t \delta'(u_t) = (1 - \tau_t^k)r_t^k + \tau_t^k \delta'(u_t)$$

Here μ_t , $\lambda_{o,t}$ are Lagrangian multipliers, $q_t = \mu_t / \lambda_t$ is

Tobin's q value, π_t is t period inflation index.

B. Sticky Salary Setting

Drawing on Erceg et al. (2000), we assume that each household is a monopoly provider of different labor. $N_{i,t}$ is providing labor. And $i \in [0, 1]$. The aggregate form of heterogeneous labor is as follows:

$$N_t = (\int_0^1 N_{i,t}^{\frac{\theta_w-1}{\theta_w}} di)^{\frac{\theta_w}{\theta_w-1}}$$

Here θ_w is the alternative elasticity of the different labor force. The demand function of the individual labor force is obtained by maximizing profit:

$$N_{i,t} = (\frac{W_{i,t}}{W_t})^{-\theta_w} N_t$$

Bring zero profit to condition, and obtained:

$$W_t = (\int_0^1 W_{i,t}^{1-\theta_w} di)^{\frac{1}{1-\theta_w}}$$

We introduce the Calvo (1983) method to achieve the sticky wage setting. Suppose that each period has a fixed probability $1 - W_w$ that the family can change the wage. In order to maximize the expected utility, the family develops the optimal form of sticky wage as follows:

$$MAX \sum_{k=0}^{\infty} (\beta W_w)^k [-\chi \frac{N_{o,t+k}^{1+\eta}}{1+\eta} + \lambda_{t+k}(1 - \tau_{t+k}^n) \frac{W_{o,t}}{P_{t+k}} N_{o,t+k}]$$

Solve the real optimal sticky wage:

$$w_{o,t}^* = \frac{\theta_w}{\theta_w - 1} \frac{\tilde{H}_{1t}}{\tilde{H}_{2t}}$$

$$\tilde{H}_{1t} = \chi \frac{w_t^{\theta_w(1+\eta)}}{(w_{o,t}^*)^{\theta_w(1+\eta)}} N_t^{1+\eta} + W_w \beta E_t (\pi_{t+1})^{\theta_w(1+\eta)} \tilde{H}_{1t+1}$$

$$\tilde{H}_{2t} = \lambda_t (1 - \tau_t^n) \frac{w_t^{\theta_w}}{(w_{o,t}^*)^{\theta_w}} N_t + W_w \beta E_t (\pi_{t+1})^{\theta_w-1} \tilde{H}_{2t+1}$$

According to the formula (14), we write the real wage as an exponential form:

$$w_t^{(1-\theta_w)} = (1 - W_w)(w_{o,t}^*)^{(1-\theta_w)} + W_w (w_{t-1})^{1-\theta_w} \pi_t^{\theta_w-1}$$

C. Final Product Manufacturers

We set the production function of the final goods manufacturer as Dixit-Stiglitz function.

$$Y_t = (\int_0^1 Y_{j,t}^{\frac{\theta_p-1}{\theta_p}} dj)^{\frac{\theta_p}{\theta_p-1}}$$

Here θ_p is the alternative elasticity of the different intermediates, $Y_{j,t}$ is the intermediate product, and $j \in [0, 1]$.

Through the manufacturer profit maximization and zero profit, we can obtain the demand for intermediate goods and price function.

$$Y_{j,t} = \left(\frac{P_{j,t}}{P_t}\right)^{-\theta_p} Y_t P_t = \left(\int_0^1 P_{j,t}^{1-\theta_p} dj\right)^{\frac{1}{1-\theta_p}}$$

D. Intermediate Goods Manufacturers

We set the intermediate goods manufacturer's production function as C-D function.

$$Y_{j,t} = Z_t K_{G,t-1}^{\kappa_G} (u_t K_{j,t-1})^\alpha N_{j,t}^{1-\alpha}$$

Here $K_{G,t-1}$ is the public capital stock, κ_G is the output elasticity of public capital. $j \in [0, 1]$. Z_t is total factor productivity. We set it to the AR (1) procedure:

$$\log(Z_t) = \rho_z \log(Z_{t-1}) + \sigma_z \epsilon_t^z$$

Intermediate goods manufacturers pursue cost minimization.

$$MIN : W_t^p N_{j,t} + R_t^{kp} \bar{K}_{j,t}$$

$$S.T : Z_t K_{G,t-1}^{\kappa_G} (\bar{K}_{j,t}^\alpha) N_{j,t}^{1-\alpha} \geq \left(\frac{P_{j,t}}{P_t}\right)^{-\theta_p} Y_t$$

