Models for Estimating Precipitable Water Vapour and Variation of Dew Point Temperature with Other Parameters at Owerri, South Eastern, Nigeria

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Abstract: Precipitable water vapour (PWV) is a vital component of the atmosphere and appreciably controls many atmospheric processes. The PWV is not easy to measure with sufficient spatial and time resolution under all weather conditions. In this paper, three precipitable water vapour models; the Smith, Won and Leckner’s models were evaluated and compared for Owerri (Latitude 5.48°N, Longitude 7.00°E, and 91 m above sea level) using meteorological parameters of monthly average daily maximum temperature, minimum temperature and relative humidity during the period of sixteen years (2000-2015). The Leckner’s model was found most suitable and therefore recommended for estimating PWV for the location with range between 3.253 and 4.662 cm. The highest PWV occurred in June for Won and Leckner’s models while for Smith’s model it occurred in September; the lowest PWV occurred in January for all the evaluated models. The result showed that high values of dew point temperature ($T_{dew}$), PWV and relative humidity (RH) were observed during the raining season and low values in the dry season; this is an indication that the dew point temperature is a reflection of the PWV and RH. The dew point temperature is an opposite reflection of the virtual temperature ($T_{virtual}$), potential temperature ($T_{potential}$) and mean temperature ($T_{mean}$). The dew point temperature increases and decreases with mean temperature in the months from January to March and in July respectively for the location under investigation. The values of the dew point temperature indicated that the air is stable signifying no development of severe weather condition like thunderstorms. The maximum and minimum virtual temperature correction of 3.3246°C and 2.3371°C occurred in June and January respectively while for the dew point depression, it occurred in the months of January and September with 8.7514°C and 2.1094°C. The descriptive statistical analysis shows that the dew point temperature, potential temperature, mean temperature and virtual temperature correction data spread out more to the left of their mean value (negatively skewed), while the virtual temperature and dew point depression data spread out more to the right of their mean value (positively skewed). The dew point temperature and the virtual temperature correction data have positive kurtosis which indicates a relatively peaked distribution and possibility of a leptokurtic distribution while the virtual temperature, potential temperature, mean temperature and dew point depression data have negative kurtosis which indicates a relatively flat distribution and possibility of platykurtic distribution.

Keywords: Precipitable Water Vapour, Dew Point Temperature, Relative Humidity, Virtual Temperature, Potential Temperature and Mean Temperature
1. Introduction

Water vapor plays a vital role in climate change, hydrological processes, Earth’s energy balance, and weather systems [1-3]. Water vapor is the most abundant greenhouse gas in the atmosphere, and it accounts for about 60% of the natural greenhouse effect [4]. As a result of this, the saturation vapor pressure is expected to increase as a response to rises in air temperature. Therefore, atmospheric water vapor provides a strong positive feedback for global warming as well as carbon (iv) oxide, ozone, methane, and other greenhouse gases [1, 5-9]. Thus, the processes on how water vapor changes in both the real atmosphere and climate models is significant, not only for a better understanding of water vapor feedback on global warming but also for the exploration of climate change [10].

Water vapor absorbs most solar radiation and is considered the most important greenhouse gas in the atmosphere [11]. It can also lead to global warming as it is the major cause of the greenhouse effect. It cycles continuously through the process of evaporation and condensation, transporting heat energy around the earth and between the surface and the atmosphere [12].

The quantity of liquid water that would be acquired if all the vapour in the atmosphere within the vertical column were compressed to the point of condensation is called PWV [13]. Generally, the standard methods for PWV measurement are radiosondes [14], ground-based microwave radiometers, LIDAR systems [15-16], LASER systems [17] and GPS satellites [18-22]. Nevertheless, each method has its own drawbacks. LIDAR measurements are costly [23]. Low spatial resolution restricts the use of space based instruments [23]. It is almost impossible to quantify an exact PWV trend from radiosonde PWV owing to limitations such as incomplete and inhomogeneous observations and sparse spatial distributions [7, 24]. Furthermore, numerous factors such as variation in instrumentation, uncontrollable balloons, upgrades to instruments, and temporal inhomogeneities sometimes cause spurious shifts in the radiosonde PWV time series [25].

