

Logarithmic running of ‘t Hooft-Polyakov monopole to dark energy

M. S. El Naschie

Dept. of Physics, University of Alexandria, Alexandria, Egypt

Email address:

Chaossf@aol.com

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Abstract: The paper presents a particle physicists’ interpretation of the mathematical abstract concept of a five dimensional empty set as the source of dark energy and dark matter. It turns out that the simplest alternative physical interpretation at least from the view point of the GUT unification of fundamental interaction is the theoretically well established but experimentally never found yet ‘t Hooft-Polyakov magnetic giant monopole with the predicted huge mass of ten to the power of 16 Gev. In fact it will be shown here using exact renormalization equations that running the preceding energy logarithmically leads to a prediction of the ordinary and the total dark energy density of the cosmos in complete agreement with our earlier result $E(O) = mc^2/22$ and $E(D) = mc^2(21/22)$ based on the afore mentioned set theoretical concepts as well as with all the relatively recent cosmological measurements. The decisive steps in the present derivation consists of two realizations. First and to our deepest surprise and delight, $E = \gamma mc^2 = mc^2$ is actually a unification formula uniting classical, relativistic and quantum mechanics where $\gamma = 1$ corresponds to a 100% energy density. Second and also not expectedly, the logarithmic running of ‘t Hooft-Polyakov’s monopole energy leads to a reduction factor $\gamma = 1/\lambda$ where $\lambda = \frac{1}{2} \ln \frac{M(\text{monopole})}{m(\text{electron})} = 22.18033989$, in full agreement with our previous results using entirely different approaches. Finally the results are validated using ‘t Hooft’s dimensional regularization $D = 4 - \epsilon$ by setting $\epsilon = 2\phi^5$ where ϕ^5 is Hardy’s quantum entanglement and $\phi = 2/\sqrt{5} + 1$.

Keywords: Dark energy, Grand Unification, Giant ‘T Hooft-Polyakov Monopole, Quantum Relativity Renormalization Equations, Fractal Spacetime, Quantum Field Theory, Super Symmetry, Dark Matter, Planckton, ‘T Hooft Renormalization

1. Introduction

The major challenge of explaining that our universe is neither static nor simply expanding with a decreasing rate as it was thought for a considerable time but in fact suffers an increased expansion was tackled in numerous recent publications [1-18]. Thus we have offered in the last two years several alternative theories all leading virtually to precisely the same quantitative and qualitative results, namely that the ordinary measurable energy density $E(O)$ is given by

$$E(O) = (\phi^5 / 2)(mc^2) \tag{1}$$

$$= mc^2 / 22$$

where m is the mass, c is the speed of light, ϕ^5 is Hardy’s generic probability of quantum entanglement [6,12] and $\phi = 2 / (1 + \sqrt{5})$. Consequently the rest which we refer to for simplicity as dark energy but really mean dark energy as

well as dark matter must be [19]

$$E(D) = (1 - \phi^5 / 2) (mc^2) \tag{2}$$

$$= (5\phi^2 / 2)(mc^2)$$

$$= mc^2 (21 / 22)$$

It is needless to reiterate that $E(D)$ could never be measured directly until this point of time but its existence is inferred from the increased rather than decreased rate of cosmic expansion as well as several observed astronomical anomalies [1-5]. It then turned out that $E(O)$ is the energy stored in a five dimensional zero set volume modeling the quantum particle while $E(D)$ is the energy stored in the five dimensional volume of the empty set modeling the quantum wave [10-12]. This line of reasoning may be labeled

transfinite set theoretical-topological resolution of dark energy [9-13]. Another line of attack on this problem was undertaken using geometrical reasoning based upon the properties of real physical spacetime akin to that proposed by Cartan and Einstein as influenced by the pioneering work of the brothers Cosserat [9,20].

In the present work we want to utilize more traditional particle physicists' conceptions in solving this problem and bring it nearer to the understanding of conventional high energy physics and quantum field theory [20-30]. This possibility was indeed realized via a GUT scenario based upon 't Hooft-Polyakov giant monopole [31] as will be explained in the next section.