Solve the real wage and real capital returns are as follows:

$$w_t = (1 - \alpha) m c_t Z_t K_{G,t-1}^{\kappa_G} \bar{K}_t^\alpha N_t^{(-\alpha)}$$

$$r_t^k = (\alpha) m c_t Z_t K_{G,t-1}^{\kappa_G} \bar{K}_t^{\alpha-1} N_t^{(1-\alpha)}$$

Referring to the Calvo (1983) hypothesis, we will set the probability of intermediate goods companies changing-price as $1 - W_p$. The probability that firm k does not adjust prices is $(W_p)^k$. The sticky price setting takes the form:

$$MAX : E_t \sum_{k=0}^{\infty} (W_p \beta)^k \frac{u'(C_{t+k})}{u'(C_t)} \left(\frac{P_{j,t}}{P_{t+k}}\right)^{-\theta_p} Y_{t+k} - m c_{t+k} \left(\frac{P_{j,t}}{P_{t+k}}\right)^{-\theta_p} Y_{t+k}$$

Solve the optimal price of viscous intermediate and write the form of inflation:

$$\pi_t^* = \frac{\theta_p}{\theta_p - 1} \pi_t \frac{x_{1t}}{x_{2t}}$$

$$x_{1t} = u'(C_t) m c_t Y_t + (\beta W_p) E_t (\pi_{t+1})^{\theta_p} x_{1t+1}$$

$$x_{2t} = u'(C_t) Y_t + (\beta W_p) E_t (\pi_{t+1})^{\theta_p - 1} x_{2t+1}$$

The price index equation is written in the form of inflation:

$$\pi_t^{1-\theta_p} = (1 - W_p) (\pi_t^*)^{1-\theta_p} + W_p$$

E. Central Bank

We assume that the central bank follows the Taylor rule and focuses on interest rate adjustment.

$$R_t - R_s = (1 - \rho_R) (R_{t-1} - R_s) + \rho_R [\gamma_\pi (\pi_t - \pi_s) + \gamma_y (\log(Y_t) - \log(Y_s))]$$

Here R_s is the steady-state interest rate, π^s is the steady-state inflation, and Y^s is the steady-state output. Parameter ρ_R determines the smoothness of the interest rate. γ_π and γ_y determine the extent to which interest rates

deviate from the steady state for inflation and output.

F. Financial Department

We set the budget in the form of a balance as follows:

$$\frac{B_t}{P_t} + \tau_t^n w_t N_t + \tau_t^c C_t + [u_t r_t^k - \delta(u_t)] \tau_t^k K_{t-1} = C_{G,t} + I_{G,t} + T R_t + \frac{R_{t-1} B_{t-1}}{\pi_t P_{t-1}}$$

Government revenue comes from taxes and bonds, spending for government consumption, government investment, transfer payments and repayment of the previous debt. The form of government public capital accumulation is as follows:

$$K_{G,t} = (1 - \delta_G) K_{G,t-1} + [1 - S_{G,t} \left(\frac{I_{G,t}}{I_{G,t-1}}\right)] I_{G,t}$$

Here, δ_G is the depreciation rate of public capital, we assume that the government's investment adjustment cost form the same as private capital.

$$S_{G,t} = \frac{\kappa}{2} \left[\frac{I_{G,t}}{I_{G,t-1}} - 1 \right]^2$$

For the sake of generality, we refer to Schwarzmueller's (2015) fiscal rule set.

$$\widehat{C}_{G,t} = -\phi_C (\widehat{S}b_{t-1}) - \gamma_C (\widehat{S}b_t) + u_t^C$$

$$\widehat{I}_{G,t} = -\phi_I (\widehat{S}b_{t-1}) - \gamma_I (\widehat{S}b_t) + u_t^I$$

$$\widehat{\tau}_t^c = \phi_{Tc} (\widehat{S}b_{t-1}) + \gamma_{Tc} (\widehat{S}b_t)$$

$$\widehat{\tau}_t^n = \phi_{Tn} (\widehat{S}b_{t-1}) + \gamma_{Tn} (\widehat{S}b_t)$$

$$\widehat{\tau}_t^k = \phi_{Tk} (\widehat{S}b_{t-1}) + \gamma_{Tk} (\widehat{S}b_t)$$

Here, $\widehat{S}b_t$ represents the debt ratio of the government in period t . ϕ_i ($i = C, I, Tc, Tn, Tk$) is the adjustment parameter of the fiscal policy to the economic growth, and γ_i ($i = C, I, Tc, Tn, Tk$) is the adjustment parameter of the fiscal policy to the debt ratio deviating from the steady state. u_t^i ($i = C, I$) is the financial impact, subject to AR (1) process.

