

The Application of ARIMA Model in 2014 Shanghai Composite Stock Price Index

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Abstract: In order to study the changes of Shanghai Composite Stock Price Index (SCSPI) and predict the trend of stock market fluctuations, this paper constructed a time-series analysis. A non-stationary trend is found, and an ARIMA model is found to sufficiently model the data. A short trend of Shanghai composite stock price index is then predicted using the established model.

Keywords: The Shanghai Composite Stock Price Index (SCSPI), Prediction, ARIMA Model

1. Introduction

There are more than 3000 stocks in China stock market, and Shanghai Composite Stock Price Index (SCSPI) is a good representatives for all the stocks in China market. SCSPI is the first release of the stock index in China, and it is calculated based on all the stocks in Shanghai stock market. In the financial industry of China, the prediction of Shanghai composite stock price index is always a high-profile topic, which is useful in avoiding the risk of investment interests, and also in reflecting the changes of structure, activities and trends of China macro-economic. If investors can accurately predict the stock market trend, the invest risk can be reduced and the benefits can be maximized. Thus, scientific and reasonable forecast of stock index really vital to financial practices.

A lot of methods have been used for SCSPI, including autoregressive model, autoregressive moving average model, autoregressive conditional heteroscedasticity model, autoregressive integrated moving average model (ARIMA) and so on. In the balance of predict and explanation, ARIMA is a wildly used model. In this paper, the SCSPI data of 2014 is firstly examined and then ARIMA model is used to fitted the data.

Stock price forecasting are most concerned about the stock opening price, closing price, the highest price, the lowest price and volume. In technical analysis, the highest and lowest price represents the comprehensive fighting among multi outer forces. The transacted volume represents the

market activity and popularity, and the closing price is on behalf of the balance from the multi contest, which can be seen as the opening price of the next trading day. According to the technical analysis theory and the basic hypothesis, a trading day closing price is not only associated with the previous trading day closing price, the highest price, the lowest price and volume, but also with the historical trading day's closing price, the highest price, low price and volume. In view of the important role in the analysis of stock market closing price, the SCSPI data used in this paper is based on closing prices of the stocks, in the time span of January 2, 2014 to December 31, 2014, with 234 observations. The Data is obtained from the financial part of Sina.com. A short list of the data can be seen in Table 1. All computations are done by using SAS software (SAS® 9.2, SAS Institute Inc., Cary, N.C.).

2. ARIMA Modeling

2.1. ARIMA Model

In statistics and econometrics, and in particular in time series analysis, an autoregressive integrated moving average (ARIMA) model is a generalization of an autoregressive moving average (ARMA) model. These models are fitted to time series data either to better understand the data or to predict future points in the series (forecasting). They are applied in some cases where data show evidence of

non-stationarity, where an initial differencing step (corresponding to the "integrated" part of the model) can be applied to reduce the non-stationarity. Non-seasonal ARIMA models are generally denoted ARIMA (p, d, q) where parameters p, d, and q are non-negative integers, p is the order of the Autoregressive model, d is the degree of differencing, and q is the order of the Moving-average model. Seasonal ARIMA models are usually denoted ARIMA (p, d, q) (P, D, Q), where m refers to the number of periods in each

season, and the uppercase P, D, Q refer to the autoregressive, differencing, and moving average terms for the seasonal part of the ARIMA model. ARIMA models form an important part of the Box-Jenkins approach to time-series modelling.

When two out of the three terms are zeros, the model may be referred to based on the non-zero parameter, dropping "AR", "I" or "MA" from the acronym describing the model. For example, ARIMA (1,0,0) is AR(1), ARIMA(0,1,0) is I(1), and ARIMA(0,0,1) is MA(1).

Table 1. A short list of the SCSPI data in 2014, which contains transaction date, open price, maximum price, close price, minimum price, volume and transaction amount.