The temperature at which the moisture/liquid water (water vapour) in the atmosphere evaporates at same rate at which it condenses is known as dew point temperature. Dew point temperature values are vital to meteorologists because it measures essentially the state of the atmosphere based on how much water vapor is present [26]. Similarly, dew point temperature offers a fairly direct sense of how comfortable or uncomfortable warm air is felt. Dew point provides us with an idea for forecasting the next day low temperatures, under certain conditions the lowest temperature tends to be close to the dew point at the time of maximum temperature the day before [27]. The values of dew point temperature aids in prognosticating the formation of fog or dew and in estimating rain, snow, dew, evapotranspiration, near surface humidity and other meteorological parameters. In addition, higher dew points through the troposphere (especially those above 60°C) can help to support more numerous and/or severe thunderstorms when other factors favor their formation. The importance of dew point temperature affects us in one way or the other especially when one recognizes this important factor, the amount of moisture in a gas, impacts much more than Heating, Ventilation and Cooling (HVAC) considerations. (i) It is an essential factor in convective heat transfer, combustion of fossil fuels and combustion engineering, drying of paper, cardboard, plastics, wood, tobacco, leather, printed goods, textiles and grain. (ii) It plays a key role in the efficient use of energy in many chemical manufacturing processes as well as the attainment of high product yield. (iii) The effect of moisture in gases also plays a very important role in corrosion phenomena which can result in damage and loss of not only unprotected metals, like iron and steel structural components, but also improperly treated or stored steel and other metal products [28].

The virtual temperature is the temperature that dry air would need to attain in order to have the same density as the moist air at the same pressure. Because moist air is less dense than dry air at the same temperature and pressure, the virtual temperature is always greater than the actual temperature. However, even for very warm and moist air, the virtual temperature exceeds the actual temperature by only a few degrees [29].

The potential temperature $T_{\text{potential}}$ of an air parcel is defined as the temperature that the parcel of air would have if it was expanded or compressed adiabatically from its existing pressure and temperature to a standard pressure $p_0$ (generally taken as 1000 hPa) [29].

The purpose of this study was to (i) compare three precipitable water vapour (PWV) models to ascertain their suitability for Owerri (ii) to estimate dew point temperature and to investigate its variation with the PWV, relative humidity, virtual temperature, potential temperature and mean temperature. (iii) Evaluation of virtual temperature correction and dew point depression along with descriptive statistical analysis.

2. Study Area

Figure 1 shows the study area under investigation. Imo is a state in Nigeria located in south eastern Nigeria. Owerri (Latitude 5.48°N, Longitude 7.00°E, and 91 m above sea level) is the capital city of Imo and one of the largest in the state. The State is bordered by Abia State on the East, River Niger and Delta State to the West, Anambra State on the North and Rivers State to the South. Based on the changes that occur as a result of rising surface temperature and rainfall, the area is likely vulnerable to the consequences of global warming [30]. Two seasons are identified, wet and dry seasons. The rainy season is from April to October while the dry season is from November to March. Double maxima, with the first maximum in June and the second in September also characterized the climate. There is therefore a “little dry season” in-between known as “August Break” brought about by the seasonal north and southward movement of the ITCZ.
(Inter-Tropical Convergence Zone). An average annual temperature above 20°C (68.0°F) creates an annual relative humidity of 75%, with humidity reaching 90% in the rainy season [30]. The dry season experiences two months of Harmattan from late December to late February. January and March are the hottest months [30].

Imo state has three main political zones; this are, Okigwe (Imo North), Orlu (Imo West) and Owerri (Imo East). According to Okorie [31], the state has a population of about 3, 927, 563 with male, 1, 976, 471 and female 1, 951, 092. The state is blessed with natural resources which include, crude oil, natural gas, lead and zinc. Economically exploitable flora like the iroko, mahogany, obeche, bamboo, rubber tree and oil palm predominate [30].

