

# Performance Optimization and Modelization of a Photovoltaic Pumping System

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**Abstract:** The photovoltaic (PV) pumping system is a widely used application in Mauritania to ensure the water supply in rural area for populations needs. The system is composed of a PV generator, a DC/DC converter, a DC/AC inverter, a BLDC motor and a centrifugal pump. Study in this article we study with simulation in Matlab/ Simulink environment the performances of the PV pumping system taking into account the climate parameters (solar irradiance, and ambient temperature), and the effect of the total manometric head (HMT) on the pumped flow rate. In addition it also counted the electrical energy and flow rate of the each climatic parameter. Two mathematical motor –pump models for PV application, were proposed in this article to contribute in the studies of PV pumping sizing. These models link directly the operating current to the voltage and electrical power to the flow rate of the pump versus total head.

**Keywords:** Generator Photovoltaic, System, Power, Converter, Motor-pump, Flow Rate, Total Manometric Head (HMT)

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## 1. Introduction

The water pumping system is one of the applications mostly used in the production of renewable energy. This application is used in the isolated areas (usually isolated mountain areas or rural areas) where we do not have the electricity grid [1].

The populations often use the PV pumping system for the household usage, the water that people need or for irrigation, so this is one of the factors that can play an important role for stability of the rural world life [2].

The dimensioning of PV pumping system studied in [3] and the efficiency of a PV pumping system are mainly based on the effect of solar irradiation. Several research projects have been carried out on the renewable energy conversion systems and their applications which can be summarized in the following two points:

1. The search for precise mathematical models that represent the real photovoltaic cell made it possible to retain the works of [4].
2. The selected models were designed to reflect correctly the influence of different atmospheric conditions on solar cell parameters. In this context, we must not forget to mention other works on optimization methods such as those of [5]. These methods are considered capable of determining the maximum power point of I (V) and P (V) characteristics of the photovoltaic cell.
3. The search for the development of a determined mathematical models, which represent the optimization of the hydraulic part, made it possible to retain the work of [6, 7]. It is also possible to list other works, such as

those of [8].

These different researches have had the objective of proposing a use of PV pumping for any lighting condition and temperature. In this pumping test facility we obtain, for each fixed pumping head, the pumped flow versus input voltage, simultaneously we measure the consumed current and therefore, we get the relation between the curves P-Q and I-V and the pumped flow rate is highly sensitive to the total manometric head (HMT), by comparing with the climatic parameters (solar irradiation and ambient temperature).

## 2. Description and Modeling of the Photovoltaic Pumping System

### 2.1. System Description

The system studied is shown in Figure 1, we have three parts that make up the PV pumping system; A PVG consisting of two PV panels connected in series with a capacity of 190 Wp for each, a DC/DC power converter, and a permanent magnet DC motor coupled directly to a centrifugal pump.

The PV panel parameters are shown in table 1. The Lorentz ps1200 c-sj8-5 used includes a multistage centrifugal pump, sensor less PM BLDC motor and a controller. The controller performances are shown in table 2 [9].