2. Assembling the Fundamental Equations Needed for the Analysis

Central to our present analysis are a few fundamental equations revolving around a transfinitely exact version of the logarithmic renormalization equations of the strong interaction and grand unification [21]. In the transfinite form these otherwise quite complex equations take an unheard of simplicity [22]. For GUT unification for instance the fundamental equation [21-25, 32]

$$\bar{\alpha}_u = \bar{\alpha}_3 + \bar{\alpha}_4 + \frac{1}{N} \ell_n \frac{M_u}{M_o} \quad (3)$$

becomes

$$\begin{aligned} \bar{\alpha}_u (\text{GUT}) &= \bar{\alpha}_3 + \bar{\alpha}_4 + \frac{1}{N} \ell_n \frac{10^{16} \text{Gev}}{M_z} \\ &= (9+1) + (1) \left[\ell_n \left(\frac{10^{16} \text{Gev}}{91 \text{Gev}} \right) \right] \\ &= 10 + 32.330501 N \\ &= 42.33 \\ &\approx 42 \end{aligned} \quad (4)$$

where 10^{16} Gev is the grand unification energy scale, $M_z = 91 \text{Gev}$ is the mass of the Z^0 particle and $\bar{\alpha}_3 = 9$ and $\bar{\alpha}_4 = \bar{\alpha}_{\text{QG}} = 1$ are the inverse coupling of the strange interaction and the coupling of quantum gravity respectively [11,12,18]. We note the proximity of $\bar{\alpha}_u \approx 42.33$ to the exact value found using various methods $\bar{\alpha}_u = 42.36067977$ [26,27]. It is instructive before going any further to consider the case of super symmetric GUT [29-32]. In this case all that changes is that $N = 2$ instead of 1 which is the minimal case of a single super symmetric partner to each fermion or Boson. Inserting one finds

$$\begin{aligned} \bar{\alpha}_u (\text{super symmetric GUT}) &= 10 + \left(\frac{1}{2} \right) (32.33) \\ &\approx 10 + 16.18 \\ &\approx 26 \end{aligned} \quad (5)$$

in full agreement with all results reported in the literature [24-27]. More over we note that $\bar{\alpha}_u \approx 26$ is the same value found when gravity is involved which proves the point observed some time ago, namely that super symmetry already implies quantum gravity whether gravity is involved explicitly or not [21-27]. What may be less well known in the field is the fact that probing the Planck scale leads also automatically to the quantum gravity result as may be demonstrated in the following analysis in which we take M_u to be the Planck mass, i.e. Planckton with a mini black hole mass 10^{19} Gev and replace M_z by the electron scale $m_e = 0.511 \text{mev}$ [21-25, 33]. Inserting one finds

$$\begin{aligned} \bar{\alpha}_u (\text{Planck}) &= (\bar{\alpha}_3 = 0) + (\bar{\alpha}_4 = 1) + \left(\frac{1}{2} \right) \ell_n \frac{10^{19} \text{Gev}}{(0.511)(10)^{-3} \text{Gev}} \\ &= 1 + \frac{1}{2} \ell_n (10^{22} / 0.511) \\ &= 1 + \frac{1}{2} (51.32825773) \\ &= 1 + 25.664 \\ &\approx 26.664 \end{aligned} \quad (6)$$

Note that the correct result was found but only after setting $N = 2$ as well as the obvious values $\bar{\alpha}_4 = \bar{\alpha}_{\text{QG}} = 1$ and $\bar{\alpha}_3 = \infty$ which means $\bar{\alpha}_3 = 0$ [24-27]. Encouraged by these results we could apply the entire previous mathematical machinery developed initially by the pioneering efforts of 't Hooft, Kadanof, Wilson, Fisher and Gross to find the exact value of the most basic and fundamental constants of nature, namely $\bar{\alpha}_o \approx 137$. Without going into detail this is found to be [24-27]

$$\bar{\alpha}_o = (\bar{\alpha}_2 + \bar{\alpha}_3 + \bar{\alpha}_4) + (\bar{\alpha}_1) (1/\phi) \quad (7)$$