Figure 1. Map of (a) Google map showing the study area (b) Map of Nigeria showing the study area.

3. Methodology

The monthly average minimum temperature, maximum temperature and relative humidity meteorological data used in this study were obtained from the European Centre for Medium-Range Weather Forecasts (ECMWF) at 2m height for owerrri, Imo state located in the South Eastern, Nigeria during the period of sixteen years (2000-2015).

Smith [32] developed a correlation between precipitable water and dew point temperature. The coefficients in this correlation vary with latitude and season. Atwater and Ball [33] simplified Smith [32] correlation to

\[ w' = \exp(0.07074 T_{dew} + D) \]  \( (1) \)

where \( w' \) is in centimeters, \( T_{dew} \) is the station’s dew-point temperature in degrees Celsius and \( D = -0.02290 \) from April to June and 0.02023 for the remaining months.

For all seasons, Won [34] has developed a simple correlation as follows

\[ w' = 0.1 \exp(2.2572 + 0.05454 T_{dew}) \]  \( (2) \)

The precipitable water as obtained from Equations (1) and (2) applies to prevailing station pressure and temperature. However, the attenuation equations often require this quantity to be reduced to a datum of 1013.25 mbars pressure and 273 K temperature. Paltridge and Platt [35] suggest the following formula for reduction of \( w' \) to the datum conditions:

\[ w = w'(\frac{p}{1013.25})^{3/4}(\frac{273}{T})^{1/2} \]  \( (3) \)

where \( w \) is the reduced precipitable water in centimeters, \( p \) is station pressure in millibars, and \( T \) is the surface (dry-bulb) temperature in degrees Kelvin.

Leckner [36] has presented the following formula, which expresses precipitable water in terms of relative humidity:

\[ w = \frac{0.495 \varphi p_s}{T} \]  \( (4) \)

where \( \varphi \) is relative humidity in fractions of one, \( T \) is ambient temperature in degrees Kelvin and \( p_s \) is the partial pressure of water vapour in saturated air and is given by the semi empirical equation as

\[ p_s = \exp(26.23 - \frac{5416}{T}) \]  \( (5) \)

The pressure and temperature correction is not necessary in equation (4) since it is already included in its numerical constant.
The dew point temperature \( T_{dew} \) was obtained using [37] as:

\[
T_{dew} = T - \left( \frac{100 - RH}{5} \right)
\]

(6)

where \( T \) and \( RH \) are the mean temperature and relative humidity in degree Celsius and percentage respectively.

The Virtual temperature \( T_{virtual} \) was obtained using the expression [29] as

\[
T_{virtual} = \frac{T}{1 - \varepsilon(1 - \varepsilon)}
\]

(7)

where \( \varepsilon \) is water vapour pressure and \( \varepsilon \) is a constant given as \( \varepsilon = 0.622 \).

The Potential temperature \( T_{potential} \) was obtained using the expression [29] as

\[
T_{potential} = T_{mean} \left( \frac{p_0}{p} \right)^{R/cp}
\]

(8)

Equation (8) is called Poisson’s equation, where \( p_0 \) is a standard pressure generally taken as 1000 hPa and \( R/cp = 0.286 \).

The virtual temperature \( T_{vc} \) correction is given by [29] as

\[
T_{vc} = T_{virtual} - T_{mean}
\]

(9)

The dew point depression \( T_{depression} \) is given by [29] as

\[
T_{depression} = T_{mean} - T_{dew}
\]

(10)

In this paper, the skewness and kurtosis tests were studied. The skewness test \( (\sigma_s) \) measures the asymmetry of the parameters data around their mean value; it is a measure of symmetry, or more precisely, the lack of symmetry [38]. It gives information about the direction of variation of the dataset [38]. If \( \sigma_s = 0 \), the data have a Gaussian distribution (normal distribution), while \( \sigma_s < 0 \) indicates that the data are spread out more to the left of the mean value than to its right (negatively skewed), when \( \sigma_s > 0 \) signifies that data are spread out more to the right than to its left (positively skewed) [39].