**Table 1.** Datasheet of the ASTROPOWER MODEL AP 190.

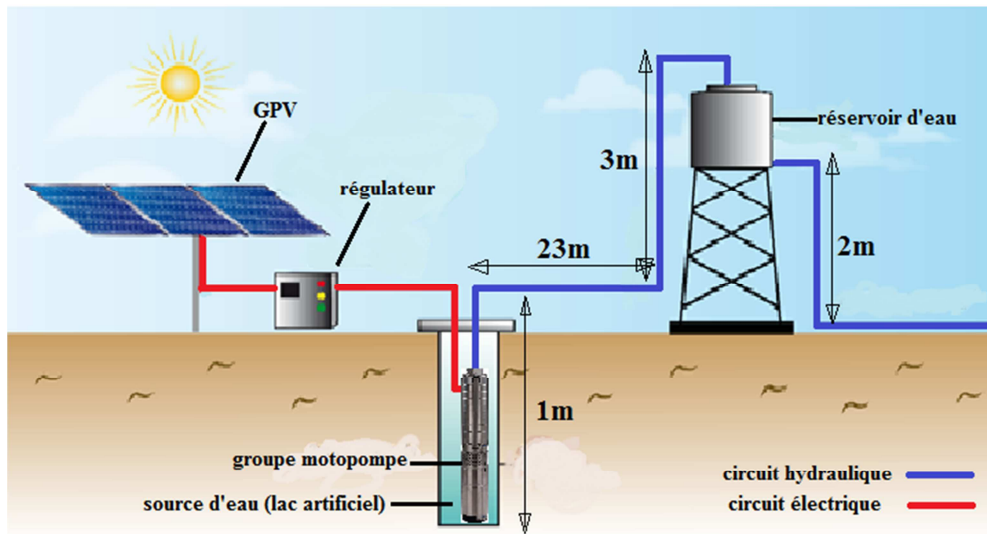
Parameters	Value
Rated power	190 watt
Rated voltage	25.8V
Rated current	7.36A
Open circuit voltage	32.3V
Short circuit current	8.18A

Photovoltaic module rated at  $1000\text{W/m}^2$  solar irradiation and  $25^\circ\text{C}$  cell temperature. The rated power of PV devices does not give an accurate indication of the outdoor performance, especially when the PV modules aren't a brand new one.

**Table 2.** Controller Performance.

Item # 1222	1222
Lift [m]	0-40m
max. flow rate [ $\text{m}^3/\text{h}$ ]	7.5
Max. efficiency [%]	48
PVG nominal voltage DC	72- 96V
PVG open circuit voltage DC	200V
Solar generator [Wp]	350-1200
Max. motor current (A)	9.5
Pump type	Centrifugal
Motor power	1.7kw
Motor rate	900-3300

This study was performed at the Higher Institute of Technological Education (ISET- Rosso) in Rosso-Mauritania ( $16^\circ30'$  North latitude,  $15^\circ48'$  West longitude at 8m altitude above the sea level).



**Figure 1.** The experimental setup.

### 2.2. Pumping System Modeling (Method)

These included parts giving the modeling of the PV panel, and the Pump motor modelization.

### 2.3. PVG System Modeling

A photovoltaic module is composed by photovoltaic cells, connected in series or in parallel, in literature we can find two types of PV cell modeling; the model with a single diode or the other with two diodes, [10], in our case, we use the a

single diode model Figure 2. This cell generates a current-voltage (I-V) characteristic that is strongly nonlinear, and so power (P-V).

In order to detect this point, an attempt is made to trace these two characteristics using a variable resistive load or an electronic load [11].

In this paper, we have chosen to work with the Luxor 190M model whose characteristic datasheet are presented in Table 1.

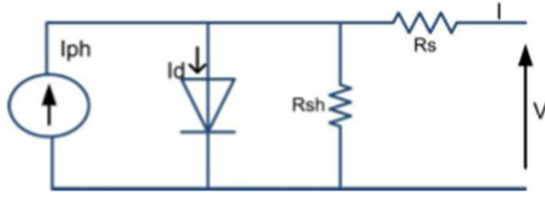


Figure 2. Electrical model of the photovoltaic cell.

From this circuit, and applying Kirchhoff's law, we shall derive the following equations:

$$I = I_{ph} - I_s \left( \exp \left( \frac{V + R_s I}{V_t} \right) - 1 \right) - \left( \frac{V + R_s I}{R_{sh}} \right) \quad (1)$$

with:  $V_t$ : the thermal tension written as  $(A * K * T) / q$ ,

$A$ : is the ideality factor of the diode, ( $K=1, 3805.10^{-38}$  J/K) is the Boltzmann constant,  $T$ : is the ambient temperature

in°C, ( $q=1.02 \times 10^{-19}$  C): is the electron charge,  $I_{ph}$ : is the photocurrent which is proportional to the solar irradiation flux,  $I_s$ : the diode saturation current,  $R_s$  and  $R_{sh}$ : are respectively the series and parallel resistance of the cell,  $V$  and  $I$ : are respectively the voltage and the current of the cell.