Date	Open Price	Max Price	Close price	Min price	Volume	Transaction Amount (China Yuan)
2014/1/2	2112.126	2113.11	2109.387	2101.016	6848548800	61921353728
2014/1/3	2101.542	2102.167	2083.136	2075.899	8449724000	72372232192
2014/1/6	2078.684	2078.684	2045.709	2034.006	8958760800	72895397888
2014/1/7	2034.224	2052.279	2047.317	2029.246	6340293600	54638641152
2014/1/8	2047.256	2062.952	2044.34	2037.11	7164736000	62941429760
2014/1/9	2041.773	2057.196	2027.622	2026.446	7594188000	67605663744
2014/1/10	2023.535	2029.297	2013.298	2008.007	7561612000	61044551680
2014/1/13	2014.978	2027.181	2009.564	2000.404	6654477600	55616749568
2014/1/14	2007.156	2027.428	2026.842	2001.135	7036661600	56687624192
2014/1/15	2024.228	2027.409	2023.348	2010.204	6743622400	57740357632
2014/1/16	2022.538	2034.707	2023.701	2014.407	7275572000	62829760512
2014/1/17	2017.522	2017.868	2004.949	2001.33	6730572000	57039564800
2014/1/20	2001.894	2005.938	1991.253	1984.824	5627124800	48298782720
2014/1/21	1992.015	2014.152	2008.313	1992.015	5984491200	52017917952
2014/1/22	2009.969	2052.339	2051.749	2008.93	9889285600	84126662656
2014/1/23	2048.331	2052.528	2042.18	2039.052	8421058400	76083322880
2014/1/24	2037.667	2060.986	2054.392	2034.453	9294792000	82346180608
2014/1/27	2044.272	2044.846	2033.3	2029.626	8881542400	81914216448
2014/1/28	2036.402	2047.129	2038.513	2026.987	7252904000	65751605248
2014/1/29	2042.176	2051.583	2049.914	2039.771	7386546400	67694125056
2014/1/30	2045.931	2045.931	2033.083	2031.466	6261518400	58264498176

2.2. Building Stationary Sequence

A timing diagram is firstly plot using all the SCSPI data of 2014 based on closing stocks price. As shown in Figure 1, a clear increasing trend can be found from the diagram, which is corresponding the increasing China economics. The SCSPI changes from around 2100 points in the beginning to around 3250 points in the end of year 2014. The increasing trend breaks the hypotheses of weaker stationary. In many application cases, the weaker stationary is used instead of strongly stationary.

A weaker form of stationarity commonly employed in time series is known as second-order stationarity, which only require that 1st moment and auto-covariance do not vary with respect to time. So, for a continuous-time random process $x(t)$, it has the following properties: the mean function $E\{x(t)\}$ must be constant and the covariance function depends only on the difference between t_1 and t_2 and only needs to be indexed by one variable rather than two variables.

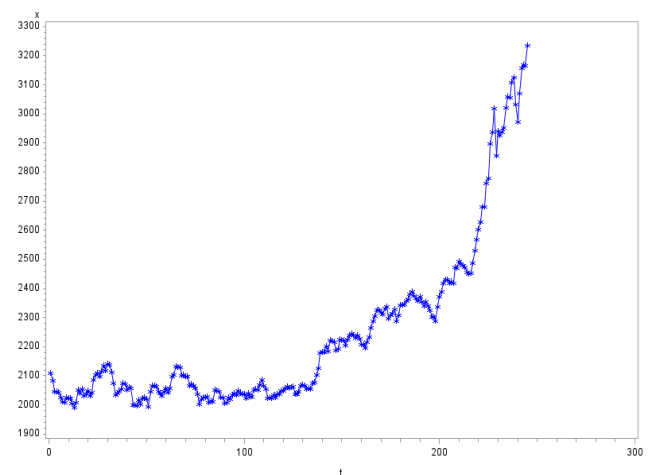


Figure 1. The timing diagram plot of SCSPI data of 2014 based on closing stocks price.

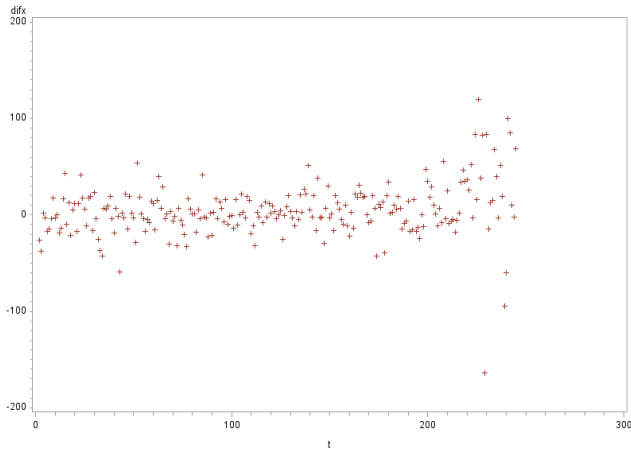


Figure 2. The timing diagram plot of the First order differencing data on SCSPI data of 2014 based on closing stocks price.