The Kurtosis test \( (k_u) \) explains the shape of a random variable’s probability distribution, that is it characterizes the relative peakedness or flatness of a distribution compared to the normal distribution [38]. It measures the degree of normality of each of the meteorological parameters under investigation [39]. For \( k_u = 0 \) the data have normal distribution, for \( k_u > 0 \) the data have positive kurtosis which connotes peaked distribution, that is, leptokurtic distribution (that is, too tall), when \( k_u < 0 \) the data have negative kurtosis which implies flat distribution, that is, platykurtic distribution (that is, too flat, or even concave if the value is large enough).

4. Results and Discussion

The result in figure 2 revealed that; the Smith’s model increases from its minimum value of 3.436 cm in the month of January to March and slightly decreases in April and then increases to July and decreases with a dip downward in the month of August and then increases to its maximum value of 4.807 cm in the month of September and drop subsequently to December.

The Won’s model increases from its minimum value of 2.401 cm in the month of January and attained its maximum value of 3.135 cm in June and then decreases to August and slightly increases to September and drop subsequently to December.

The Leckner’s model increases gradually from its
minimum value of 3.253 cm in the month of January and attained its maximum value of 4.662 cm in the month of June and then decreases to August and slightly increases to September and drop subsequently to December.

The result of the Won’s model showed that the precipitable water vapour are far away from the other models; however, the Leckner’s model slightly overestimated the Smith’s model in the months of April, May and June. The Leckner’s precipitable water vapour model is found in between the two models and was reported most suitable model for estimating precipitable water vapour for the study area, since statistical test for validation was not carried out. The conclusion drawn from this as to which model is most suitable for PWV estimation is in conformity with the study analyzed in [40].

Figure 3 shows the variation of dew point temperature with precipitable water vapour at Owerri, Nigeria.

Figure 3 shows the variation of dew point temperature with precipitable water vapour for the location under investigation. The dew point temperature and precipitable water vapour increases from their minimum value of 18.061°C and 3.253 cm in the month of January and attained their maximum value of 22.879°C and 4.662 cm in the month of June and decreases from June to August with a dip downward; though the dew point temperature is more conspicuous. The dew point temperature and precipitable water vapour increases to September and drop to December. The result indicated high and low values of dew point temperature and precipitable water vapour during the raining and dry seasons respectively. The result further showed that the dew point temperature is a reflection of the precipitable water vapour.

Figure 4 shows the variation of dew point temperature with relative humidity at Owerri, Nigeria.

Figure 4 shows the variation of dew point temperature with relative humidity for the location under investigation.
The relative humidity increases from its minimum value of 56.243% in the month of January to 89.002% in July and then decreases slightly in the month of August and increases to its maximum value of 89.453% in September and drop subsequently to December. The dew point temperature follows similar pattern of variation except that its minimum value of 18.061°C was observed in the month of January and maximum value of 22.879°C in the month of June; the decrease in the value of dew point temperature begins from July while for relative humidity is from August. High and low values of dew point temperature and relative humidity were observed during the raining and dry seasons respectively. The result of this study revealed that the dew point temperature is a reflection of relative humidity.