There are several characteristics of the solar cell that enables us to determine the working areas of the cell. PV cell displays none linear I-V and P-V characteristic curves. P-V curve represent the relation between the output voltage and power produced from the cell. Whereas the I-V curve represents the relation between the output current and voltage. The intersection of the curve with the y-axis gives the short circuit current and the intersection of the curve with the x-axis gives the open circuit voltage. Where the P-V curve colored green, the I-V curve colored blue. We plot the I-V and P-V characteristics of a module, shown in Figure 3.

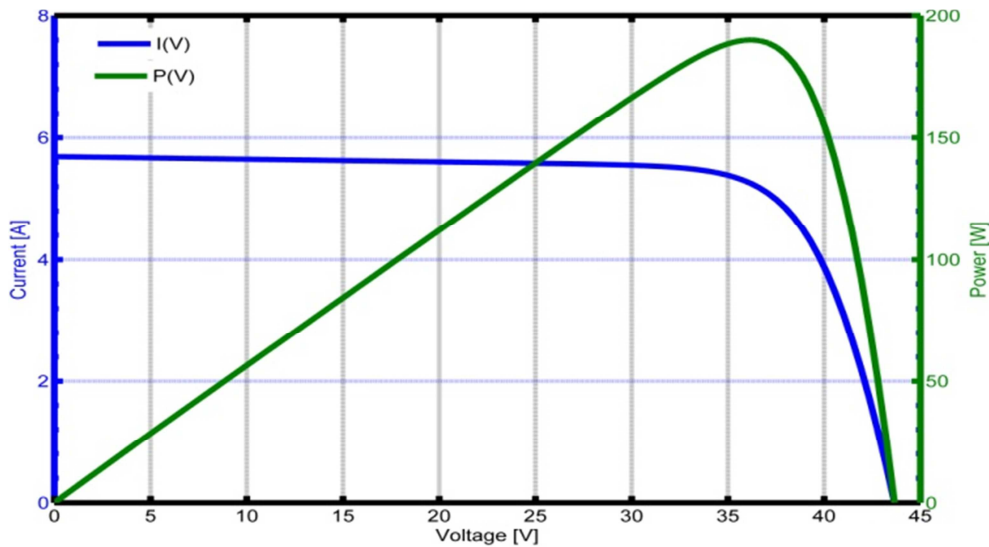


Figure 3. P-V Characteristic and I-V characteristic curve of a PVG.

#### 2.4. Motor-pump Modelization

There are several types of electrical motors that can be used to run the pump such as AC, DC, permanent magnet, brushed, brushless, synchronous and asynchronous, variable reluctance, and many more. If DC motor is used then the PV array could be directly connected to the motor, however the brushes of the motor needs to be changed regularly.

Using AC motor will require the use of an inverter between the PV and the motor. Normally, the motor and pump are built-in together for submersible and floating systems. In the surface system, it is possible to select the pump and motor separately and evaluate their performance [12].

The energy required to lift a certain amount of water over a certain height for a day is calculated from the required flow rate and total manometric head HMT data and is expressed in watt hours. This calculation is a function of a hydraulic constant ( $C_H$ ) and is inversely proportional to the efficiency of the pump set used.