where $\bar{\alpha}_1 = 60$, $\bar{\alpha}_2 = 30$, $\bar{\alpha}_3 = 9$, $\bar{\alpha}_4 = 1$, $1/\phi = 1 + \phi = 1.618033989$ and $\phi = (\sqrt{5} - 1)/2$. Inserting we find

$$\begin{aligned} \bar{\alpha}_o &= R^{(4)} (1/\phi)^{5-1} \\ &= (20) (1/\phi)^4 \\ &= 137 + k_o \\ &= 137 + \phi^5 (1 - \phi^5) \\ &= 137.082039325 \end{aligned} \quad (8)$$

exactly as should be [26,27] where $k = \phi^3 (1 - \phi^3)$, $k_o = k_o = \phi^5 (1 - \phi^5)$, $\phi = 1/(1 + \sqrt{5})$ and ϕ^5 is Hardy's quantum entanglement probability. Now we are in a position to tackle the problem at hand regarding dark energy [5-36].

3. Coupling at the Threshold of GUT and Dark Energy Density

Let us apply our renormalization equation to the situation when the unification scale is that of the 't Hooft-Polyakov GUT monopole and the reference scale is that of

electromagnetism. Thus we are involving a giant monopole with $M \approx 10^{16}$ Gev indirectly with the smallest magnetic charge possible associated with normal electric current, i.e. the electron. Setting $N = 2$ and observing that $\bar{\alpha}_3$ and $\bar{\alpha}_4$ must be zero, one finds

$$\begin{aligned} \bar{\alpha}_u &= 0 + \frac{1}{2} \ell_n \left[\frac{10^{16} \text{Gev}}{(0.511)(10)^{-3} \text{Gev}} \right] \\ &= \frac{1}{2} \left(\ell_n \frac{10^{19}}{0.511} \right) \\ &= \frac{1}{2} (44.42050246) \\ &\approx 22.2 \\ &\approx 22 + k \end{aligned} \tag{9}$$

In other words $\bar{\alpha}_u = (26 + k) - 4 = 22 + k$ could naturally be interpreted as the compactified dimensions of the bosonic string space of the Nambu-Veneziano strong interaction model [15] bringing two instructive tautological equations [9,19]

$$\begin{aligned} \sum_1^4 \bar{\alpha}_u &= 60 + 30 + 9 + 1 \\ &= (D^{(10)})^2 \\ &= 100 \end{aligned} \tag{10}$$

and

$$\begin{aligned} D(26) + \bar{\alpha}_2 + 44 \\ = 100 \end{aligned} \tag{11}$$

to interact with the basically cosmic measurement of energy expressed in a percentage [19]

$$\begin{aligned} E_{\text{total}\%} &= \left(\frac{1}{2} 2 + k\right)\% + (22 + k)\% + 73.3116292\% \\ &= (4.568497187) + (22 + k) + (73.3116292) \\ &= 100\% \end{aligned} \tag{12}$$

Thus the following two energy densities sum up the most important conclusions which we can draw from the preceding analogy:

$$\begin{aligned} \text{(a)} \quad E(O) &= mc^2 / (\bar{\alpha}_u) = mc^2 / (22 + k) \\ \text{(b)} \quad E(D) &= 1 - E(O) \end{aligned} \tag{13}$$

$$\begin{aligned} &= \left[\frac{1}{1 + \frac{1}{21+k}} \right] mc^2 \\ &= mc^2 [(21+k)/(22+k)] \end{aligned} \tag{14}$$

We note that E(D) clearly marks the state when our essentially fractal universe [34,35] shrinks to almost one dimension. The exact value is actually one plus the ratio one

to what is left from the $26 + k$ when we allow for the 5 dimensions of de Sitter which is the precursor for the ten dimensionality of superstrings and the eleven dimensions of super gravity and Witten's M-theory. Of course it all started with Kaluza-Klein's 5D space and it may be at least a source of bemusement to ponder if there are truly non-trivial deep connections between the sum of all internal and space dimensions involving E8E8 and Einstein's $D^{(4)}$ on the one side and the sum of all inverse fundamental constants on the other side, which leads to $D^{(5)}$

$$\begin{aligned} \frac{|E8E8| + D^{(4)}}{\sum_1^4 \bar{\alpha}_i} &= \frac{496 + 4}{100} \\ &= D^{(5)} \\ &= 5 \end{aligned} \tag{15}$$