Figure 5 shows the monthly variation of dew point temperature, virtual temperature, potential temperature and mean temperature for the location under investigation. The result revealed that the virtual temperature is greater than the dew point temperature, potential temperature and mean temperature while the dew point temperature has the lowest value. The potential temperature and mean temperature follows similar pattern of variation and the virtual temperature follows almost similar pattern of variation; the virtual temperature, potential temperature and mean temperature increases slightly from January to March and decreases from March to July and maintain almost a constant value from July to September and increases from September to December while the virtual temperature decreases slightly from November to December. On the other hand, the dew point temperature increases from it minimum value of 18.061°C in the month of January and attained its maximum value of 22.879°C in the month of June and decreases from June to August with a dip downward and then increases to September and drop to December. The result of this study showed high values of virtual temperature, potential temperature and mean temperature during the dry season and low values during the raining season while for the dew point temperature high values were recorded during the raining season and low values during the dry seasons; this shows that the dew point temperature is an opposite reflection of the virtual temperature, potential temperature and mean temperature. Considering the dew point temperature and the mean temperature; the dew point temperature increases with increase in mean temperature from January to March and decreases with decrease in mean temperature in the month of July for the location under investigation. The result indicated that the dew point temperature is always less than the mean/air temperature which implies that mean temperature cannot be lower than the dew point temperature; this helps meteorologists predict temperature lows in a weather forecast. The moderate values of the dew point temperature signifies the stability of air for the study area and less tendency of development of thunderstorms as very high dew point temperature can bring about severe weather condition.

Table 1. Monthly average virtual temperature correction and dew point depression for Owerri, Nigeria.

<table>
<thead>
<tr>
<th>Month</th>
<th>(T_{\text{dew}}) (°C)</th>
<th>(T_{\text{virtual}}) (°C)</th>
<th>(T_{\text{potential}}) (°C)</th>
<th>(T_{\text{mean}}) (°C)</th>
<th>(T_{\text{v}}) (°C)</th>
<th>(T_{\text{depression}}) (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>JAN</td>
<td>18.0611</td>
<td>29.1496</td>
<td>27.6106</td>
<td>26.8125</td>
<td>2.3371</td>
<td>8.7514</td>
</tr>
<tr>
<td>FEB</td>
<td>20.196</td>
<td>30.4729</td>
<td>28.5771</td>
<td>27.7219</td>
<td>2.751</td>
<td>7.5259</td>
</tr>
<tr>
<td>MAR</td>
<td>21.1418</td>
<td>30.7715</td>
<td>28.6814</td>
<td>27.8125</td>
<td>2.959</td>
<td>6.6708</td>
</tr>
<tr>
<td>APR</td>
<td>21.5848</td>
<td>30.3427</td>
<td>28.1172</td>
<td>27.219</td>
<td>3.0709</td>
<td>5.6871</td>
</tr>
<tr>
<td>MAY</td>
<td>22.3406</td>
<td>29.9304</td>
<td>27.4276</td>
<td>26.9699</td>
<td>3.2335</td>
<td>4.3563</td>
</tr>
</tbody>
</table>
The maximum and minimum virtual temperature correction of 3.3246°C and 2.3371°C was obtained in the months of June and January with an average value of 3.0177°C. The maximum and minimum dew point depression of 8.7514°C and 2.3566°C was obtained in the months of January and September with an average value of 4.8817°C. The result shows that the maximum and minimum dew point depression and virtual temperature correction occurred in the month of January. The average dew point temperature, virtual temperature, potential temperature and mean temperature are 21.3878°C, 29.2872°C, 26.9812°C and 26.2695°C respectively for Owerri during the period under investigation.

The results shown in Table 2 showed that the dew point temperature, potential temperature, mean temperature and virtual temperature correction data spread out more to the left of their mean value (negatively skewed), while the virtual temperature and dew point depression data spread out more to the right of their mean value (positively skewed). The virtual temperature, potential temperature, mean temperature and dew point depression data seem to have a quasi-Gaussian distribution. Skewness of exactly zero is quite not likely for real world data [38]. The dew point temperature and virtual temperature correction data are more divergent away from the normal distribution. It is clear from Table 2 that the dew point temperature and the virtual temperature correction data have positive kurtosis which indicates a relatively peaked distribution and possibility of a leptokurtic distribution. The virtual temperature, potential temperature, mean temperature and dew point depression data have negative kurtosis which indicates a relatively flat distribution and possibility of platykurtic distribution.