The water flow rate required per day ( $m^3/s$ ) is calculated using on the following equation:

$$Q = \frac{R_p * E}{C_H * HMT} \quad (2)$$

where  $C_H$  is the hydraulic constant. The equation is given as follows:  $C_H = g\rho/3600$ , where ( $\rho=1000$  Kg/ $m^3$ ) is the density of water, ( $g = 9.81$  m/ $s^2$ ) is the acceleration due to gravity, 3600 is the number of second per hour, HMT is the total manometric head,  $Q$  is the flow rate ( $m^3/s$ ),  $E$  is the PV energy kWh and  $R_p$  is the subsystem (motor and pump) efficiency, with typical values range between 0.45- 0.55.

The mathematical models of the inverter and the motor pump set are described in a great number of research papers. Thus, we can quote [13].

These models describe the characteristics of each component of the pumping subsystem as the inverter, the motor or the pump. But these models do not give a direct relationship between the operating electrical powers of the pump.

In this paper, we use a mathematical model which directly links to the output water flow rate  $Q$  versus the input operating electric power  $P$  and total head  $h$ . this model is based on the analysis of the experimental results of one type

pumping subsystems [14].

With regard to the equation (3) connecting the characteristic

I-V of the pump with the pumping height and the equation (4) in form Q-V which develops characteristics to obtain the performance curves of the pump are proposed by the authors.

In the case of the current versus the voltage, we found that it is linear. In the case of the flow, the experimental points present a certain curvature; therefore it seems more suitable to use second-degree equation. For this reason, we suggested the following equation:

$$I(V) = aV + b \quad (3)$$

$$Q(V) = cV^2 + dV + e \quad (4)$$

With I and Q being positive. Where a, b, c, d and e are parameters easily obtained by means of an iterative Newton technique.

The researchers, generalized the model for all heights by linking all the coefficients a, b, c, d and e to the pumping height H by the following second-degree equations:

$$a(h) = a_0 + a_1h + a_2h^2 + a_3h^3 \quad (5)$$

$$b(h) = b_0 + b_1h + b_2h^2 + b_3h^3 \quad (6)$$

$$c(h) = c_0 + c_1h + c_2h^2 + c_3h^3 \quad (7)$$

$$d(h) = d_0 + d_1h + d_2h^2 + d_3h^3 \quad (8)$$

Where the constant  $a_i$ ,  $b_i$ ,  $c_i$  and  $d_i$  are the secondary parameters and depend only on the pumping subsystem type.

On the other hand, the model which gives P (Q) of the pump motor unit for different pumping heights has been developed by [15].

This model directly links the useful electrical power P a function to the water flow of the pump Q as follows:

$$P(Q, h) = a_0j(h)Q^3 + a_1j(h)Q^2 + a_2j(h)Q + a_3j(h) \quad (9)$$

The principal parameter  $a_{ij}(h)$  are constants depend of the pumping system.

### 3. System Performance Modeling

To evaluate the performance of the entire system, we will determine the performance of each subsystem [16]:

The PVG efficiency is calculated by the ratio between the electric power delivered, and the amount of sunshine  $E_s$  ( $W/m^2$ ) received on the surface  $S(m^2)$  of each PVG cell:

$$\eta_{pv} = \frac{P_{pv}}{E_s S N_s N_p} \quad (10)$$

The DC/DC Power converter efficiency is:

$$\eta_{cov} = \frac{P_{out}}{P_{pv}} = \frac{V_{out} I_{out}}{V_{pv} I_{pv}} \quad (11)$$

The motor pump system efficiency is:

$$\eta_{pump} = \frac{\rho g Q HMT}{3600 P_{out}} \quad (12)$$

where: ( $\rho = 1000 \text{ Kg/m}^3$ ) is the water density, ( $g = 9.8 \text{ m/s}^2$ ) is the gravitational constant, TMH is the total manometric head, Q is the flow rate ( $m^3/h$ ) and  $P_{out}$  is the DC/DC power converter output power.