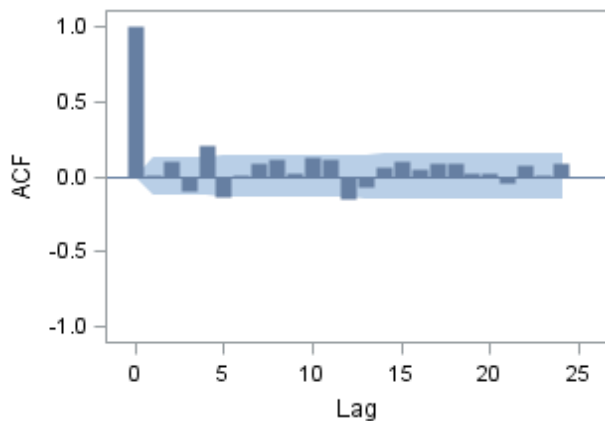


Figure 3. The Autocorrelogram on the first order differencing data of original SCSPI data.

Following ARIMA model procedure, a First order differencing is computed for the data, and then a timing diagram of the differencing data is computed and shown in Figure 2. The differencing data shows a stationary pattern, and an Autocorrelogram (Figure 3) is also done on the differencing data, which displays a short-term autocorrelation and confirms the stationarity of the differencing data. To make an accurate inference of the data, autocorrelation check for white noise is also done on the differencing data. As shown in Table 2, the white noise hypotheses is rejected on lag 6, 12, 18 and 24 with very small p-values. All these results shows that an ARMA model can be fitted to the first order differencing data.

2.3. ARIMA Modeling

The basic idea of ARIMA model is to view the data sequence as formed by a Stochastic Process on time. Once the model has been identified, the model can be used to predict the future value from the past and present value of the time series. Modern statistical methods and econometric models have been able to help companies predict the future in a certain way.

Firstly, the scatter plots of time series, self-correlation function and partial auto correlation function plot are used to test its variance, trend and seasonal variation, stability of sequence recognition. For general applications, the time series of economic events are not stationary series. The next step is to do some data manipulation on the non-stationary sequence. If the data series is non-stationary, and there is a certain growth or decline, the data difference is need to be proceed. If the heteroskedasticity is in the data, the technical data processing is required. After the data processing, the correlation function value and partial correlation function values should be not significantly different from zero.

Table 2. Autocorrelation check for white noise on the differencing data at lag 6, 12, 18 and 24.

Autocorrelation Check for White Noise									
Lag	Chi-Square	DF	P-Value	Autocorrelations					
6	20.85	6	0.0019	0.012	0.101	-0.099	0.210	-0.138	0.007
12	39.10	12	0.0001	0.089	0.116	0.018	0.123	0.113	-0.147
18	48.73	18	0.0001	-0.076	0.056	0.1	0.048	0.085	0.090
24	52.98	24	0.0006	0.019	0.024	-0.041	0.067	0.014	0.091

According to the identification rules on time series, the corresponding model can be established. If a partial correlation function of a stationary sequence is truncated, and self-correlation function is tailed, it can be concluded the sequences for AR model; if partial correlation function of a stationary sequence is tailed, and the self-correlation function is truncated, it can be determined that the MA model can be fitted for the sequence. If the partial correlation function of a stationary sequence and the auto-correlation function are trailed, then the ARMA model is suitable for the sequence.

Based on the results from section 2.2, an ARIMA model can be fitted to the original SCSPI data of 2014, and the parameters in ARIMA (p, 1, q) need to be determined then. From the Figure 3 of the Autocorrelogram, it is safe to determine that q is no more than 3, while as shown in Figure 4,

the partial autocorrelation is also no more than 3. This means that it is enough to choose the model in the set of $\{p \leq 3 \text{ and } q \leq 3\}$.

At the significant level of 0.05, no model in the forms of ARIMA (p, 1, 0) can be found which makes the coefficients of AR part are significantly different from 0. The same result can also be found in the models with the forms of ARIMA (0, 1, q). In the models in ARIMA (p, 1, q), two models (ARIMA (1,1,1) and ARIMA (2,1,1)) are found with all coefficients are significantly different from 0. The model ARIMA (1,1, 1) is chosen as it contains fewer coefficients than ARIMA (2,1,1), although the AIC of the former model are larger than the later one but only with the amount of 0.439, 0.02% the AIC amount of ARIMA (2,1,1).