These and other relations will be dealt with may be in future publications. However the author could not resist communicating yet another derivation of E(O) based on Newton's kinetic energy with a Weyl scaling made of the ratio of $D(4)$ to the difference between the exceptional manifold with $D = (5)$ ($\bar{\alpha}_o$) = 548 dimensions and the Heterotic manifold with 504 dimensions which leads to 4 excess dimensions leading to

$$E_N = \frac{m}{2} \left(\frac{4}{548 - 540} \right) (v \rightarrow c)^2 = \frac{1}{2} mc^2 \left(\frac{4}{44} \right) = mc^2 / 22 \tag{16}$$

In fact $548 - 540 = 44$ could be interpreted as $|SO(10)| = 45$ of GUT minus the single photon of Einstein, i.e. $45 - 1 = 44$ [28,29] apart of being the 44 components of a Vierbein [36]. Note also that 44 are the degrees of freedom of a massless graviton or pure gravity in $d = 11$ Witten M-theory [36].

4. Could $E = mc^2$ be a Quantum Gravity Formula – A Discussion beyond Convention

Both the P-Adic representation of $\bar{\alpha}_o = 137$ and more general Witten's T-duality [9, 36] lead us to consider the reality of the unit interval physics and that $E = \gamma mc^2 = mc^2$ states clearly that $\gamma = 1$ means $\bar{\alpha}_{OG} = 1$. Conversely $\bar{\alpha}_u = 22 + k$ means that $\gamma = 1 / \bar{\alpha}_u = 1 / (22 + k)$ and therefore the energy density is

$$E = m^2 / (22 + k) = E(\text{ordinary}) \tag{17}$$

In other words Witten's T-duality applies to the entire cosmos and could be interpreted as saying that Einstein discovered quantum gravity long before quantum mechanics was discovered. Was it genius, good luck or simply a case of Kostler sleep walking! That we will probably never know for sure but the fact that

$$E(O) + E(D) = mc^2 \tag{18}$$

where $E(O) = (\phi^5/2) mc^2$ and $E(D) = (5\phi^2/2) mc^2$ is indeed startling particularly when we realize that ϕ^5 is Hardy's experimentally verified probability of quantum entanglement [6] corresponding to the volume of the five dimensional zero set which models the quantum particle and $5\phi^2$ corresponds to the five dimensional volume of the empty set which models the quantum wave [10].

5. Conclusion

We showed in previous publications that dark energy could be determined from Rindler's spacetime [7,13]. On the other hand the Rindler wedge is usually considered a toy model for a black hole. Consequently this is by no means a toy model as is usually supposed, but a real model for the cosmos [7,13]. In a sense when Perlmutter, Schmidt and Rees measured the accelerated cosmic expansion [1-6] they were quasi-Rindler observers [7,13]. In the present work we demonstrated that it is sufficient to look at GUT unification, i.e. 10^{16} GeV using the giant form of 't Hooft-Polyakov monopole [30] to reach the same not only qualitative but also quantitative conclusions which we draw regarding dark energy from a fully Planck scale black hole unification, i.e. 10^{19} GeV [28]. The simplest ultimate validation of the present work comes however from noticing that gravity must have a profound effect on gauge forces coupling and that could be accounted for exactly via 't Hooft's dimensional regularization [37,38]. This is simply achieved by setting $\epsilon = 4 - D$ equal to $2\phi^5 = k$ and not letting $\epsilon \rightarrow 0$. That way one finds $E(\text{dark}) = [(4-k)/4]mc^2 \approx mc^2 (21/22)$ exactly as expected. The details of this analysis will be given in a forthcoming work.

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