Thus, the overall system efficiency is deduced [17].

$$\eta_{System} = \eta_{pv} \times \eta_{cov} \times \eta_{pump} \quad (13)$$

$$\eta_{System} = \frac{\rho g Q HMT}{3600 E_s S N_s N_p} \quad (14)$$

### 4. Results and Discussions

The solar irradiation variations during the experimentation and the ambient temperature variations are depicted and illustrated in Figure 4. The solar irradiation variations were in the range between 800 and 1200  $W/m^2$ , with an average value of about 920  $W/m^2$ . The ambient temperature is influencing the radiation and convective heat loss from the top surface of the photovoltaic panel.

During experimentation, the ambient temperature was varied between 21°C to about 41°C, with an average value of about 29.2°C. Similar ambient temperature variations were observed.

Station name	Serial	Start date/time	End date/time	Altitude	Longitude	Latitude
DGAB weather	000009D4	2018-09-13 18:00	2018-10-14 17:00	10	-15.777668°	16.523834°

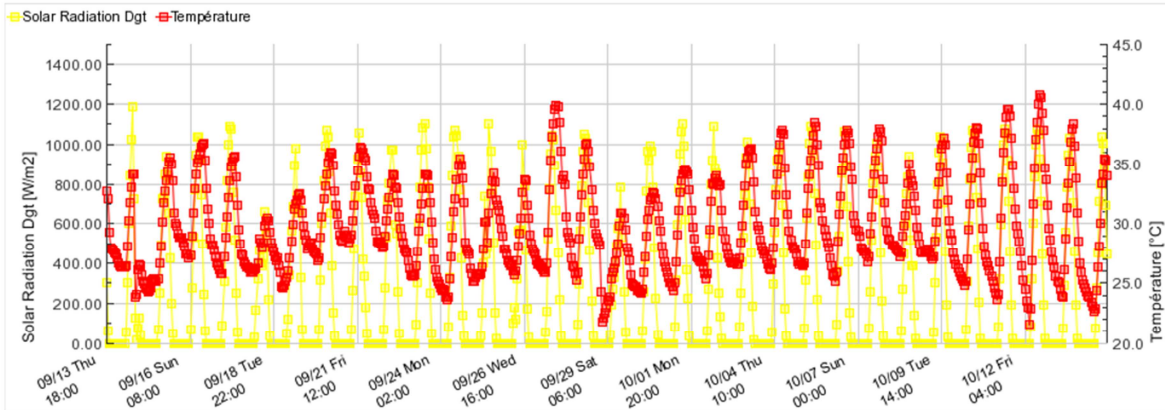


Figure 4. Variation of solar irradiation and ambient temperature.



Figures 5 and 6 show the performance of the stations during a sunny day and cloudy day. The maximum global irradiance was  $1300 \text{ W/m}^2$  (sunny day) and  $1200 \text{ W/m}^2$  (cloudy day).

The maximum temperature of the PV module was  $45^\circ\text{C}$  Figure 5 (sunny day), and  $33^\circ\text{C}$  Figure 6 (cloudy day).

Figures 5 and 6 show the performance of the station during

a sunny day, and cloudy day. The maximum of the electrical energy during the day was  $1100 \text{ Wh/day}$  (sunny day), and  $1000 \text{ wh/day}$  (cloudy day).

Final, Figures 5 and 6 show the result of the variations of the water flow rate, the maximum  $10 \text{ m}^3/\text{h}$  (sunny day), and  $5 \text{ m}^3/\text{h}$  (cloudy day).