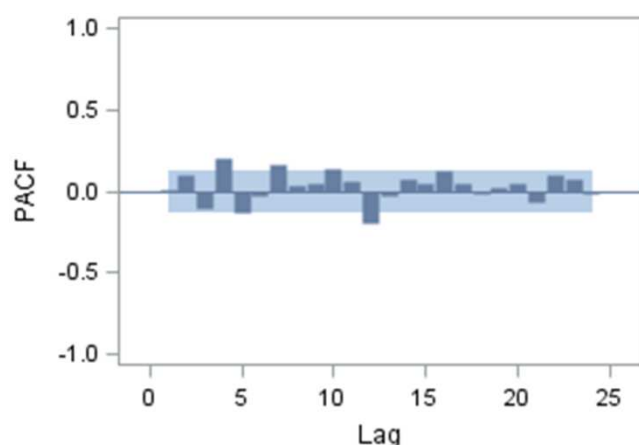


Figure 4. The partial Autocorrelogram on the first order differencing data of original SCSPI data.

The final model is

$$(1 - B)\nabla x_t = (1 - 0.98635B)\varepsilon_t,$$

which can also be written as

$$x_t = 2x_{t-1} - x_{t-2} + \varepsilon_t - 0.98635\varepsilon_{t-1}.$$

Using the built model, five steps prediction can be done and compared with the actual value, which are listed in Table 3 and Figure 5. As shown in Table 3, the forecast value is around 3255 and with a relative small standard error, which is also reflected in the 95% confidence limits.

Table 3. The next 5 steps prediction of actual SCSPI value based on the final model. The predicted value are shown with the standard error and 95% confidence limits.

Forecasts for variable x(t)				
Obs	Forecast	Std Error	95% Confidence Limits	
246	3245.2351	27.3885	3191.5545	3298.9156
247	3255.7931	38.9985	3179.3575	3332.2287
248	3266.3511	48.0887	3172.0990	3360.6032
249	3276.9091	55.9048	3167.3378	3386.4804
250	3287.4671	62.9255	3164.1354	3410.7987

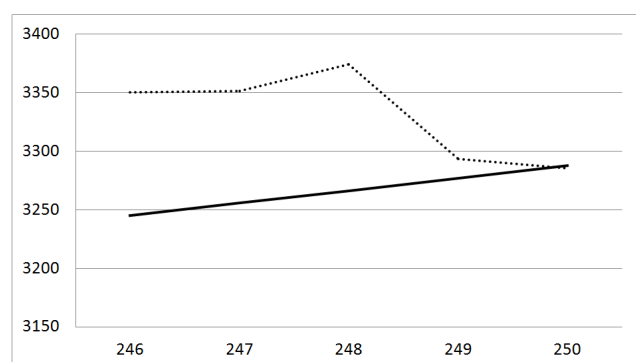


Figure 5. The dash line is draw by the actual SCSPI value, while the solid line is from the predicted values.

Although the predicted values is a little different from actual value, the increasing trend is agreed in the 3 steps, which is enough for financial practice. The fluctuation of

SCSPI is can be caused by many factors, such as China financial police, international financial events and polices. The fluctuations of stocks are non-rational, and it is influenced by many factors. No model can include all these factors. The most frequent reason which makes the stock suddenly appeared on big sell-off is the country and the global financial policy and current affairs. For example, in January 19, 2015, a lot of stocks in Shanghai stock markets are plummeted, and all financial stocks, such as brokerage stocks and bank stocks are plummeted. The Shanghai Composite Index closing price decreased from 3376.495 points down to 3116.351 points, by 260.144 points, and fell 7.70%. The main reasons is that on last weekend China Securities Regulatory Commission announced the two financial inspection and punishing results: CITIC Securities, Haitong Securities, and Guotai Junan Securities are not allowed to open new credit accounts for three months, and a number of brokers have been criticized. In addition, at the same time Swiss central bank unexpectedly announced that CHF cancelled against the euro exchange rate cap, which make CHF rise and the euro exchange rate hit a new low. By the effect of this unexpected news and weaker economic data, the United States stock indexes decreased in the next five days. The resulting turmoil in the international financial markets are also affected to China stocks markets in some extent.

3. Conclusions

This paper does a study on 2014 Shanghai Composite Stock Price Index (SCSPI). In the process of model building, the original SCSPI data is found to be un-stationary, but the first order differencing data of original SCSPI data is stationary. By comparing with several models, ARIMA (1, 1, 1) is chosen as the final model and it succeeds in predicting three steps trends of SCSPI. Considering the fluctuations of SCSPI, this model can be applied in finance practices. The fluctuations of stocks are non-rational, and it is influenced by many factors. No model can include all these factors. Although the predicted values from the suggested model is a little different from actual value, the increasing trend is agreed in the 3 steps, which is enough for financial practice. That is because in the financial practice it is very perfect to make an investment to assure a coming profit.

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