5. Conclusion

This study presents the distribution of monthly mean Precipitable water vapour (PWV) based on three models, the Smith; Won; and the Leckner’s model using meteorological parameters of monthly mean temperature and relative humidity obtained from the European Centre for Medium-Range Weather Forecasts (ECMWF) at 2m height for Owerri, Imo state located in the South Eastern, Nigeria during the period of sixteen years (2000-2015). The distribution of PWV showed clear differences; the Smith (ranging from 3.436 to 4.807 cm); Won (ranging from 2.401 to 3.135 cm) and the Leckner’s model (ranging from 3.253 to 3.135 cm). The highest PWV occurred in June for Won and Leckner’s model while for Smith’s model it occurred in September. The lowest PWV occurred in January for all the models. High values of virtual temperature, potential temperature and mean temperature were observed during the dry season and low values during the raining season while for the dew point temperature and RH, high and low values were observed during the raining and dry seasons respectively; this is an indication that the dew point temperature is an opposite reflection of virtual temperature, potential temperature and mean temperature. However, the dew point temperature is a reflection of the relative humidity. The values of the dew point temperatures indicated that the air is stable and less occurrences of thunderstorm; in view of these, this present study would help to guide against the episodes of climate induced environmental disaster like thunderstorm and can also enhance agricultural production in the study area. The maximum and minimum virtual temperature correction of 3.3246°C and 2.3371°C occurred in June and January while for the dew point depression it occurred in the months of January and September.

<table>
<thead>
<tr>
<th>Month</th>
<th>T_{dew} (°C)</th>
<th>T_{virtual} (°C)</th>
<th>T_{potential} (°C)</th>
<th>T_{mean} (°C)</th>
<th>T_{vc} (°C)</th>
<th>T_{depression} (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>AUG</td>
<td>22.4121</td>
<td>27.9845</td>
<td>25.2998</td>
<td>24.7688</td>
<td>3.2158</td>
<td>2.3566</td>
</tr>
<tr>
<td>NOV</td>
<td>21.5740</td>
<td>29.6792</td>
<td>27.3792</td>
<td>26.6031</td>
<td>3.0761</td>
<td>5.0291</td>
</tr>
<tr>
<td>DEC</td>
<td>18.7168</td>
<td>29.2391</td>
<td>27.5460</td>
<td>26.7625</td>
<td>2.4766</td>
<td>8.0458</td>
</tr>
</tbody>
</table>

**Table 2.** Descriptive statistical analysis for the estimated parameters for Owerri, Nigeria.

<table>
<thead>
<tr>
<th>Range</th>
<th>Minimum</th>
<th>Maximum</th>
<th>Sum</th>
<th>Skewness</th>
<th>Kurtosis</th>
</tr>
</thead>
<tbody>
<tr>
<td>Statistic</td>
<td>4.8183</td>
<td>28.0658</td>
<td>22.879</td>
<td>-1.279</td>
<td>0.762</td>
</tr>
<tr>
<td>T_{dew}</td>
<td>2.787</td>
<td>27.9845</td>
<td>30.772</td>
<td>0.082</td>
<td>-1.041</td>
</tr>
<tr>
<td>T_{virtual}</td>
<td>3.3816</td>
<td>25.3000</td>
<td>28.681</td>
<td>-0.175</td>
<td>-1.262</td>
</tr>
<tr>
<td>T_{potential}</td>
<td>3.0437</td>
<td>24.7690</td>
<td>27.813</td>
<td>-0.155</td>
<td>-1.240</td>
</tr>
<tr>
<td>T_{mean}</td>
<td>0.3975</td>
<td>2.3371</td>
<td>3.3246</td>
<td>-1.279</td>
<td>0.686</td>
</tr>
<tr>
<td>T_{vc}</td>
<td>6.642</td>
<td>2.1094</td>
<td>8.7514</td>
<td>0.326</td>
<td>-1.273</td>
</tr>
<tr>
<td>T_{depression}</td>
<td>-1.273</td>
<td>0.326</td>
<td>8.7514</td>
<td>-1.273</td>
<td>0.326</td>
</tr>
</tbody>
</table>
depression data have negative kurtosis which indicates a relatively flat distribution and possibility of platykurtic distribution for the location under investigation.

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