G. Parameter Calibration

Before the specific numerical simulation, we first calibrate some parameters, the calibration is mainly based on previous studies. Referencing Zhang Zuomin (2014) study, the discount rate β is 0.98. α is the elasticity of private capital output, with reference to Liu Bin (2009) estimates, to be calibrated to 0.42. Assuming that the government depreciation rate is the same as the depreciation rate δ_0 of private capital, and it is 0.025 (Zhang Zuomin, 2014). The estimated calibration value δ_2 for Leeper (2010) and Schwarzmueller (2015) is set to 0.29. According to Zhang Zuomin (2014) of the estimated investment adjustment cost parameter κ is set to 2.105, the consumption habit parameter calibration h is 0.466. According to Chen Kunting *et al.* (2006), we set the calibrated value of W_p to 0.6. As the domestic literature for wage wage settings vary widely, we assume that the wage adjustment once a year, so the

calibration value of W_w is 0.75. The alternative elasticity of the intermediate product θ_p is 10 (Zhang Zuomin, 2014). The elasticity of labor θ_w is 3. The reciprocal η of labor supply elasticity is 2.16. And the calibration value of the alternative elasticity v of private goods and public goods consumption is 0.8. According to Wang Wenfu's (2010) study, the monetary policy adjustment parameter calibration value $\rho_R=0.92$, $\gamma_\pi=1.766$, $\gamma_y=0.2533$. The proportion of private goods consumption in the total consumption of κ_c is 0.8. Referring to Wang and Yang's (2014) study, we set the steady-state tax rate calibration value $\tau_s^c=0.0937$, $\tau_s^n=0.1007$, $\tau_s^k=0.2851$. By calculating the average of government consumption and

government investment as a proportion of GDP from 2010 to 2014, the calibration value of W_{GC} is 0.135 and the calibration value of W_{GI} is 0.116. There is no consensus on the margin of safety of debt, so we use the "Maastricht Treaty" standard, the debt ratio of the steady-state value is calibrated to 60%. To ensure that each financial repayment rule has a steady state solution, we adjust the fiscal policy smoothing parameter $\phi_i(i = C, I, Tc, Tn, Tk)$ to 0.35 and the fiscal policy adjustment parameter $\gamma_i(i = C, I, Tc, Tn, Tk)$ to 0.45. The assignment of the relevant parameters is shown in Table 1.

Table 1. Parameter Calibration Table.

Parameter	Description	Value	Parameter	Description	Value
β	Subjective discount rate	0.98	γ_π	Inflation adjustment parameter	1.766
α	Output elasticity of private capital	0.42	γ_y	Output smoothing parameter	0.2533
δ_0	Depreciation	0.025	τ_s^c	Consumption tax rate	0.0937
δ_2	Two term coefficient	0.29	τ_s^n	Labor tax rate	0.1007
κ	Investment adjustment cost	2.105	τ_s^k	Capital tax rate	0.2851
h	Consumption habit parameter	0.466	W_{GC}	Government consumption accounting	0.135
W_p	Probability of not adjusting the price	0.6	W_{GI}	Government investment accounting	0.116
W_w	Probability of not adjusting wages	0.75	ϕ_i	Debt smoothing parameter	0.35
θ_p	Elasticity of substitution	10	γ_i	Debt ratio adjustment parameter	0.45
θ_w	Labor force substitution elasticity	3	SbS	Steady-state value of debt ratio	0.6
η	The reciprocal of elasticity of labor supply	2.16	ρ_Z	Total factor impact parameter	0.9
v	Private and public consumption substitution elasticity	0.8	ρ_i	Investment impact parameter	0.9
κ_c	Private goods consumption accounted for	0.8	ρ_c	Consumption impact parameter	0.9
ρ_R	Monetary smoothing parameter	0.92	κ_G	Output elasticity of public capital	0.01~0.18

H. Numerical Simulation

In order to use this model to examine the relationship between government investment efficiency and debt risk, we must choose the relevant indicators in the model as proxy variables of government investment efficiency and debt risk. Because the efficiency of government investment lies in its promoting effect on output, we use the output elasticity of public capital κ_G to represent the efficiency of government investment. At present, the main way to measure the debt risk is to investigate the fluctuation of the debt. So we use the standard deviation of the debt ratio under the impact of government investment to represent the debt risk. He Gang, Chen Wenjing (2008); Yang Feihu, Zhou Quanlin (2013) estimated that China's public capital output elasticity of 0.18

or less. Therefore, we examine the fluctuation of the corresponding elasticity of public capital output from 0.01 to 0.18.