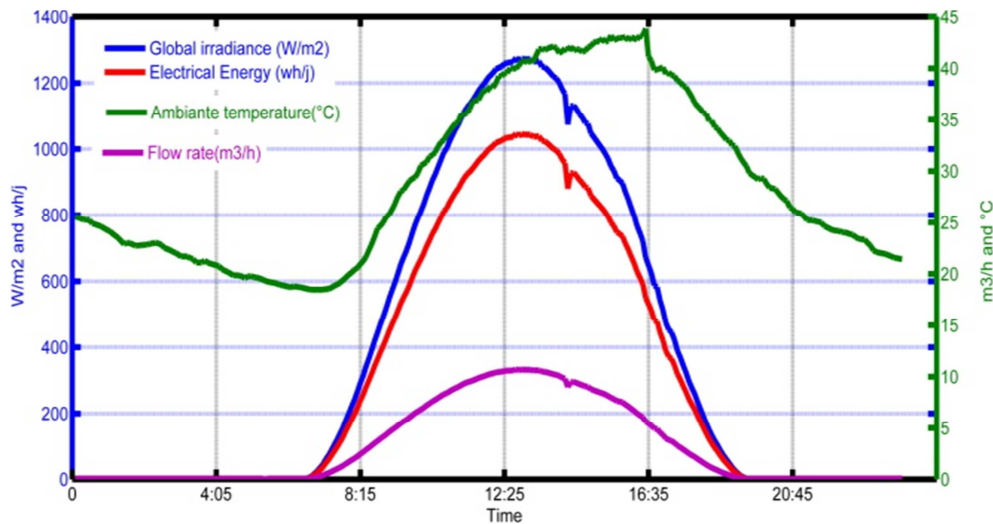


Figure 5. Performance of Solar water pumping station in sunny day.

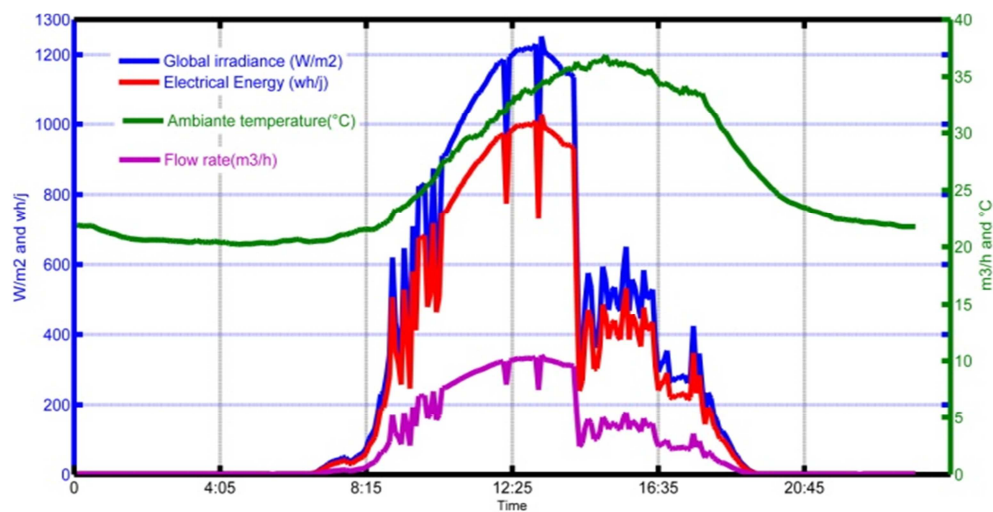


Figure 6. Performance of solar water pumping station in cloudy day.

The simulations are developed to obtain the models parameters applied to pump motor. It is necessary to physically separate the pump motor to develop in the rest of this work, simulations of current-voltage characteristics  $I(V)$  and the power-flow  $P(Q)$ . For each head, we obtained two measured curves: the  $I-V$  and the  $P-Q$  relationship of the motor pump.

Figure 7 illustrates an example of the characteristics obtained for the pump centrifugal using the experimental measurement, which represent the dependence of the current versus to the voltage for each head. From the result, we found a simple mathematical expression, which allows us to adjust the experimental value. In the case of the current versus, the voltage, it is linear equation.

The  $P(Q)$  characteristics of the one tested subsystem are carried out and plotted for each total head.

An example of the measurement values are shown in Figure 8. This represents the dependence of the electrical power,  $P$  versus to the flow rate,  $Q$  the analysis a simple mathematical mode.