We introduce fiscal investment shocks to represent the relationship between government investment efficiency and debt risk. Figure 1 shows the relationship between the elasticity of public capital output and the standard deviation of debt ratios. It can be seen from the figure that with the increase of public capital output elasticity, the fluctuation of debt ratio under the impact of financial investment is getting smaller and smaller. The government investment efficiency and the debt risk have the reverse change relations, the government investment efficiency is higher, the debt risk is lower.

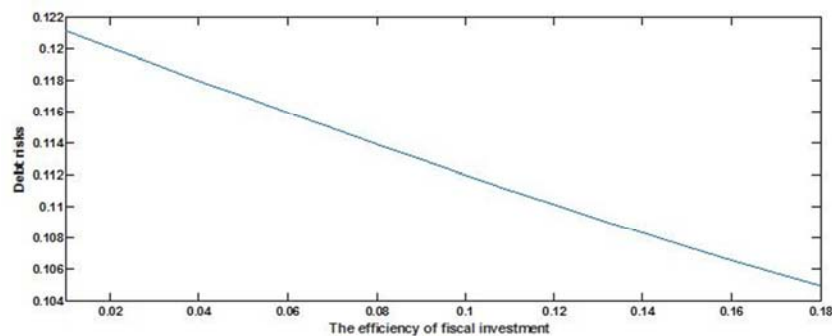


Figure 1. Relationship between Debt Risk and Government Investment Efficiency.

In order to reflect the fluctuation difference of debt ratio under different government investment efficiency level, we take the elasticity of public capital output as 0.05, 0.1 and 0.5 respectively. The impact of different debt ratio fluctuations in the situation is shown in Figure 2. From the figure, we can see

that under different conditions of the output elasticity of public capital, the fluctuation of the liability rate caused by the impact is different. The higher the elasticity of public capital output, the smaller the fluctuation of debt ratio.

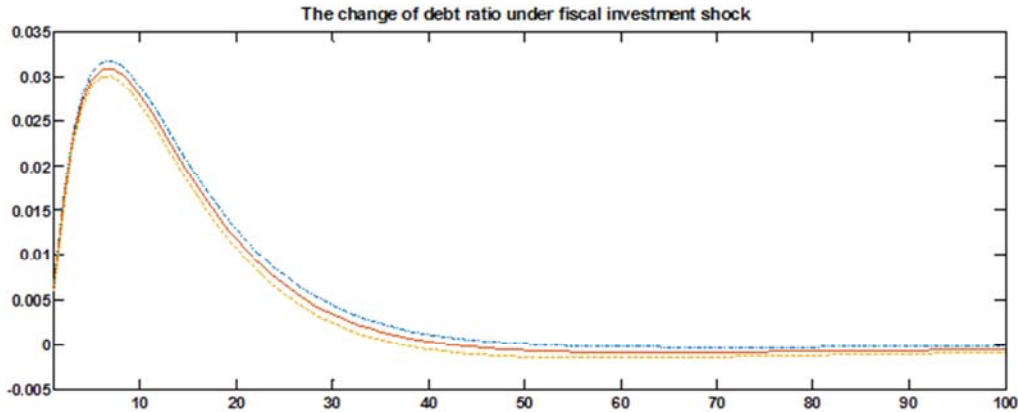


Figure 2. Debt Rate of Impact.

3. Conclusion and Suggestion

This paper examines the relationship between the efficiency of government investment and the debt risk from a theoretical perspective. By constructing a DSGE model, we can observe that there is a significant negative correlation between the efficiency of government investment and the risk of debt. Chinese economy is currently facing downward pressure. Government debt burdens are on the rise. The task of resolving the government debt risk is urgent.

This paper proposes to resolve the local government debt risk by controlling the efficiency of government investment. Improve the efficiency of government investment from government debt investment "stock" and "incremental" two aspects.

On the one hand, we need to improve the efficiency of local government's "stock" investment. At present, the problem of excess capacity in China is still grim. We need to remove the excess capacity, promote the optimization and adjustment of economic structure. We need to strengthen government budget management. We need to strictly follow the requirements of the new budget law, strengthen supervision and management, strengthen budget constraints.

On the other hand, we need to improve the efficiency of government's "incremental" investment. We must clarify the government and market boundaries. We must optimize the government investment structure. We need to focus our investments primarily on where the market fails. We need to protect the public sector investment, while continuing to vigorously promote the PPP project.

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