Figures 9 and 10 show an example of the experimental values obtained for one head. Thus to define the  $I-V$  and  $P-Q$  characteristics, we need to solve of a linear equations.

In order to validate the obtained general models, a comparative study of the previous and the present characteristics was made. In Figures 9 and 10, we illustrated the previous and the present characteristics of the centrifugal

pump head. As shown in Figures 9 and 10 the curves agree very well.

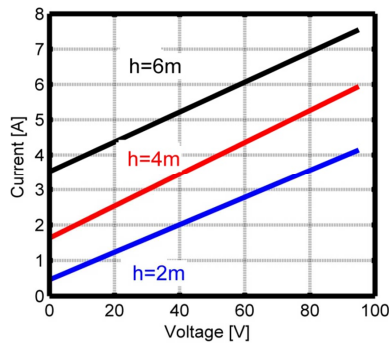


Figure 7. Characteristics current-voltage for pump for different heads.

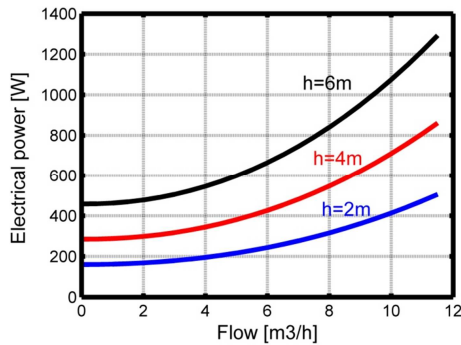


Figure 8. Characteristics Electrical power - flow rate for pump for different heads.

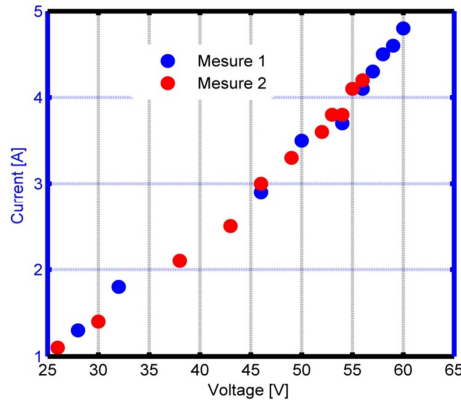


Figure 9. Characteristics current-voltage curve model validation.

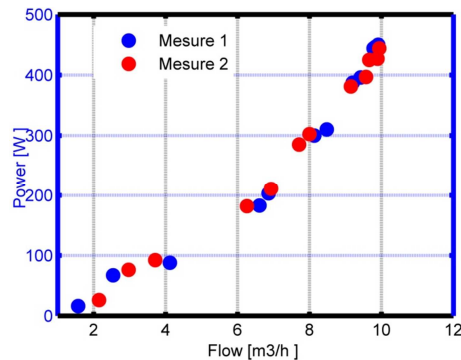


Figure 10. Characteristics Electrical power - flow rate curve model validation.

## 5. Conclusions

In this research a PV water pumping system in Mauritania climate has been designed. A case study for a small farm in the Higher Institute Technological Education (ISET- Rosso) was selected and discussed. This system is suitable for many rural zones since it's designed to work with free cost and doesn't need maintenance. The modelization and the validation of the models of the PV array and the PV pumping subsystem, allow us to simulate the performance of the PV pumping systems for several sites. The analytical model has given a great adjustment of the I-V electrical characteristic curves of the PV array versus solare irradiance and ambiante temperature. Concerning the pumping subsystems, the model for current-voltage and power-flow of PV array is found to agree with experimental curves. The development of the one motor-pump unit models allows us to obtain the operating point of the system and the pumped flow rate. The one model is based on experimental result of several photovoltaic pumps, which have been characterized completely in the pumping test facility to obtain the parameter of the model. The models are established for centrifugal pump (Lorentz ps1200 c-sj8-5) with DC motor.

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